Connecting Large Scale Structures to galactic spin

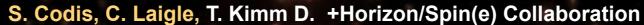


Christophe Pichon

KIAS /IAP

Can we predict the spin of galaxies on the cosmic web from first principles?

Halo



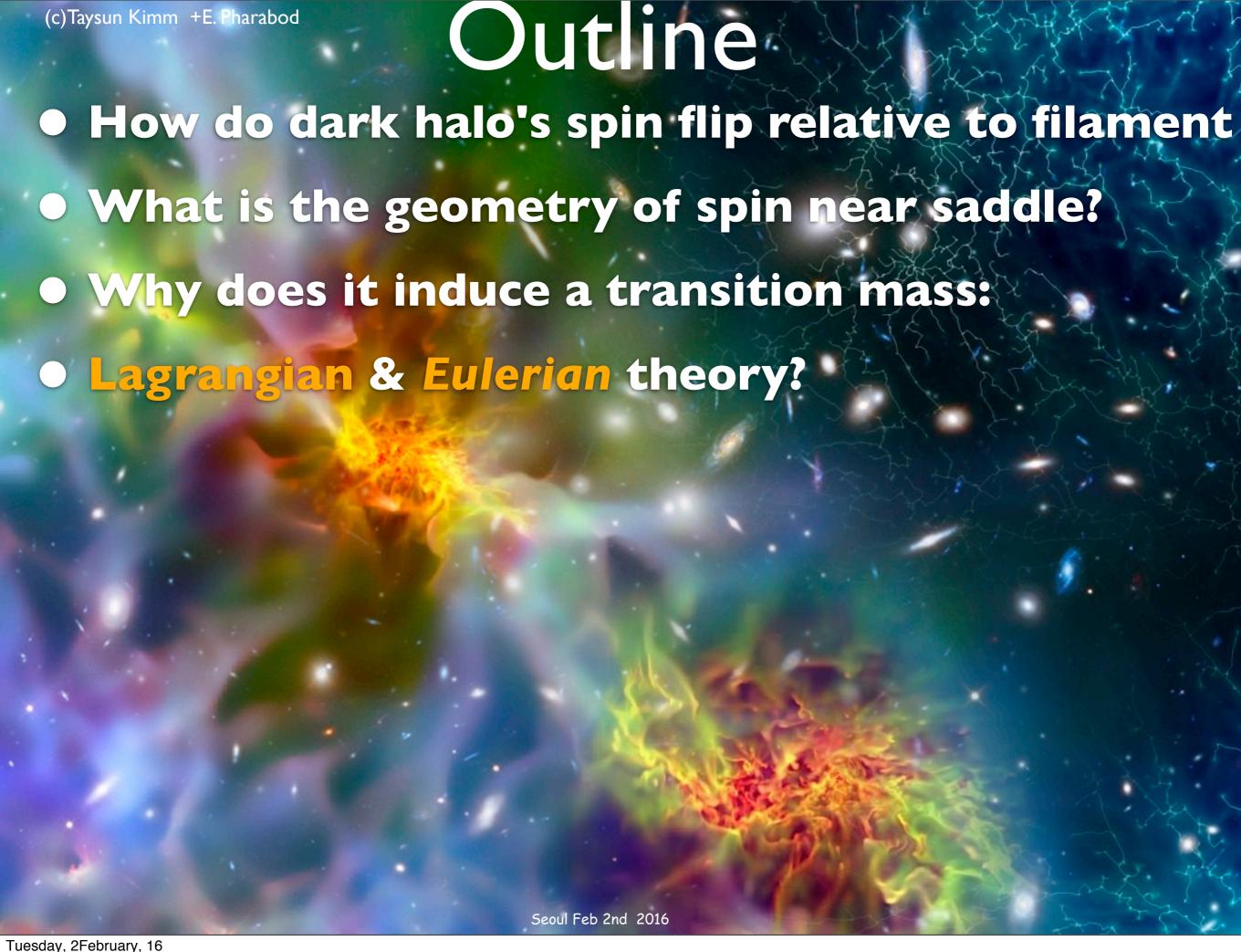
 $t_{
m dyn} \sim 1/\sqrt{
ho}$

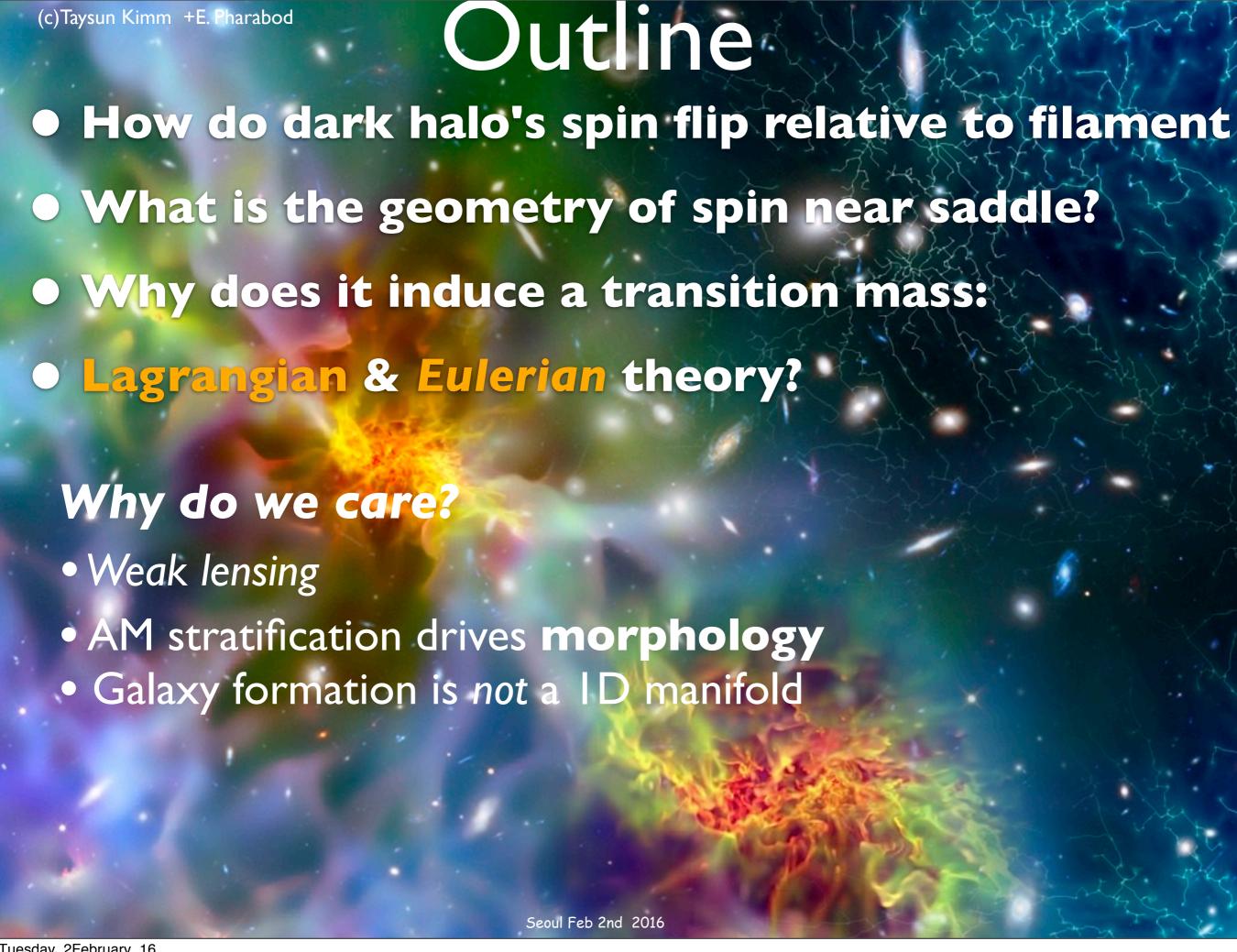
Seoul Feb 2nd 2016

Filaments

Large Scale Structures

Galaxy





Outline

- How do dark halo's spin flip relative to filament
- What is the geometry of spin near saddle?
- Why does it induce a transition mass:
- Lagrangian & Eulerian theory?

Why do we care?

- Weak lensing
- AM stratification drives morphology
- Galaxy formation is not a ID manifold

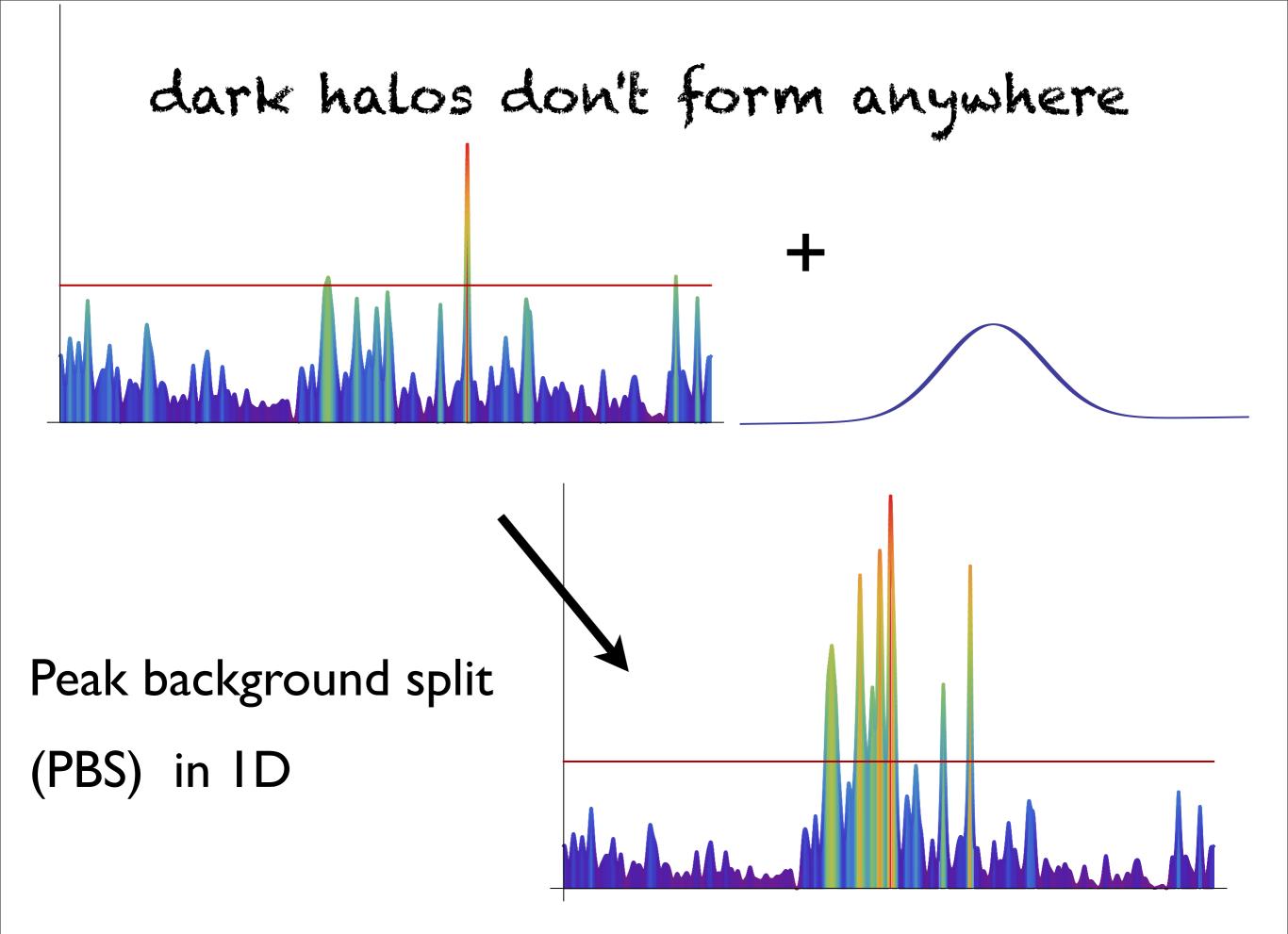
Where galaxies form does matter, and can be traced back to ICs.
Flattened filaments generate point-reflection-symmetric AM/vorticity distribution:
they induce the observed spin transition mass

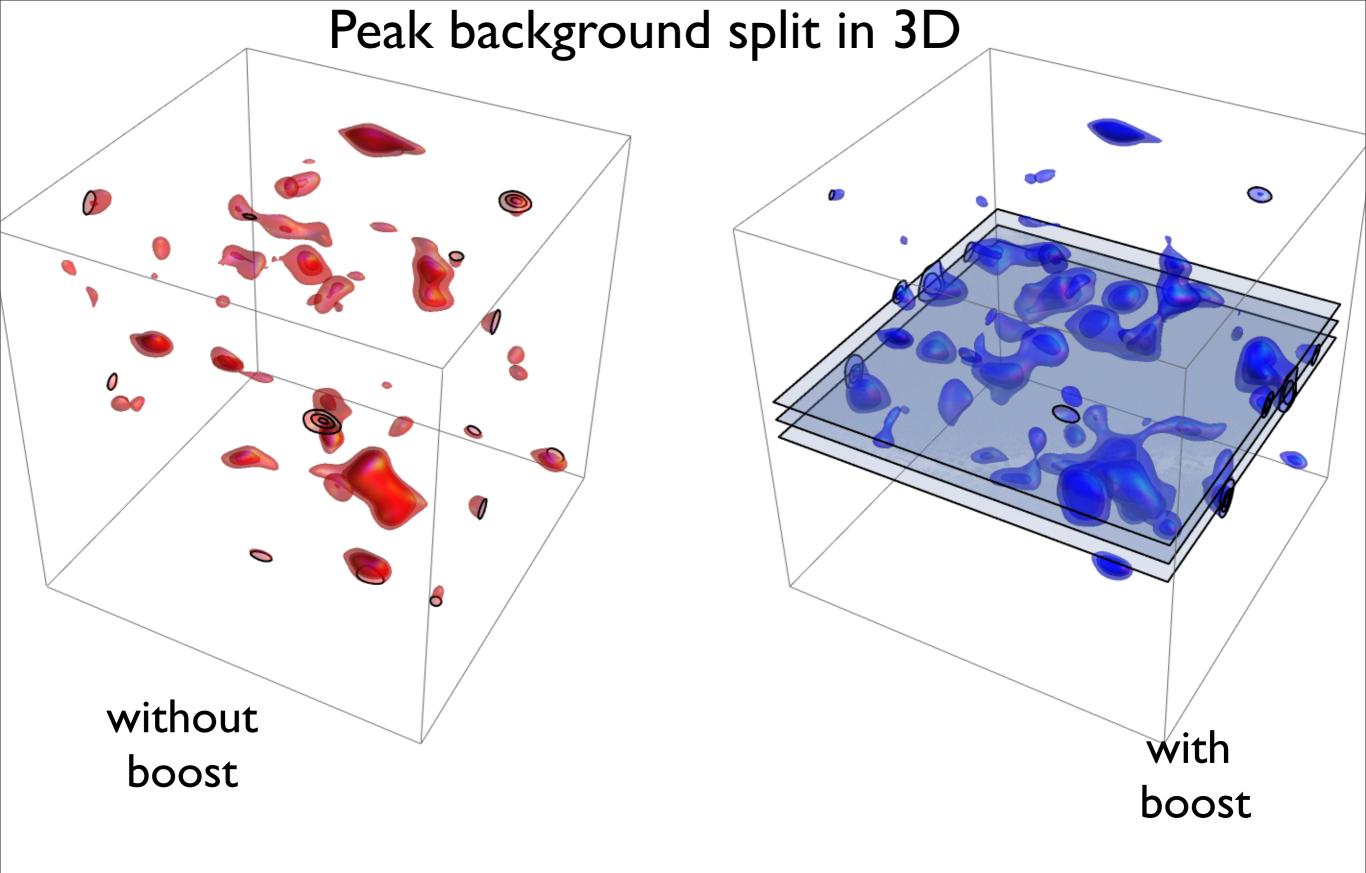
Seoul Feb 2nd 2016

PART I

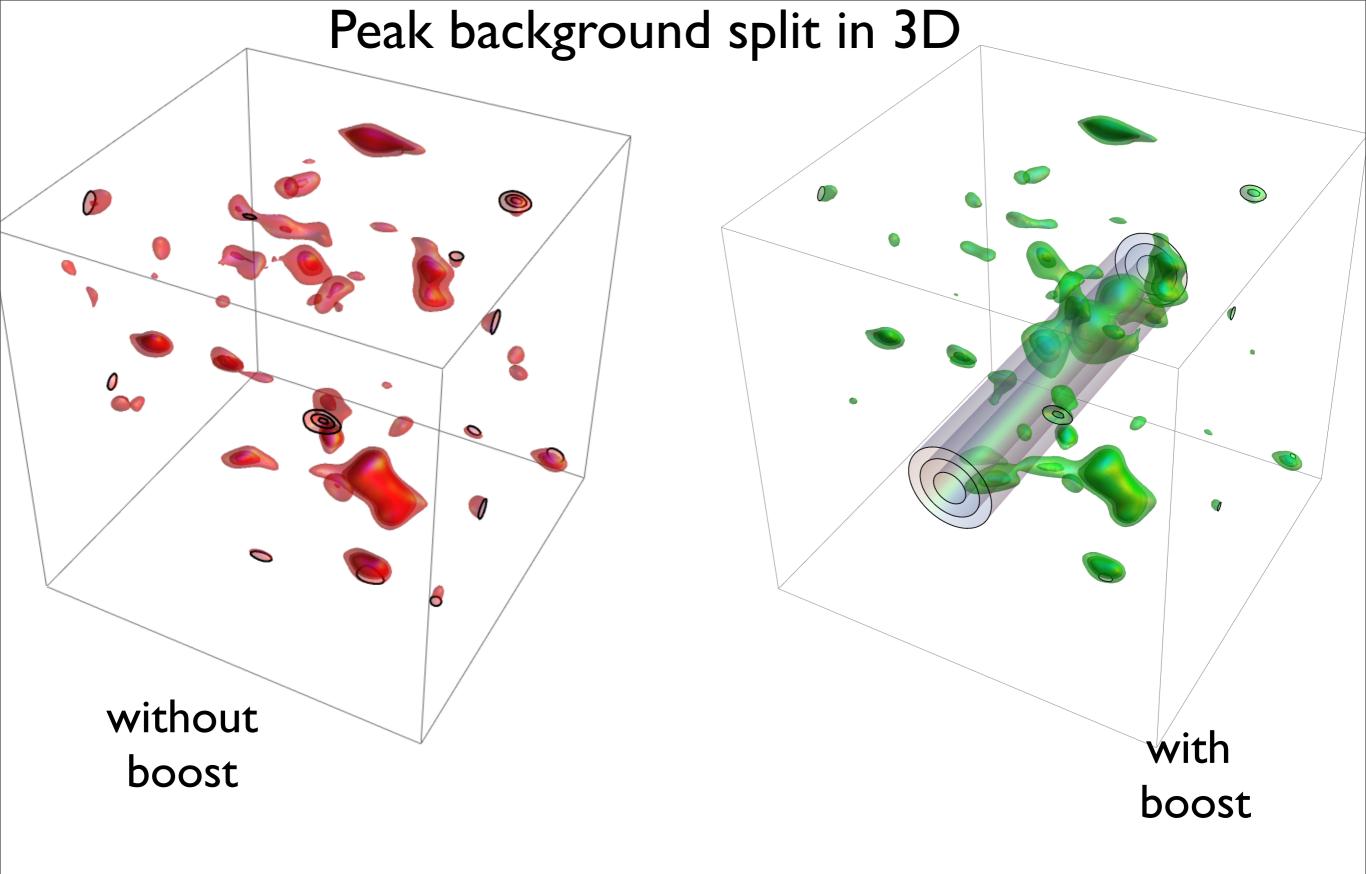
What's happening on large scales?

How is the cosmic web woven?
i.e Where do galaxies form in our Universe?
What are the dynamical implications?





Does this anisotropic biassing have a dynamical signature? yes! in term of spin!



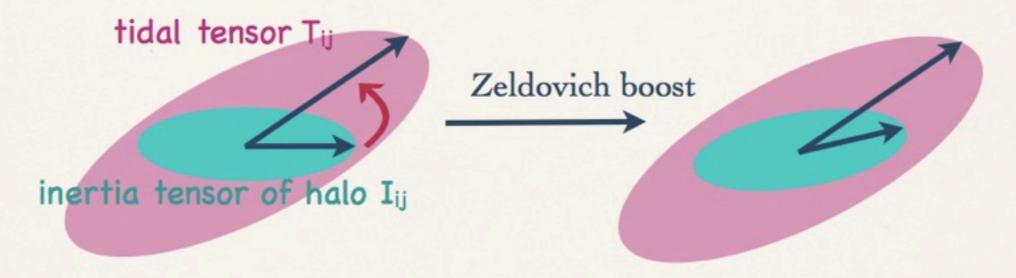
Does this anisotropic biassing have a dynamical signature? yes! in term of spin!

Tidal Torque Theory in one cartoon

Can we understand where spin and vorticity alignments come from?

-usual tidal torque theory

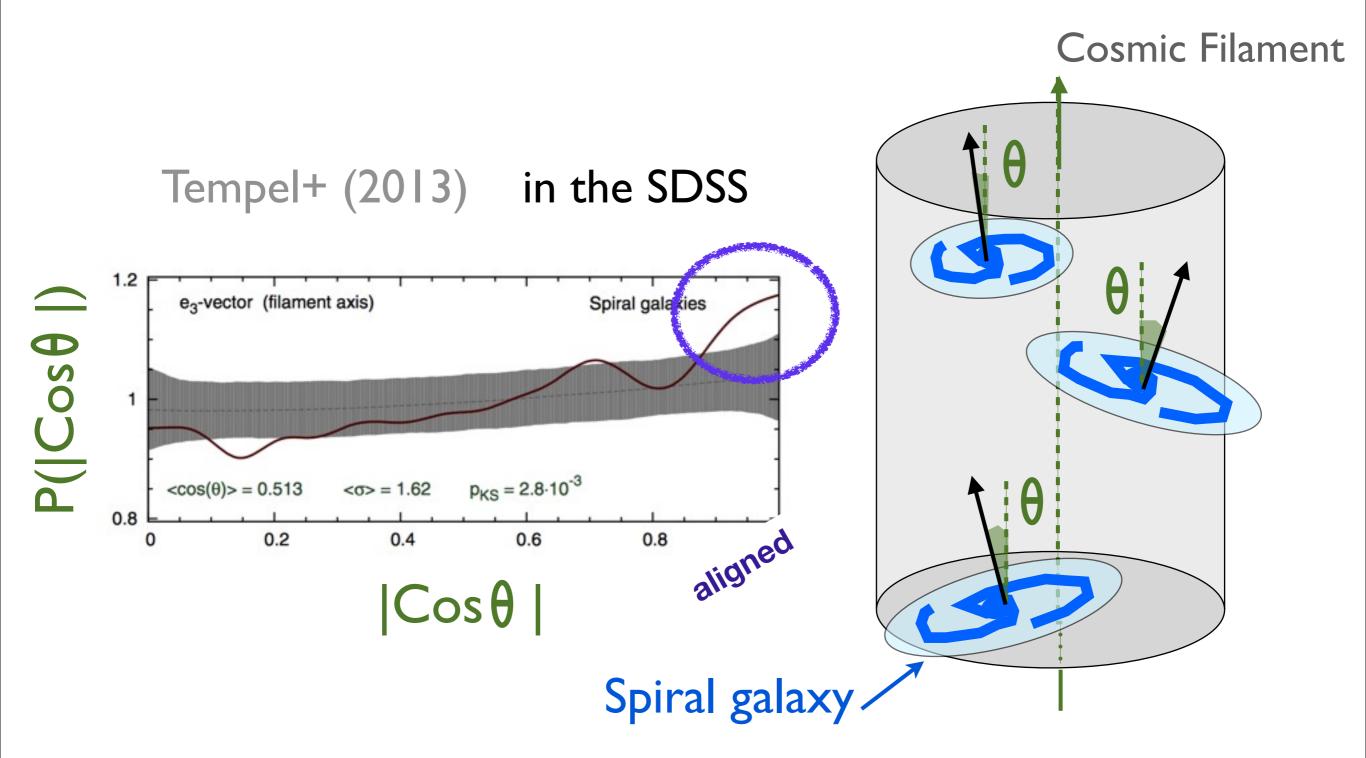
$$L_k = \varepsilon_{ijk} \, I_{li} \, T_{lj}$$



YES! via conditional TTT subject to saddle

Et Voilà!

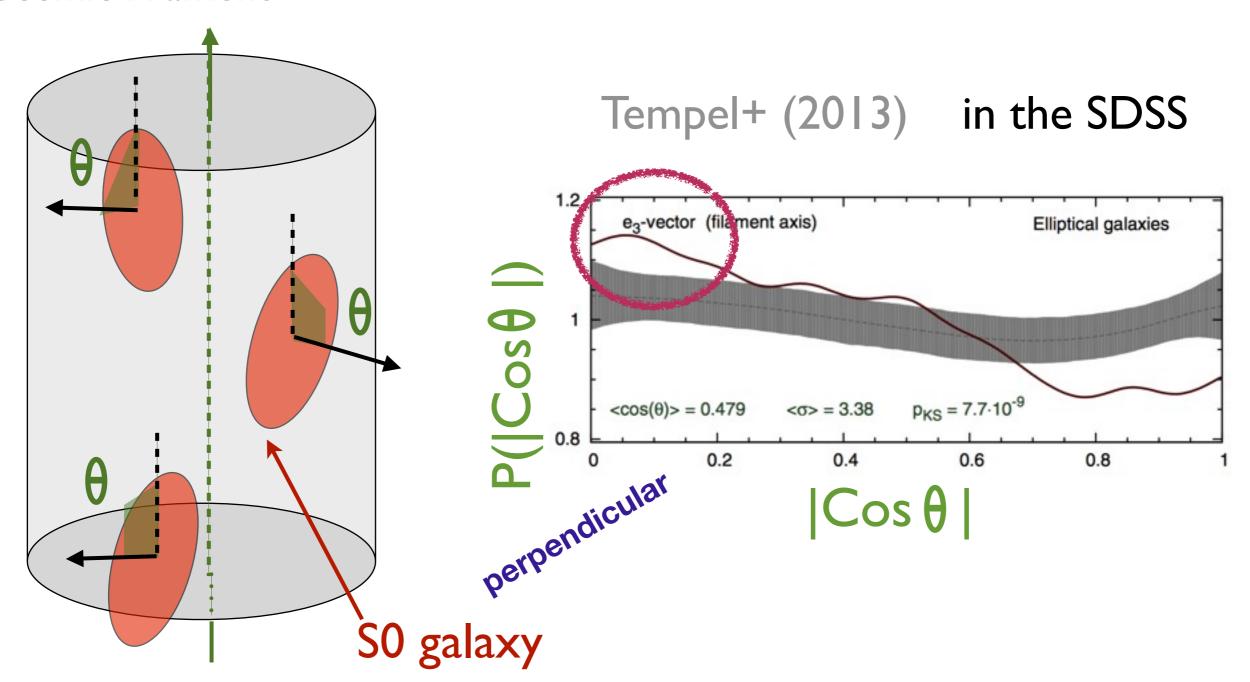
Evidences of galaxy spin - filament alignment



See also: Aragon-Calvo+ 2007, Hahn+ 2007, Paz+ 2008, Zhang+ 2009, Codis+ 2012, Libeskind+ 2013, Aragon-Calvo 2013, Dubois+ 2014

Evidences of galaxy spin - filament alignment

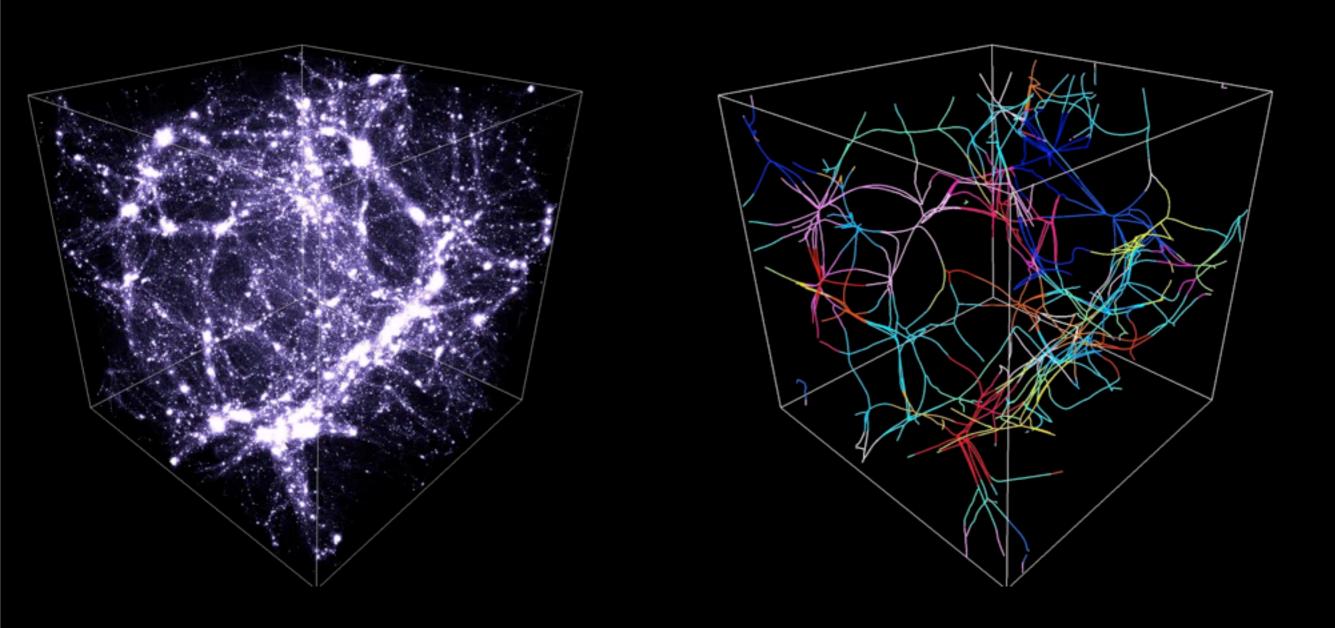
Cosmic Filament



See also:

Aragon-Calvo+ 2007, Hahn+ 2007, Paz+ 2008, Zhang+ 2009, Codis+ 2012, Libeskind+ 2013, Aragon-Calvo 2013, Dubois+ 2014

Skeleton of the LSS



traces filaments via crest lines of the density field

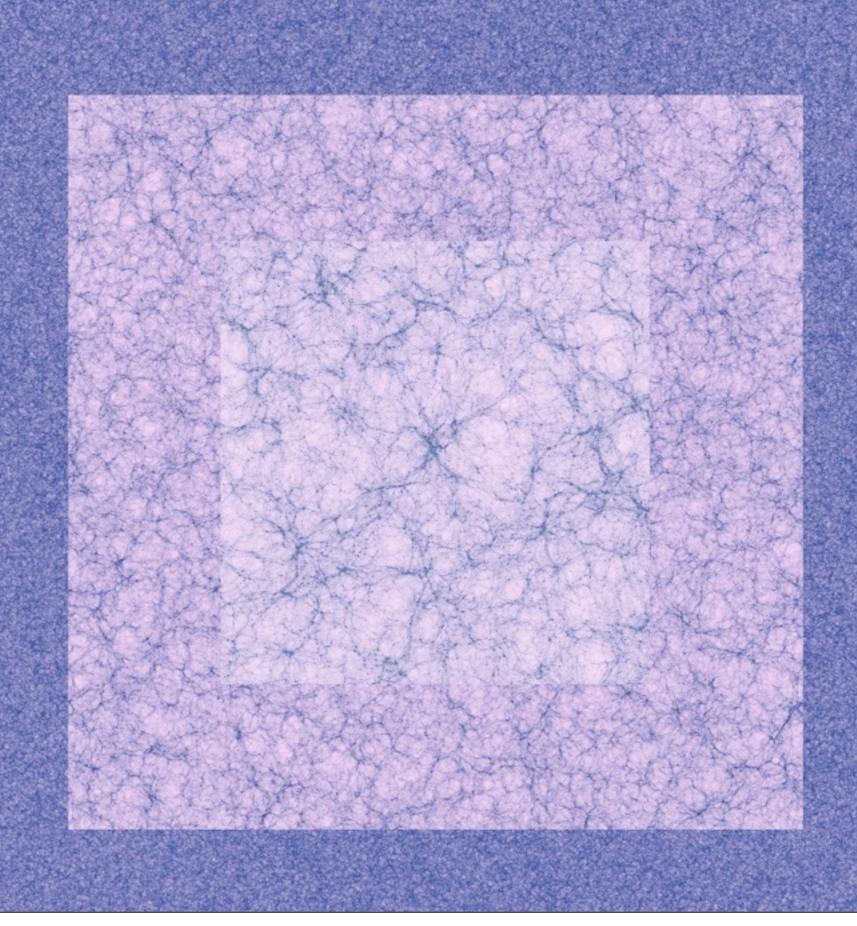
Orientation of the spins w.r.t the filaments

Horizon 4Pi:

DM only
2 Gpc/h periodic box
4096³ DM part.
43 million dark halos at
z=0

(Teyssier et al, 2009)

10 000 000 hrs CPU



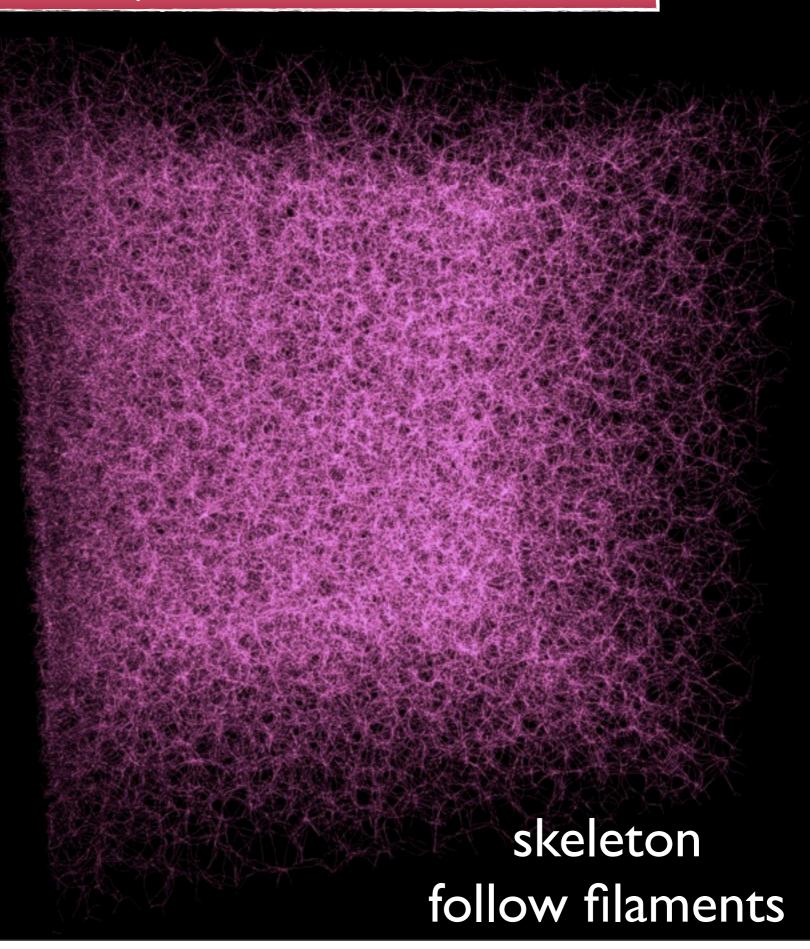
Orientation of the spins w.r.t the filaments

Horizon 4Pi:

DM only
2 Gpc/h periodic box
4096³ DM part.
43 million dark halos at
z=0

(Teyssier et al, 2009)

10 000 000 hrs CPU



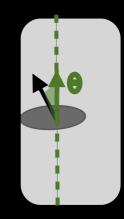
Excess probability of alignment between the spins and their host filament

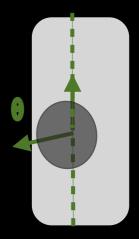
mass transition:

$$M_{\rm crit} = 4 \cdot 10^{12} M_{\odot}$$

 $M < M_{
m crit}$: aligned

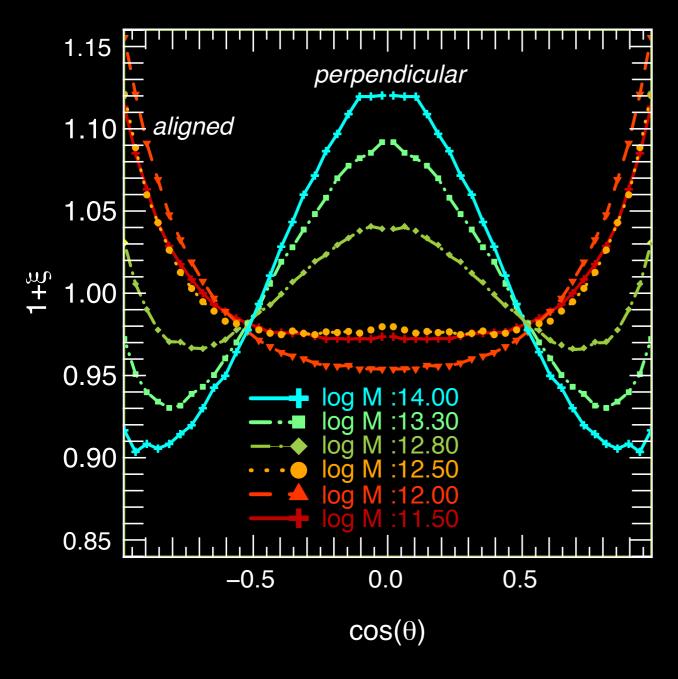
 $M>M_{\mathrm{crit}}$: perpendicular





(Codis et al, 2012)

Excess probability of alignment between the spins and their host filament

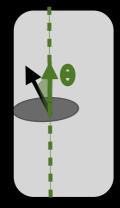


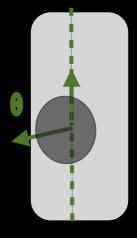
mass transition:

$$M_{\rm crit} = 4 \cdot 10^{12} M_{\odot}$$

 $M < M_{\rm crit}$: aligned

 $M>M_{
m crit}$: perpendicular

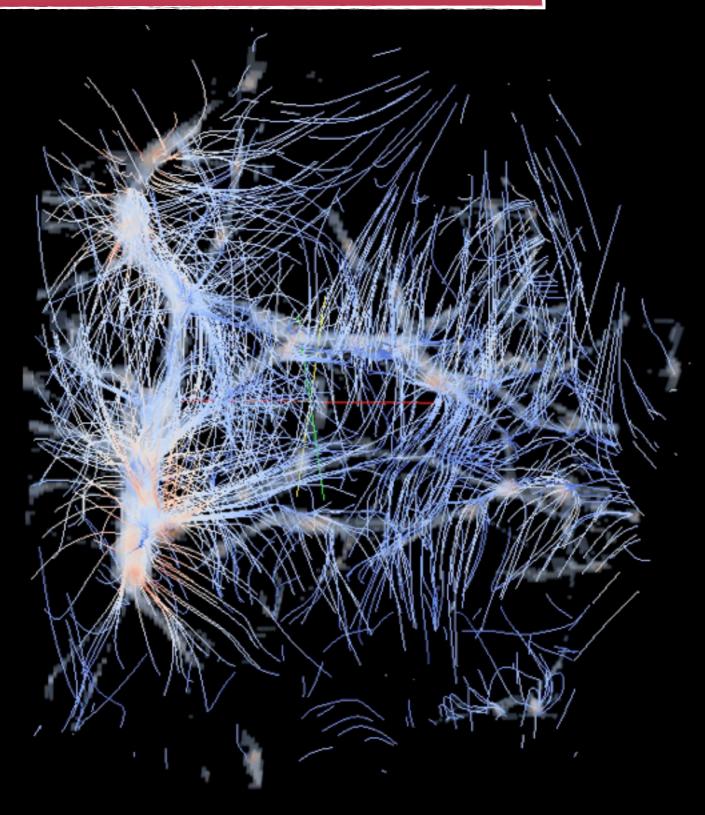




(Codis et al, 2012)

How does the formation of the filaments generate spin parallel to them?

Voids/wall saddle repel...

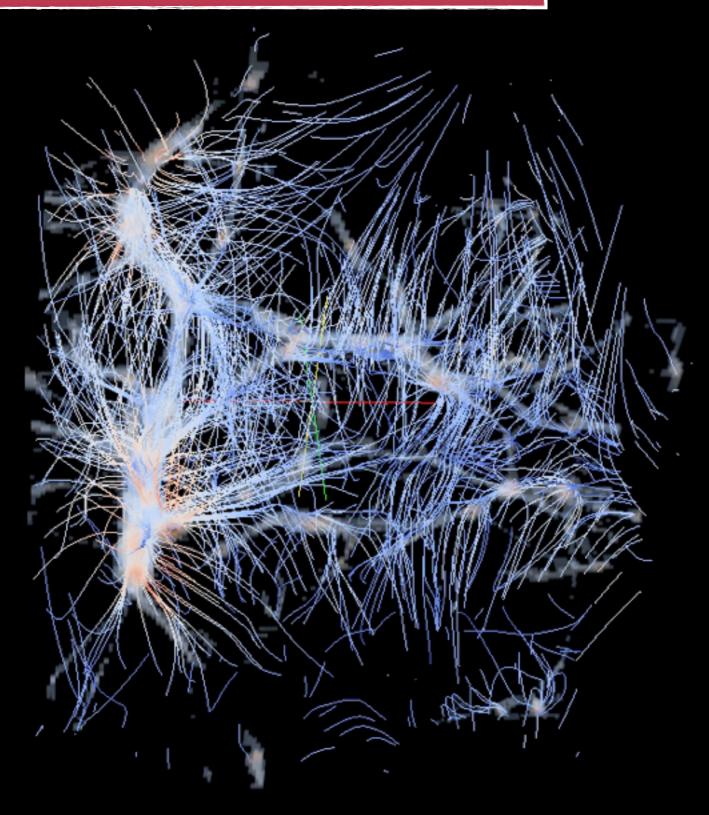


Vorticity generation in filaments

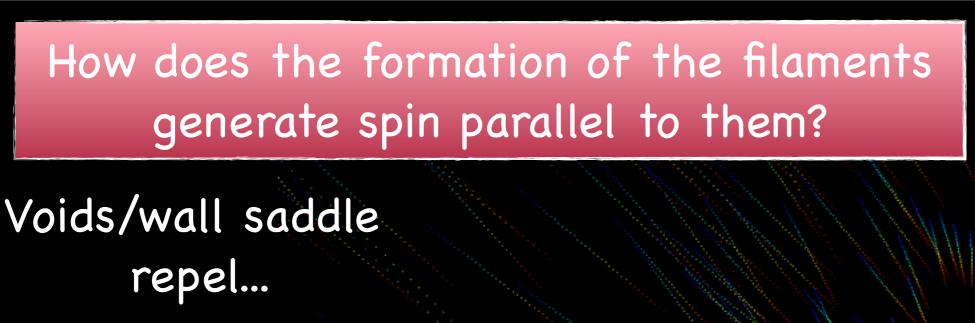
How does the formation of the filaments generate spin parallel to them?

Voids/wall saddle repel...

winding of walls into filaments



Vorticity generation in filaments

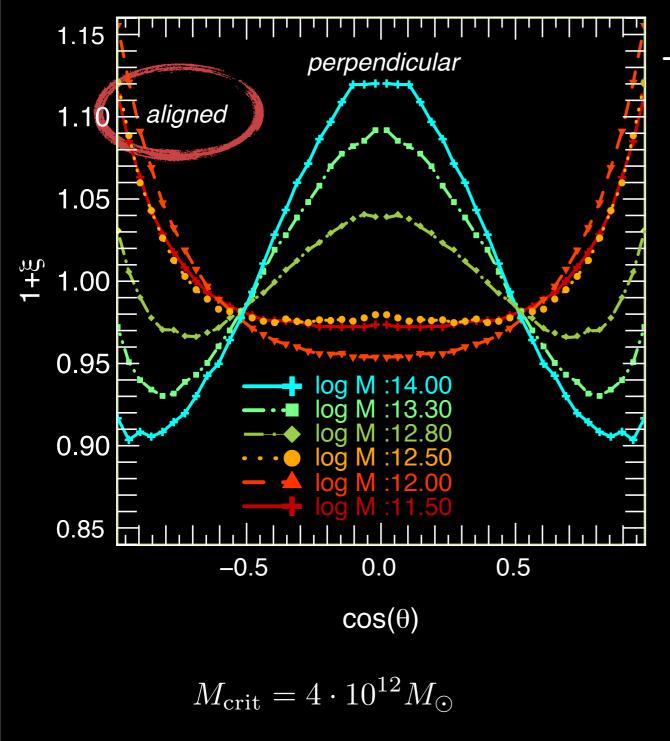


winding of walls into filaments

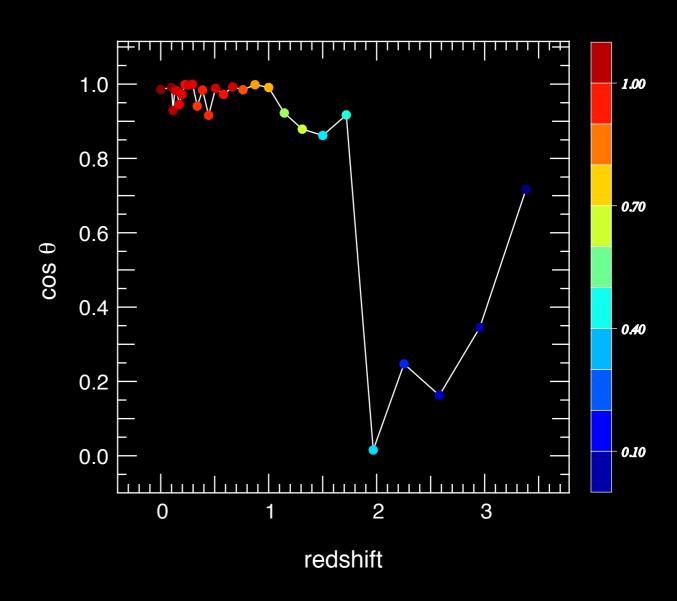
Vorticity generation in filaments

Low-mass haloes: $M < M_{\rm crit}$

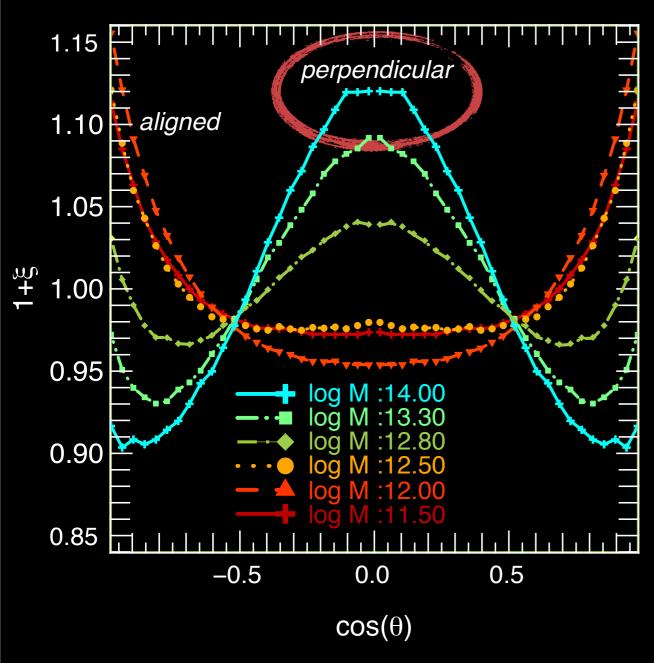




- -formed at high z during the formation within filaments
- -no major merger but smooth accretion until **z=0**

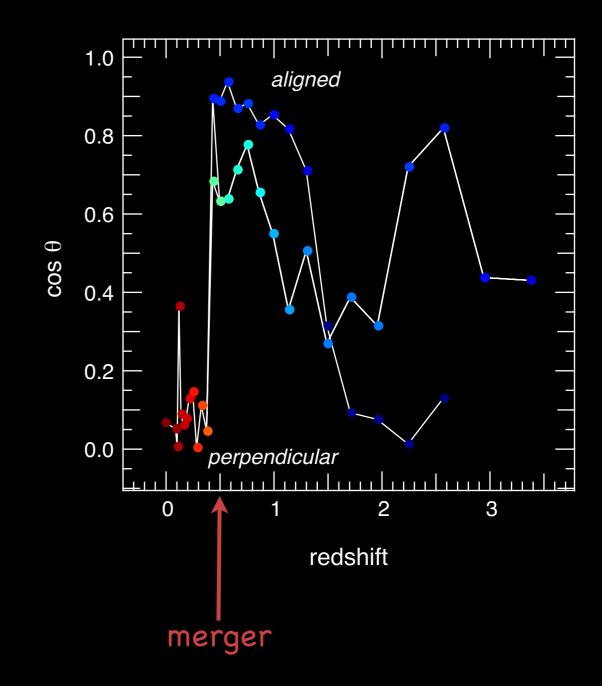


High-mass haloes: $M > M_{\rm crit}$



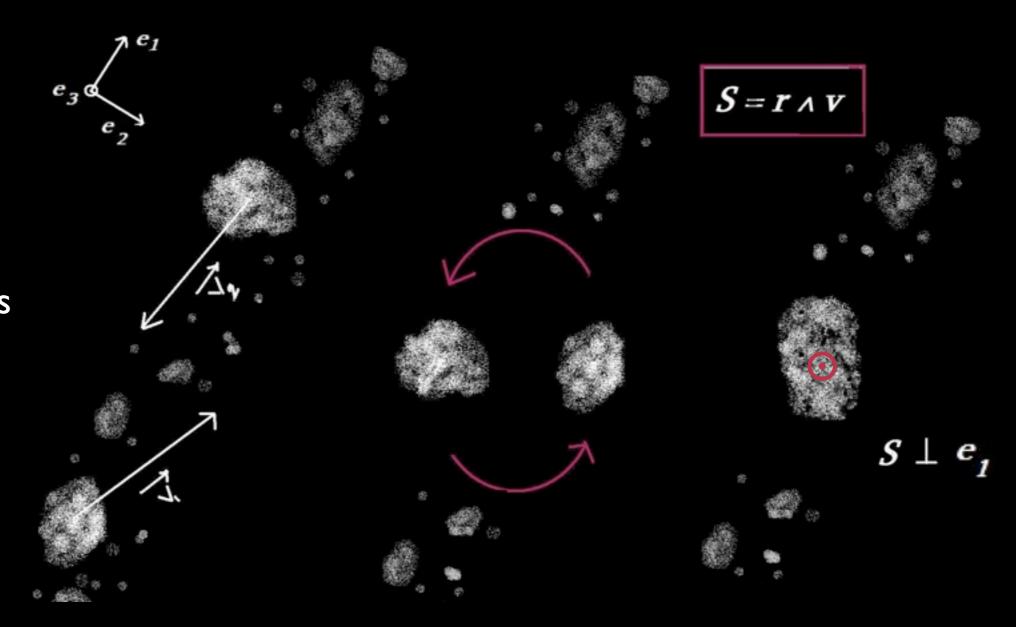
$$M_{\rm crit} = 4 \cdot 10^{12} M_{\odot}$$

formed at low z by mergers inside the filaments

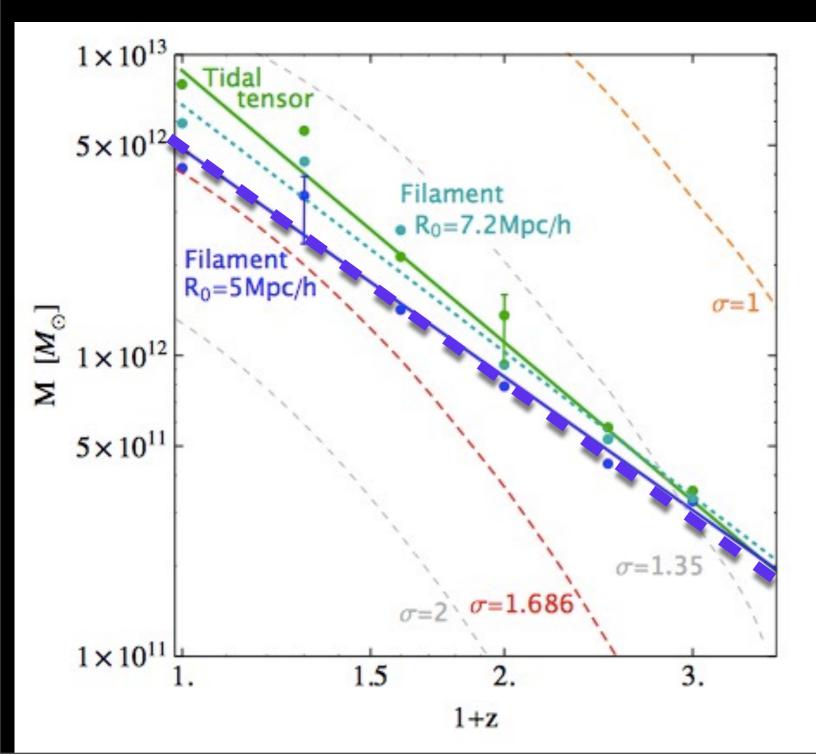


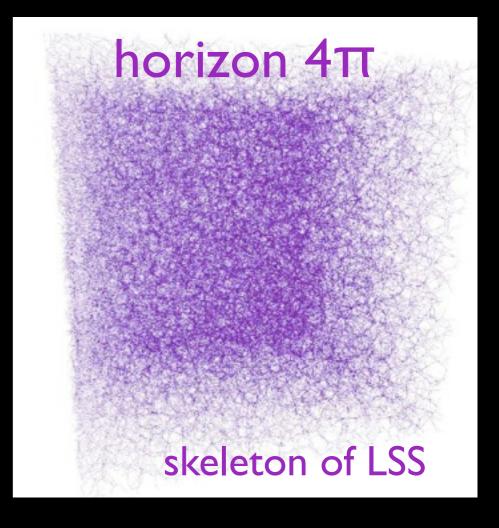
How do mergers along the filaments create spin perpendicular to them?

Halos catch up with each other along the filaments



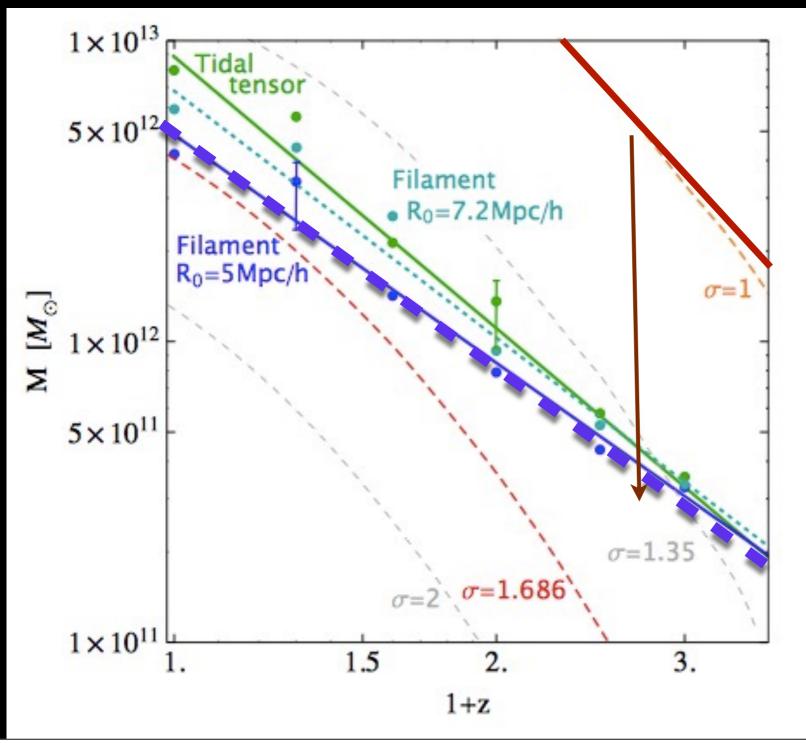
Explain transition mass?

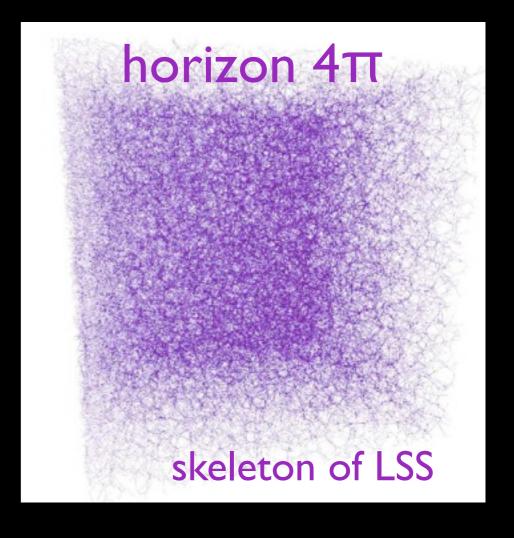




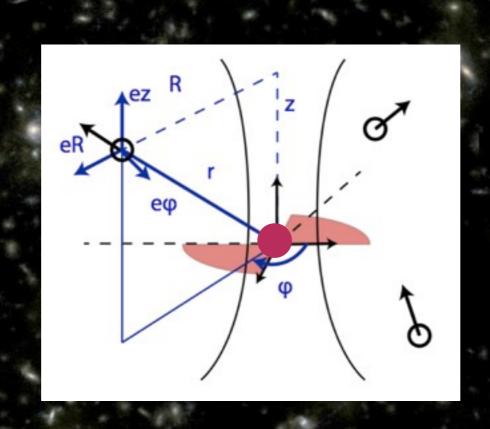
Explain transition mass?

Transition mass versus redshift: what's wrong???





Part II Tidal torque theory with a peak background split near a saddle



Seoul Feb 2nd 2016

The Idea

walls/filament/peak locally bias differentially tidal and inertia tensor: spin alignment reflect this in TTT

The picture

Geometry of spin near saddle: point reflection symmetric distribution, ~ 1/8 of 'naive size'

The Maths

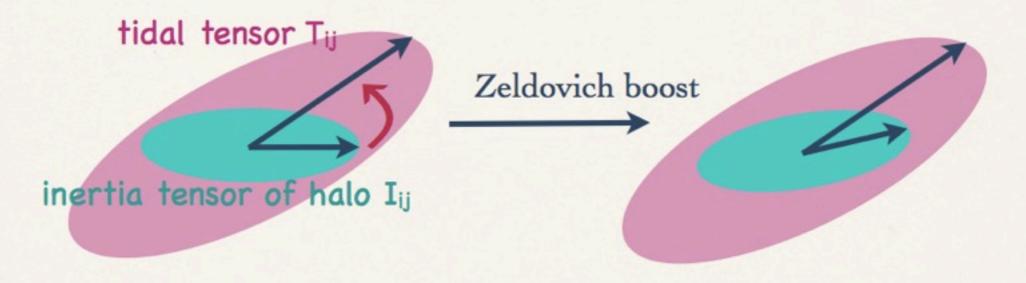
Very simple ab initio prediction for mass transition

The Lagrangian view of spin/LSS connection

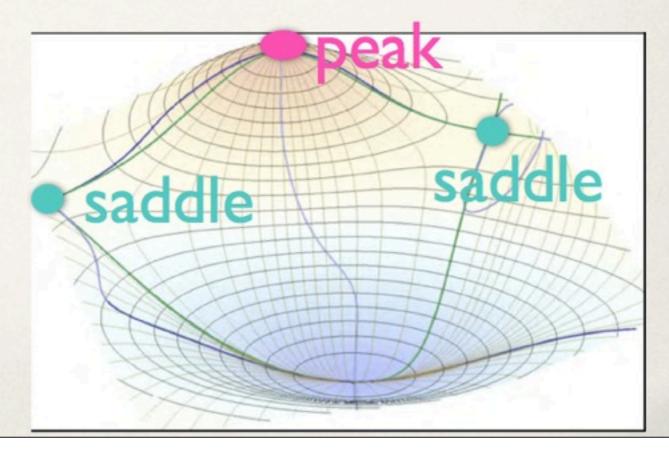
Can we understand where spin and vorticity alignments come from?

-usual tidal torque theory

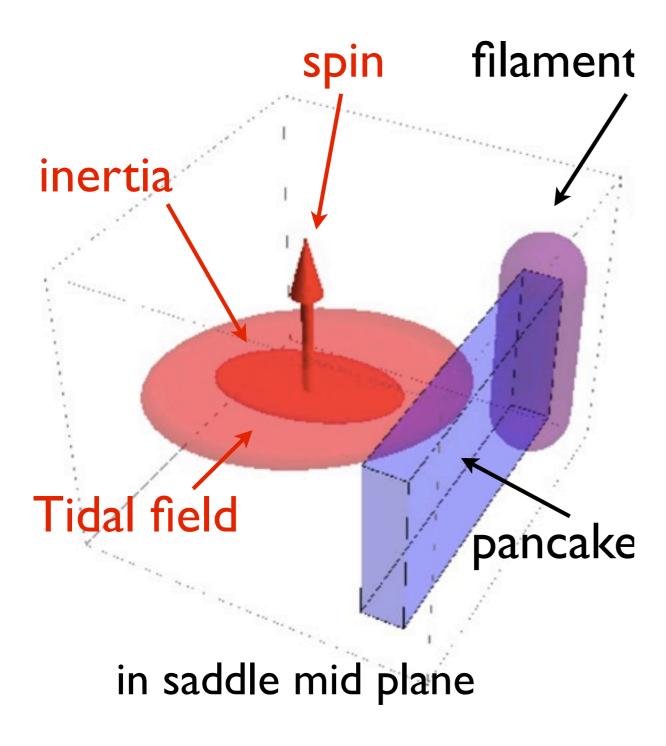
$$L_k = \varepsilon_{ijk} I_{li} T_{lj}$$



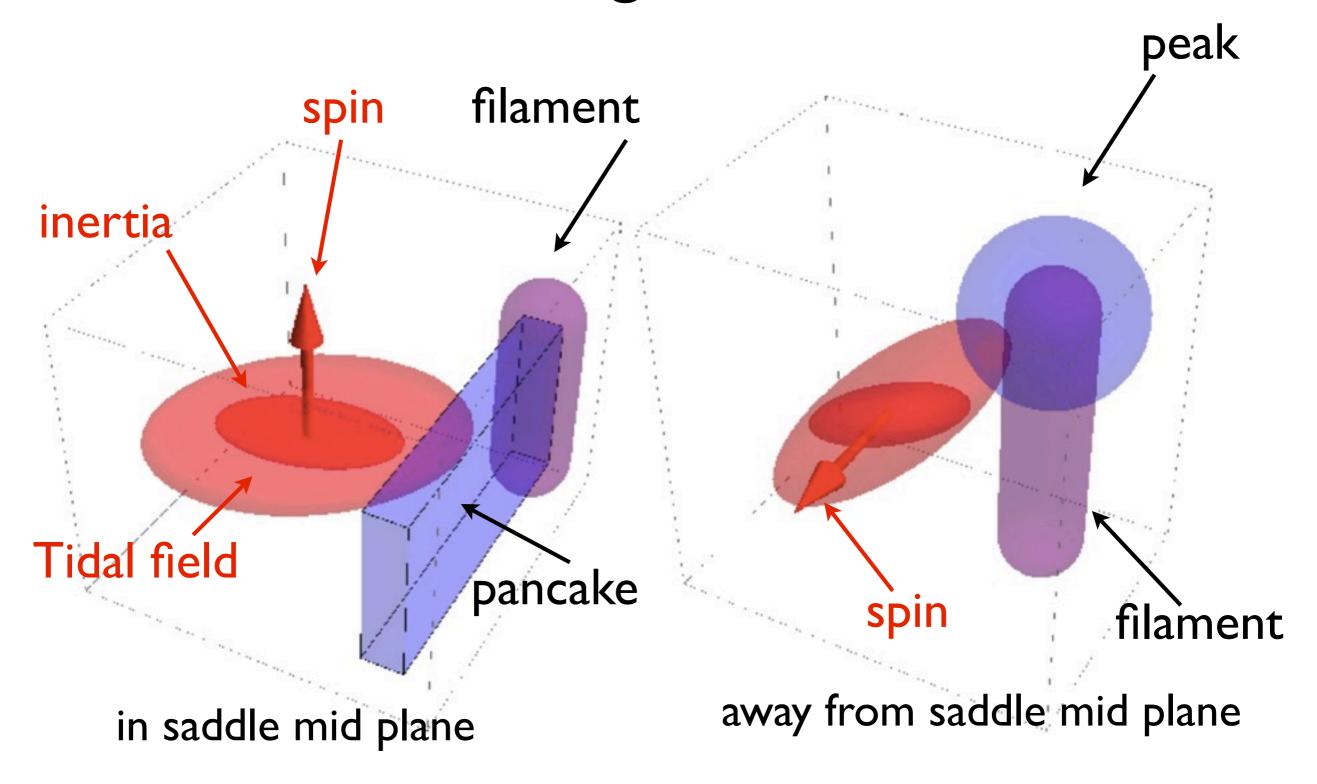
-anisotropy of the cosmic web: surrounding of a saddle point with typical geometry



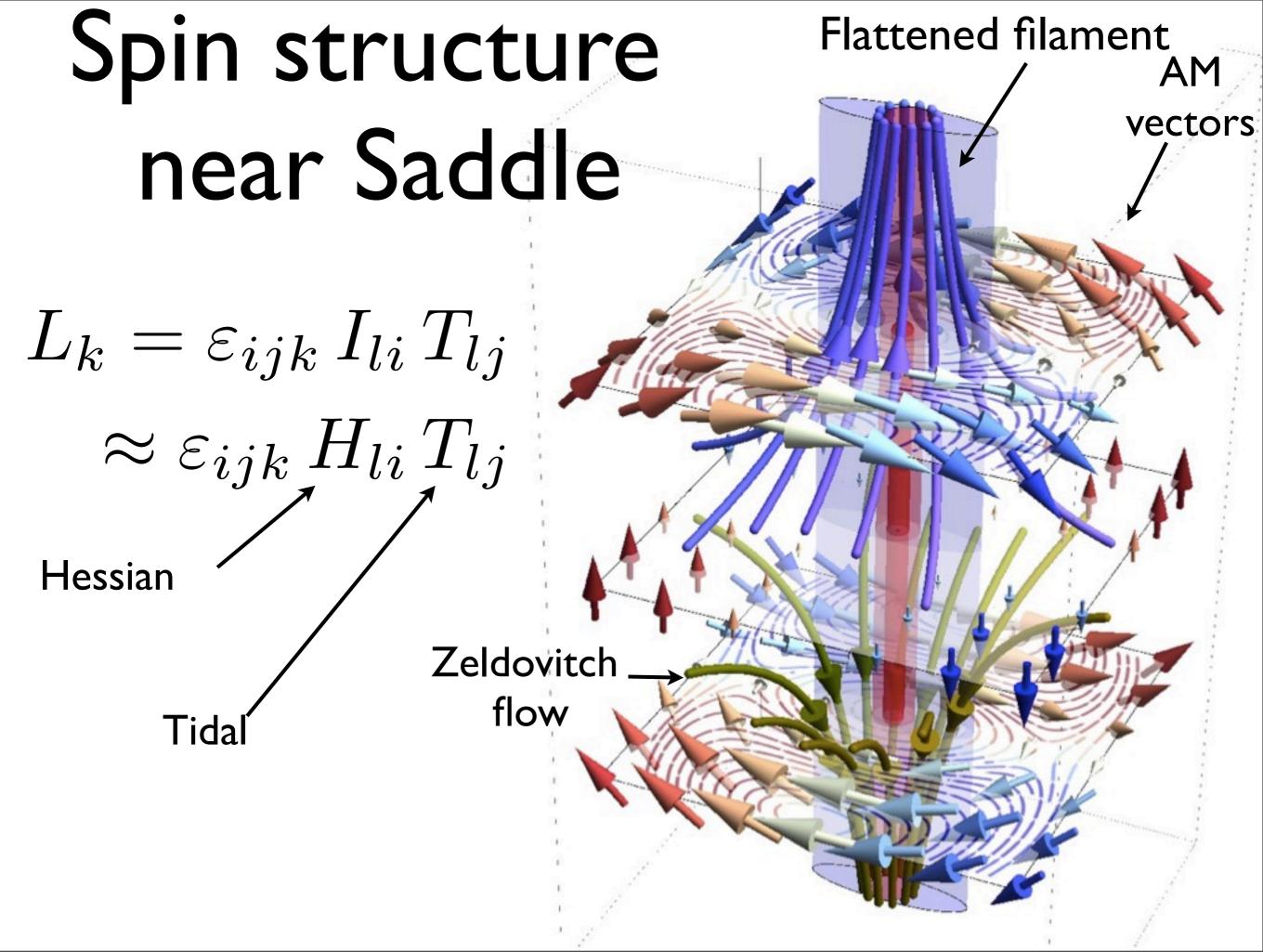
Tidal/Inertia mis-alignment

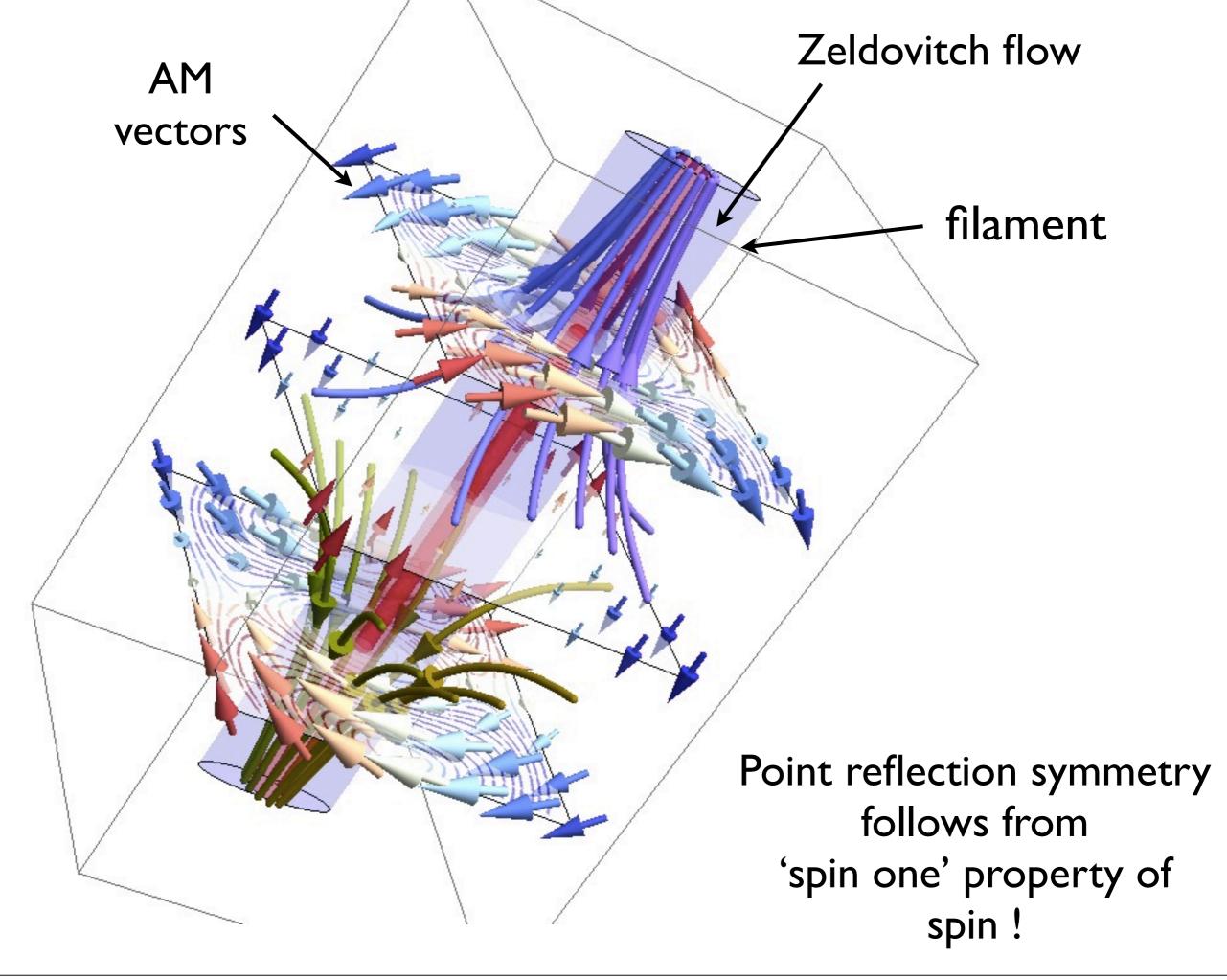


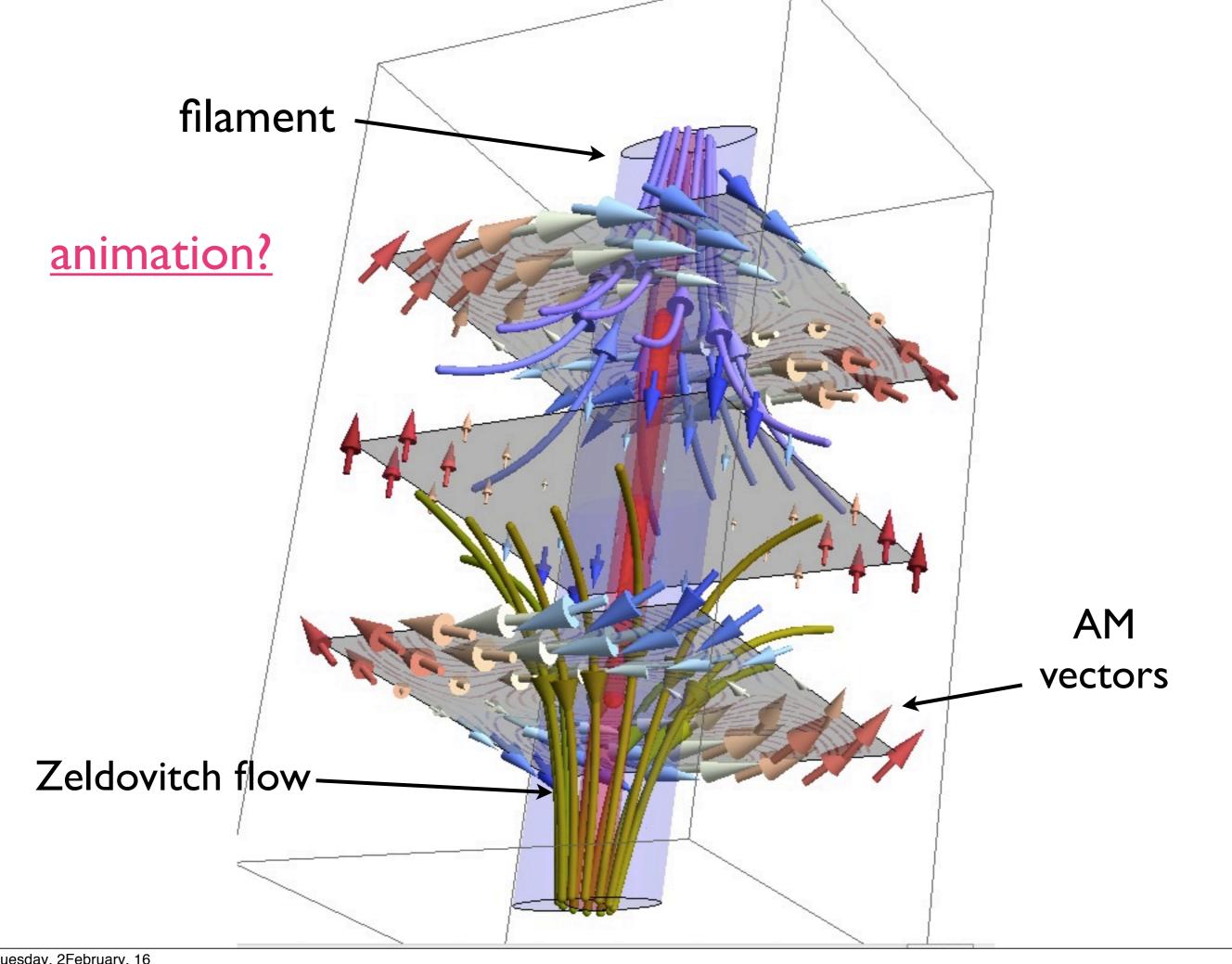
Tidal/Inertia mis-alignment

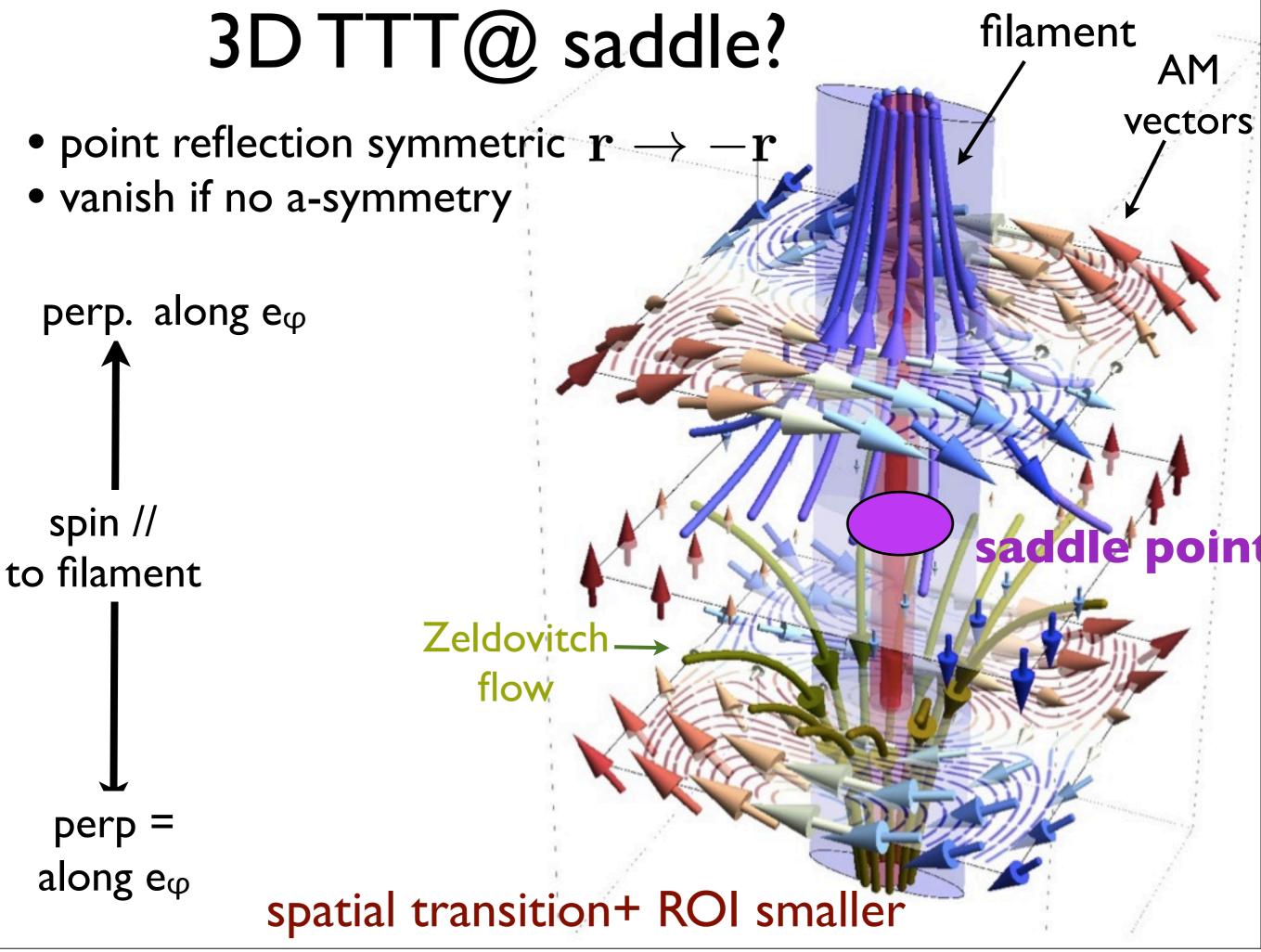


spin wall -filament spin filament-cluster animation?





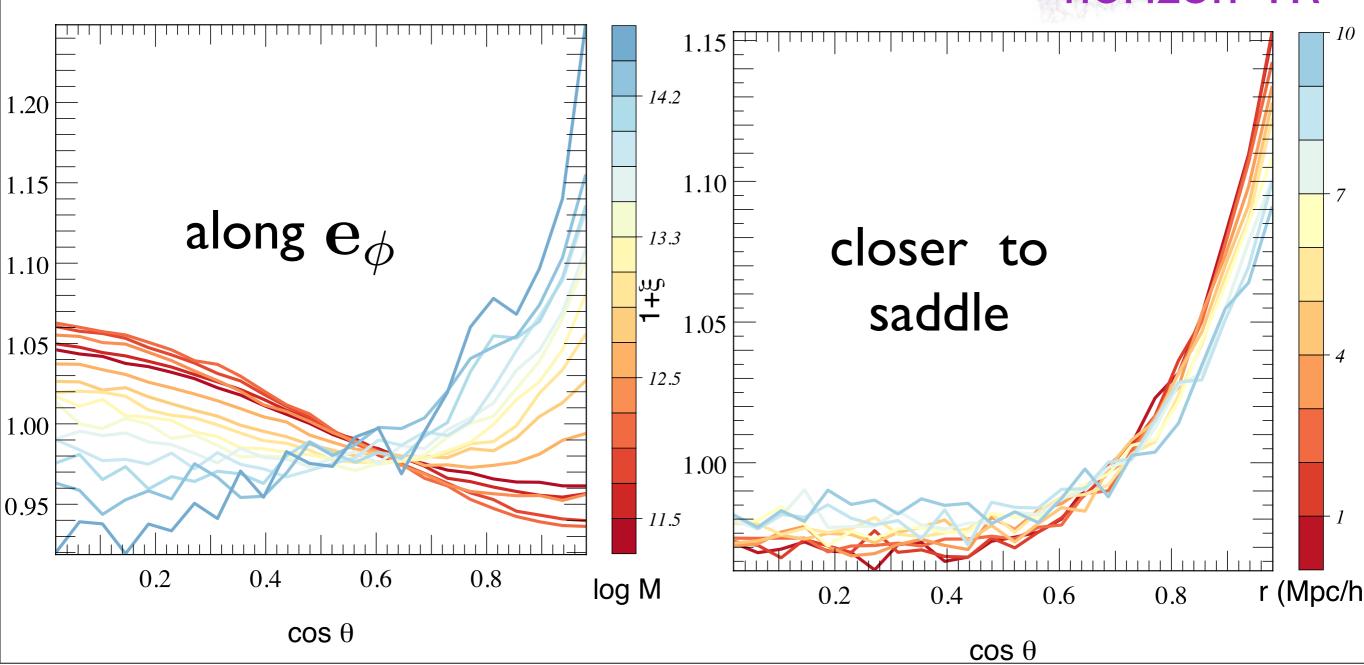




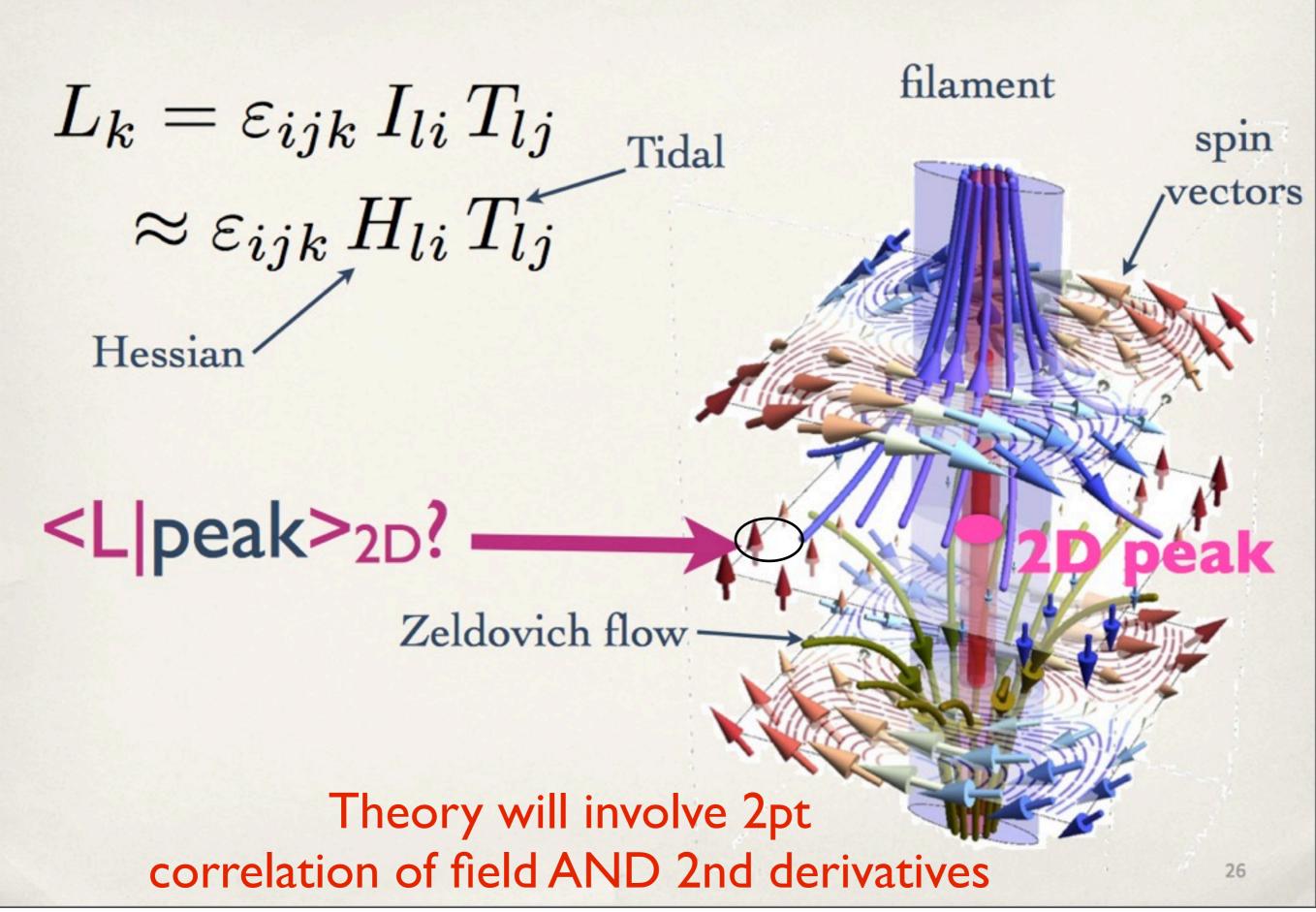
Does it work with Dark matter @ z=0?

Clear predictions of aTTT





2D Spin acquisition near peaks



TTT@ saddle?

the Gaussain joint PDF of the derivatives of the field, $\mathbf{X} = \{x_{ij}, x_{ijk}, x_{ijkl}\}$ and $\mathbf{Y} = \{y_{ij}, y_{ijk}, y_{ijkl}\}$ in two given locations (\mathbf{r}_x and \mathbf{r}_y separated by a distance $r = |\mathbf{r}_x - \mathbf{r}_y|$) obeys

$$PDF(\mathbf{X}, \mathbf{Y}) = \frac{1}{\det|2\pi\mathbf{C}|^{1/2}} \times$$

$$\exp\left(-\frac{1}{2}\begin{bmatrix} \mathbf{X} \\ \mathbf{Y} \end{bmatrix}^{\mathrm{T}} \cdot \begin{bmatrix} \mathbf{C}_{0} & \mathbf{C}_{\gamma} \\ \mathbf{C}_{\gamma}^{\mathrm{T}} & \mathbf{C}_{0} \end{bmatrix}^{-1} \cdot \begin{bmatrix} \mathbf{X} \\ \mathbf{Y} \end{bmatrix}\right), \quad (A2)$$

subject to the "saddle" constraints (2D)

"height"
$$x_{0,2}+x_{2,0}=
u,\; x_{1,2}+x_{3,0}=0,\; x_{0,3}+x_{2,1}=0,\;$$
 zero gradient $\kappa\cos(2 heta)=rac{1}{2}\left(x_{4,0}-x_{0,4}
ight),\; \kappa\sin(2 heta)=-x_{1,3}-x_{3,1}\,.$ parametrized curvature

Define the spin at point \mathbf{r}_y along the z direction as the anti-symmetric contraction of the de-traced tidal field and hessian:

 $L(\mathbf{r}_y) = \varepsilon_{ij} \overline{y}_{il} \overline{y}_{jmml} = (y_{2,0} - y_{0,2}) (y_{1,3} + y_{3,1}) +$ $\frac{y_{1,1}}{2}\left(y_{0,4}-y_{4,0}\right)-\frac{y_{1,1}}{2}\left(y_{4,0}-y_{0,4}\right).$

It is then fairly straightforward to compute the corresponding constrained expectation, $\langle L|pk\rangle$, for L as

$$L_z(r, \theta, \kappa, \nu) = \int L(\mathbf{Y}) PDF(\mathbf{X}, \mathbf{Y}|pk) d\mathbf{X}d\mathbf{Y}$$
. (A4)

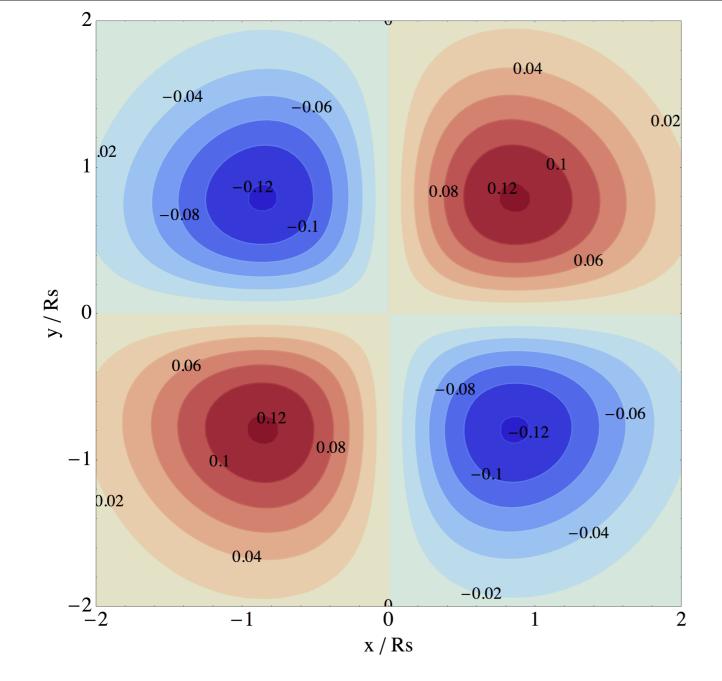


e.g. for n=-2 Incredibly simple prediction!

peak height

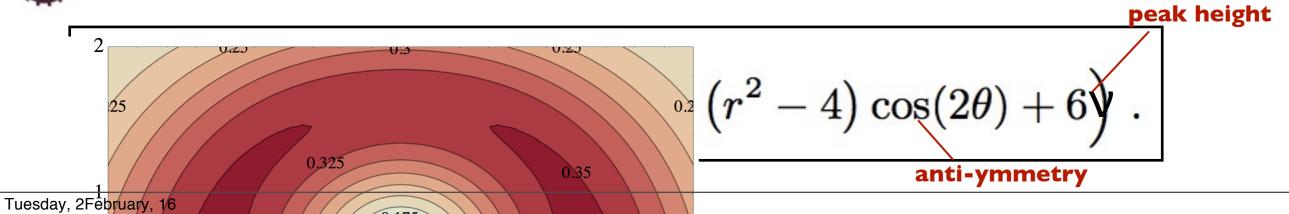
 $L_z = \kappa \frac{r^4 \sin(2\theta)}{144} e^{-\frac{r^2}{2}} \left(\sqrt{6}\kappa \left(r^2 - 4 \right) \cos(2\theta) + 6 \right).$

Tuesday, 2February, 16



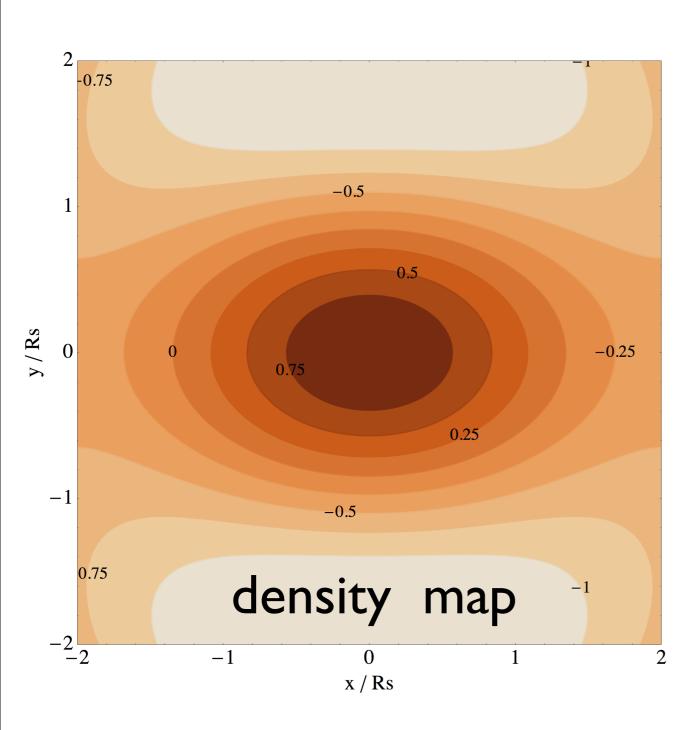


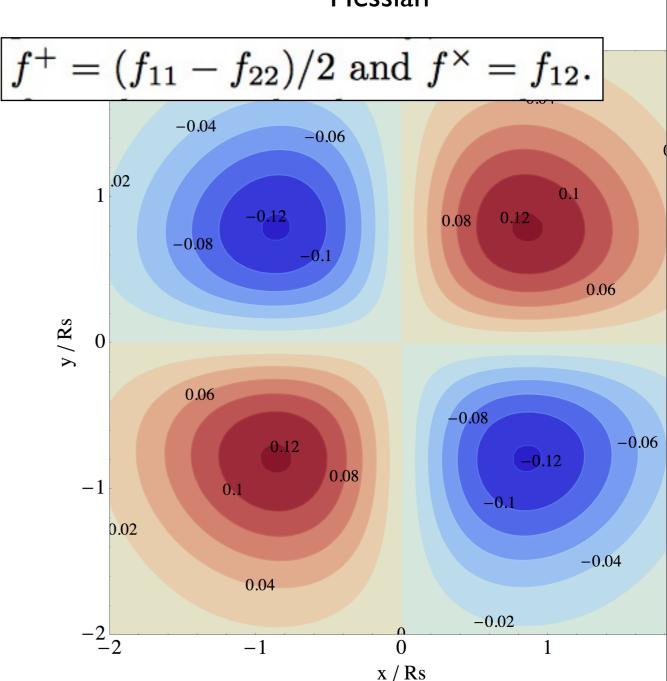
e.g. for n=-2 Incredibly simple prediction!



2D Theory of Tidal Torque @ saddle?

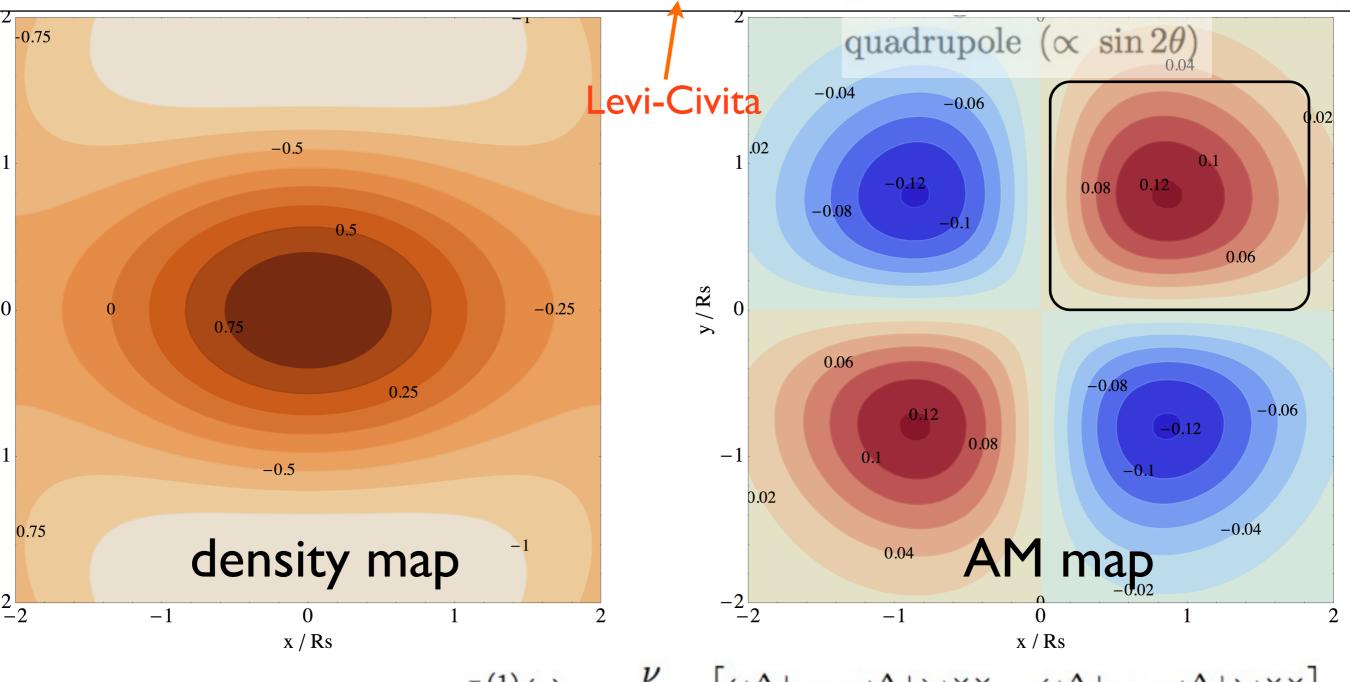
$$\delta(\mathbf{r}, \kappa, I_1, \nu | \text{ext}) = \frac{I_1(\xi_{\phi\delta}^{\Delta\Delta} + \gamma \xi_{\phi\phi}^{\Delta\Delta}) + \nu(\xi_{\phi\phi}^{\Delta\Delta} + \gamma \xi_{\phi\delta}^{\Delta\Delta})}{1 - \gamma^2} + 4 \left(\mathbf{\hat{r}}^{\text{T}} \cdot \overline{\mathbf{H}} \cdot \mathbf{\hat{r}} \right) \xi_{\phi\delta}^{\Delta+},$$
Hessian





2D Theory of Tidal Torque @ saddle?

$$\langle L_z | ext{ext}
angle = L_z(\mathbf{r}, \kappa, I_1,
u | ext{ext}) = -16(\mathbf{\hat{r}}^{\mathrm{T}}(\epsilon \cdot \mathbf{\overline{H}} \cdot \mathbf{\hat{r}}) \left(L_z^{(1)}(r) + 2(\mathbf{\hat{r}}^{\mathrm{T}} \cdot \mathbf{\overline{H}} \cdot \mathbf{\hat{r}}) L_z^{(2)}(r) \right)$$



$$L_z^{(1)}(r) = \frac{\nu}{1-\gamma^2} \left[(\xi_{\phi\phi}^{\Delta+} + \gamma \xi_{\phi\delta}^{\Delta+}) \xi_{\delta\delta}^{\times\times} - (\xi_{\phi\delta}^{\Delta+} + \gamma \xi_{\delta\delta}^{\Delta+}) \xi_{\phi\delta}^{\times\times} \right]$$

$$L_z^{(2)}(r) = (\xi_{\phi x}^{\Delta \Delta} \xi_{\delta \delta}^{\times \times} - \xi_{\phi \delta}^{\times \times} \xi_{\delta \delta}^{\Delta \Delta}) + \frac{I_1}{1 - \gamma^2} \left[(\xi_{\phi \delta}^{\Delta +} + \gamma \xi_{\phi \phi}^{\Delta +}) \xi_{\delta \delta}^{\times \times} - (\xi_{\delta \delta}^{\Delta +} + \gamma \xi_{\phi \delta}^{\Delta +}) \xi_{\phi \delta}^{\times \times} \right]$$

In order to compute the spin distribution, the formalism developed in Section 2 is easily extended to 3D. A critical (including saddle condition) point constraint is imposed. The resulting mean density field subject to that constraint becomes (in units of σ_2):

$$\delta(\mathbf{r}, \kappa, I_1, \nu | \text{ext}) = \frac{I_1(\xi_{\phi\delta}^{\Delta\Delta} + \gamma \xi_{\phi\phi}^{\Delta\Delta})}{1 - \gamma^2} + \frac{\nu(\xi_{\phi\phi}^{\Delta\Delta} + \gamma \xi_{\phi\delta}^{\Delta\Delta})}{1 - \gamma^2} + \frac{15}{2} \left(\mathbf{\hat{r}}^{\text{T}} \cdot \overline{\mathbf{H}} \cdot \mathbf{\hat{r}} \right) \xi_{\phi\delta}^{\Delta+}, \quad (3.1)$$

where again $\overline{\mathbf{H}}$ is the detraced Hessian of the density and $\hat{\mathbf{r}} = \mathbf{r}/r$ and we define in 3D $\xi_{\phi x}^{\Delta +}$ as $\xi_{\phi \delta}^{\Delta +} = \langle \Delta \delta, \phi^+ \rangle$, with $\phi^+ = \phi_{11} - (\phi_{22} + \phi_{33})/2$. Note that $\hat{\mathbf{r}}^{\mathrm{T}} \cdot \overline{\mathbf{H}} \cdot \hat{\mathbf{r}}$ is a scalar quantity defined explicitly as $\hat{r}_i \overline{H}_{ij} \hat{r}_j$. As in 2D, the expected spin can also be computed. In 3D, the spin is a vector, which components are given by $L_i = \varepsilon_{ijk} \delta_{kl} \phi_{lj}$, with ϵ the rank 3 Levi Civita tensor. It is found to be orthogonal to the separation and can be written as the sum of two terms

$$\mathbf{L}(\mathbf{r}, \kappa, I_1, \nu | \text{ext}) = -15 \left(\mathbf{L}^{(1)}(r) + \mathbf{L}^{(2)}(\mathbf{r}) \right) \cdot (\hat{\mathbf{r}}^{\text{T}} \cdot \boldsymbol{\epsilon} \cdot \overline{\mathbf{H}} \cdot \hat{\mathbf{r}}),$$
(3.2)

where $\mathbf{L}^{(1)}$ depends on height, ν , and on the trace of the Hessian I_1 but not on orientation

$$\mathbf{L}^{(1)}(r) = \left(\frac{\nu}{1 - \gamma^{2}} \left[(\xi_{\phi\phi}^{\Delta +} + \gamma \xi_{\phi\delta}^{\Delta +}) \xi_{\delta\delta}^{\times \times} - (\xi_{\phi\delta}^{\Delta +} + \gamma \xi_{\delta\delta}^{\Delta +}) \xi_{\phi\delta}^{\times \times} \right] + \frac{I_{1}}{1 - \gamma^{2}} \left[(\xi_{\phi\delta}^{\Delta +} + \gamma \xi_{\phi\phi}^{\Delta +}) \xi_{\delta\delta}^{\times \times} - (\xi_{\delta\delta}^{\Delta +} + \gamma \xi_{\phi\delta}^{\Delta +}) \xi_{\phi\delta}^{\times \times} \right] \right) \mathbb{I}_{3},$$

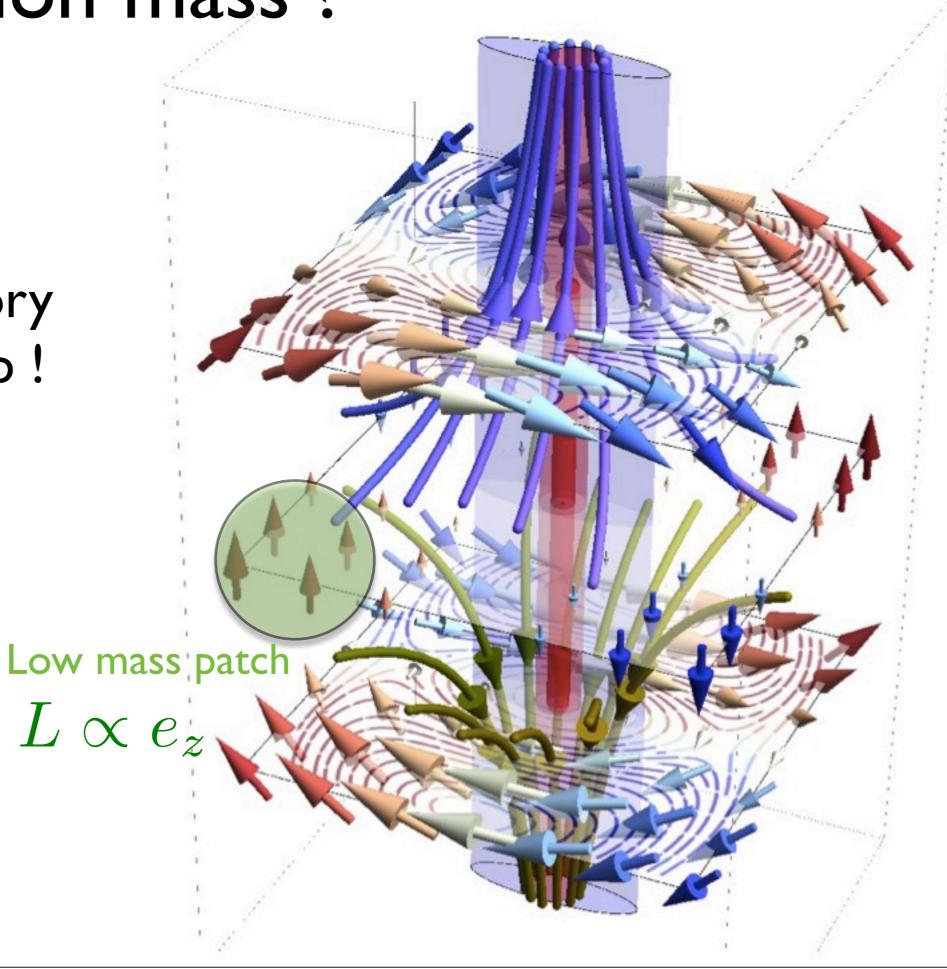
and $L^{(2)}(\mathbf{r})$ now depends on $\overline{\mathbf{H}}$ and on orientation:

$$\mathbf{L}^{(2)}(\mathbf{r}) = -\frac{5}{8} \left[2((\xi_{\phi\delta}^{\Delta +} - \xi_{\phi\delta}^{\Delta \Delta})\xi_{\delta\delta}^{\times \times} - (\xi_{\delta\delta}^{\Delta +} - \xi_{\delta\delta}^{\Delta \Delta})\xi_{\phi\delta}^{\times \times})\overline{\mathbf{H}} + ((7\xi_{\delta\delta}^{\Delta \Delta} + 5\xi_{\delta\delta}^{\Delta +})\xi_{\phi\delta}^{\times \times} - (7\xi_{\phi\delta}^{\Delta \Delta} + 5\xi_{\phi\delta}^{\Delta +})\xi_{\delta\delta}^{\times \times})(\hat{\mathbf{r}}^{\mathrm{T}} \cdot \overline{\mathbf{H}} \cdot \hat{\mathbf{r}})\mathbb{I}_{3} \right],$$

3D Transition mass?

Lagrangian theory capture spin flip!

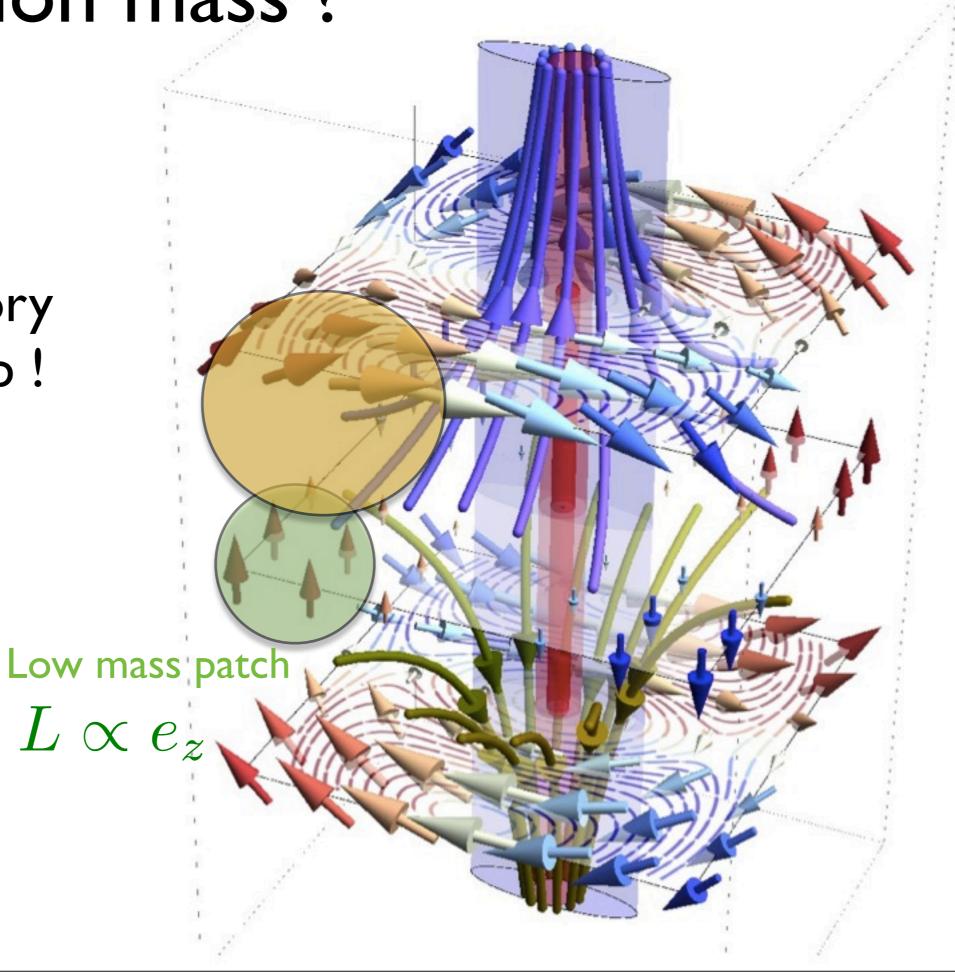
Transition mass associated with **size** of quadrant



3D Transition mass?

Lagrangian theory capture spin flip!

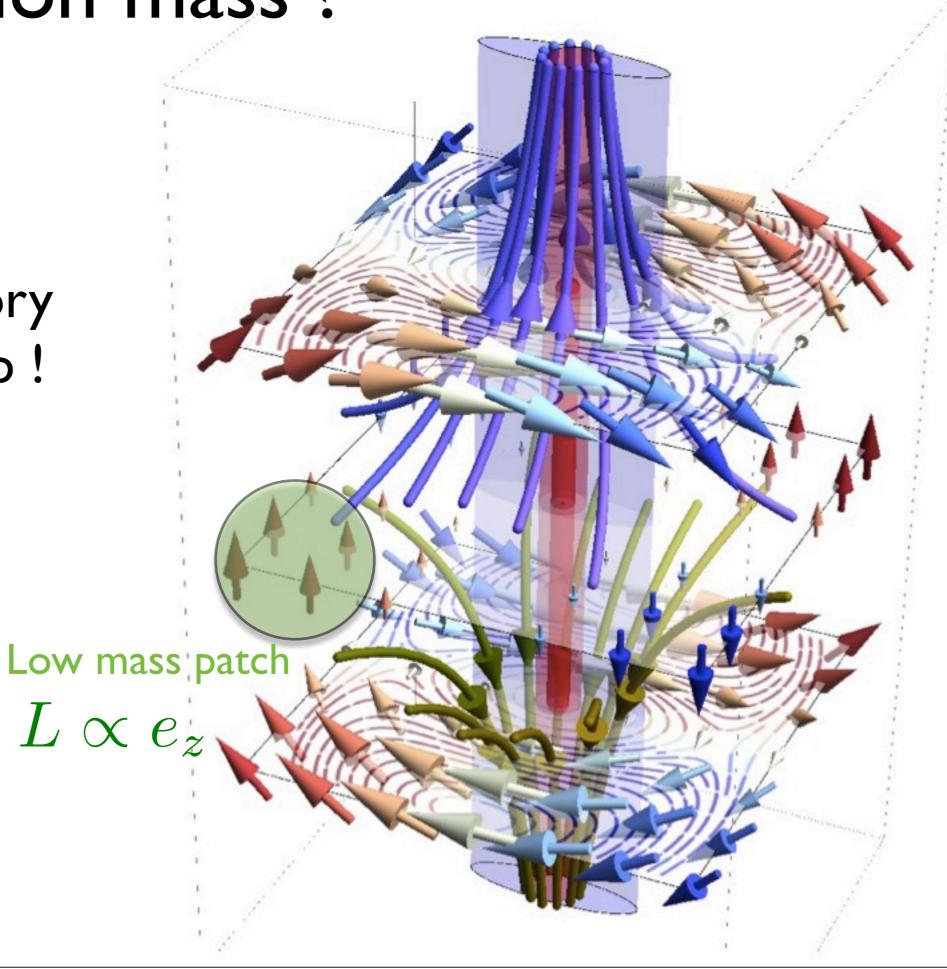
Transition mass associated with **size** of quadrant



3D Transition mass?

Lagrangian theory capture spin flip!

Transition mass associated with **size** of quadrant



3D Transition mass? High mass patch $L \propto e_{\phi}$ Lagrangian theory capture spin flip! Transition mass associated with **size** Low mass patch $L \propto e_z$ of quadrant

Geometry of the saddle provides a natural 'metric' (local frame as defined by Hessian @ saddle) relative to which dynamical evolution of DH is predicted.

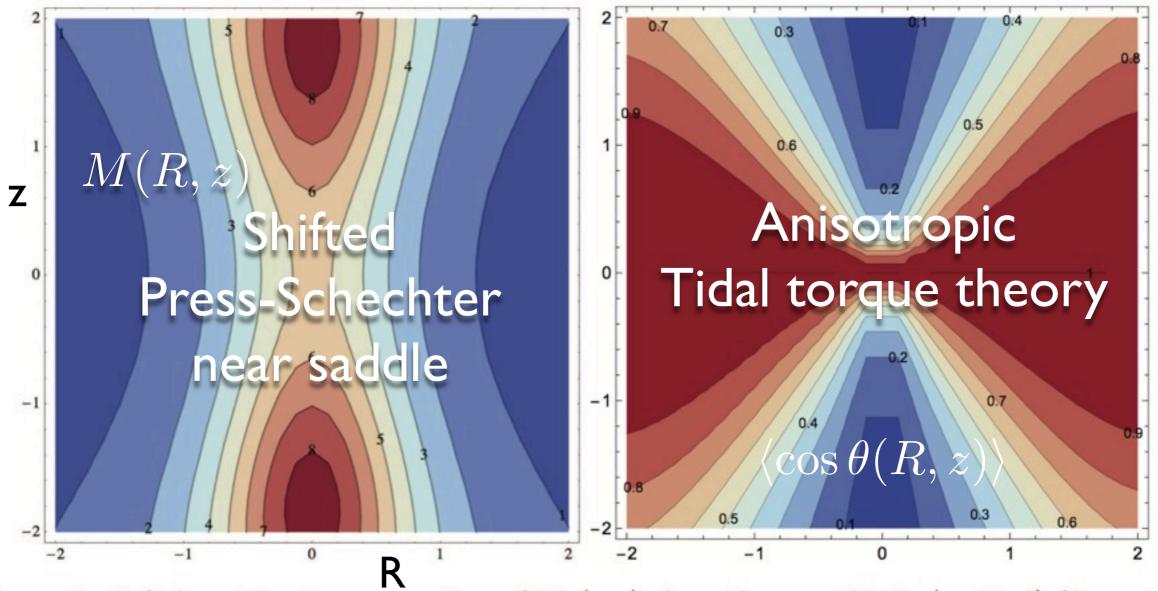


Figure 5. Left: logarithmic cross section of $M_p(r, z)$ along the most likely (vertical) filament (in units of $10^{12} M_{\odot}$). Right: corresponding cross section of $\langle \cos \hat{\theta} \rangle (r, z)$. The mass of halos increases towards the nodes, while the spin flips.

geometric split ——

mass split

cloud effect

Geometry of the saddle provides a natural 'metric' (local frame as defined by Hessian @ saddle) relative to which dynamical evolution of DH is predicted.

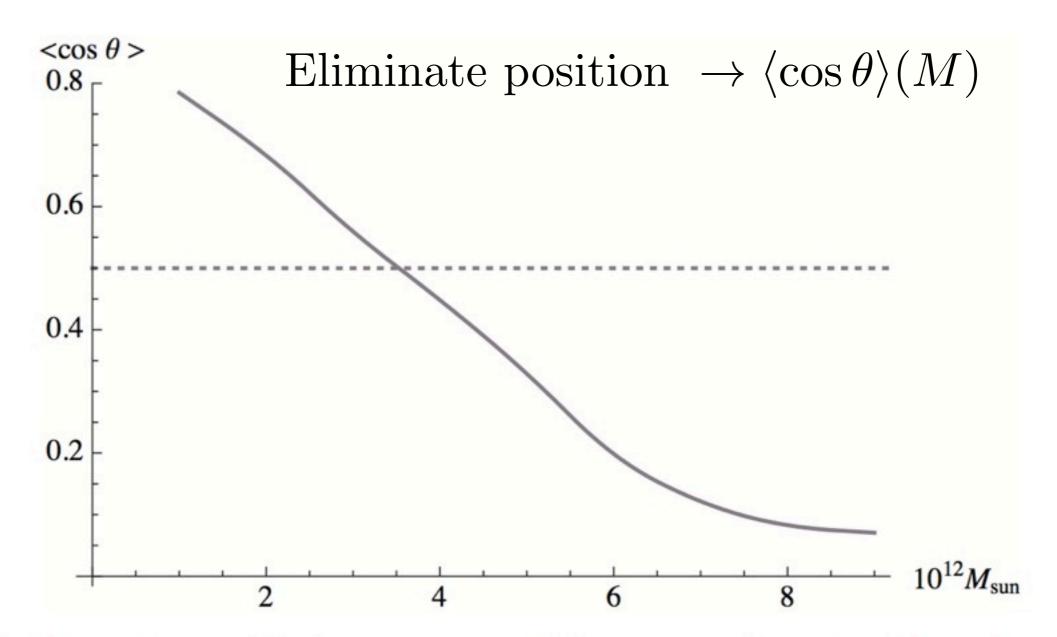


Figure 6. Mean alignment between spin and filament as a function of mass for a filament smoothing scale of 5 Mpc/h. The spin flip transition mass is around $4\,10^{12}M_{\odot}$.

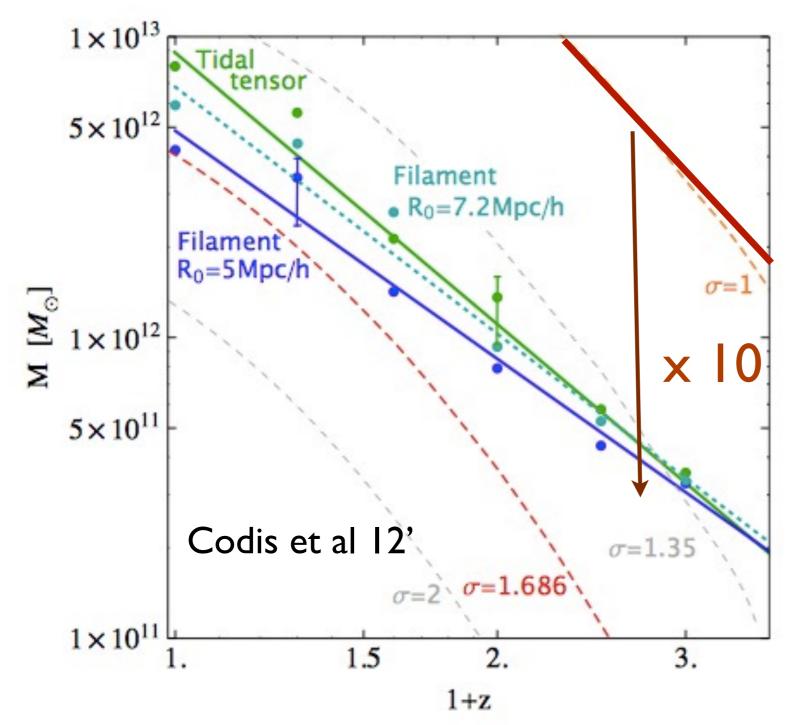
geometric split

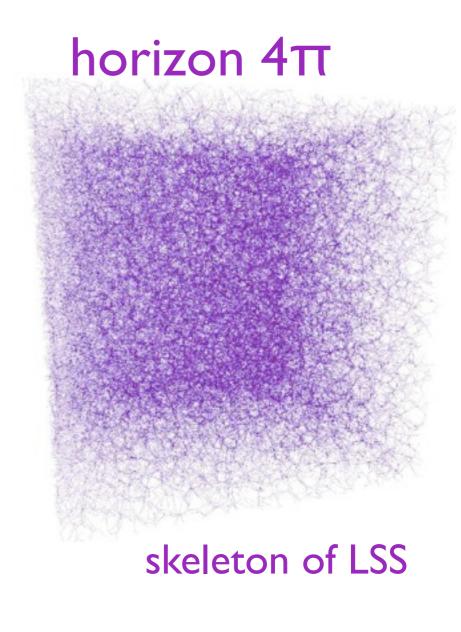
mass split

cloud effect

Explain transition mass? YES!

Transition mass versus redshift

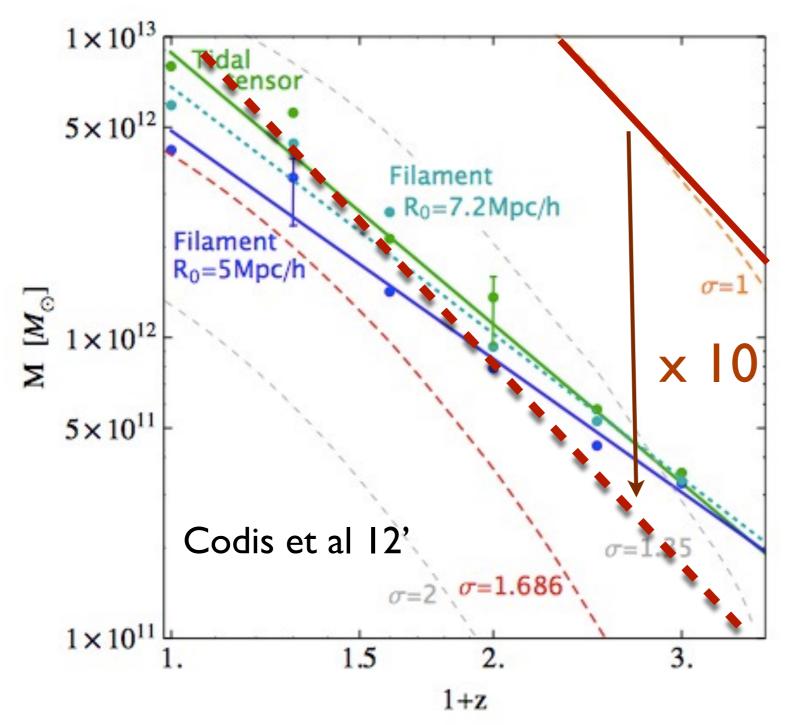


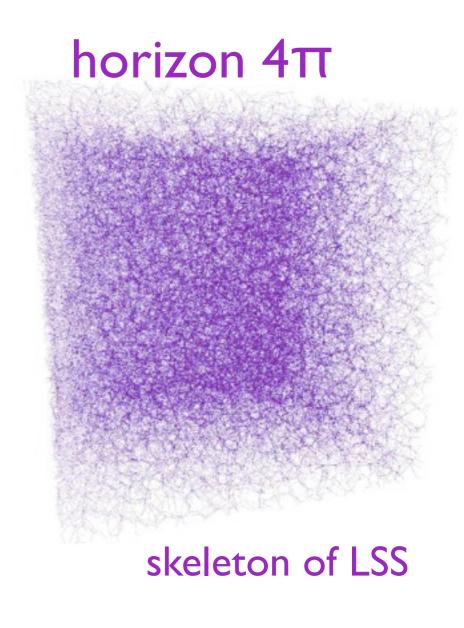


Only 2 ingredients: a) spin is spin one b) filaments flattened

Explain transition mass? YES!

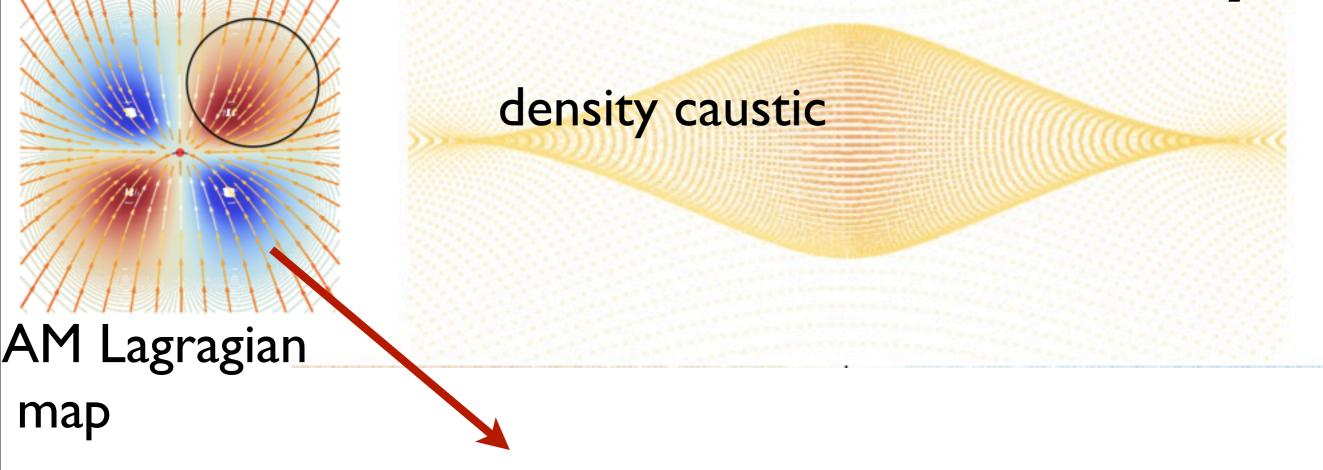
Transition mass versus redshift



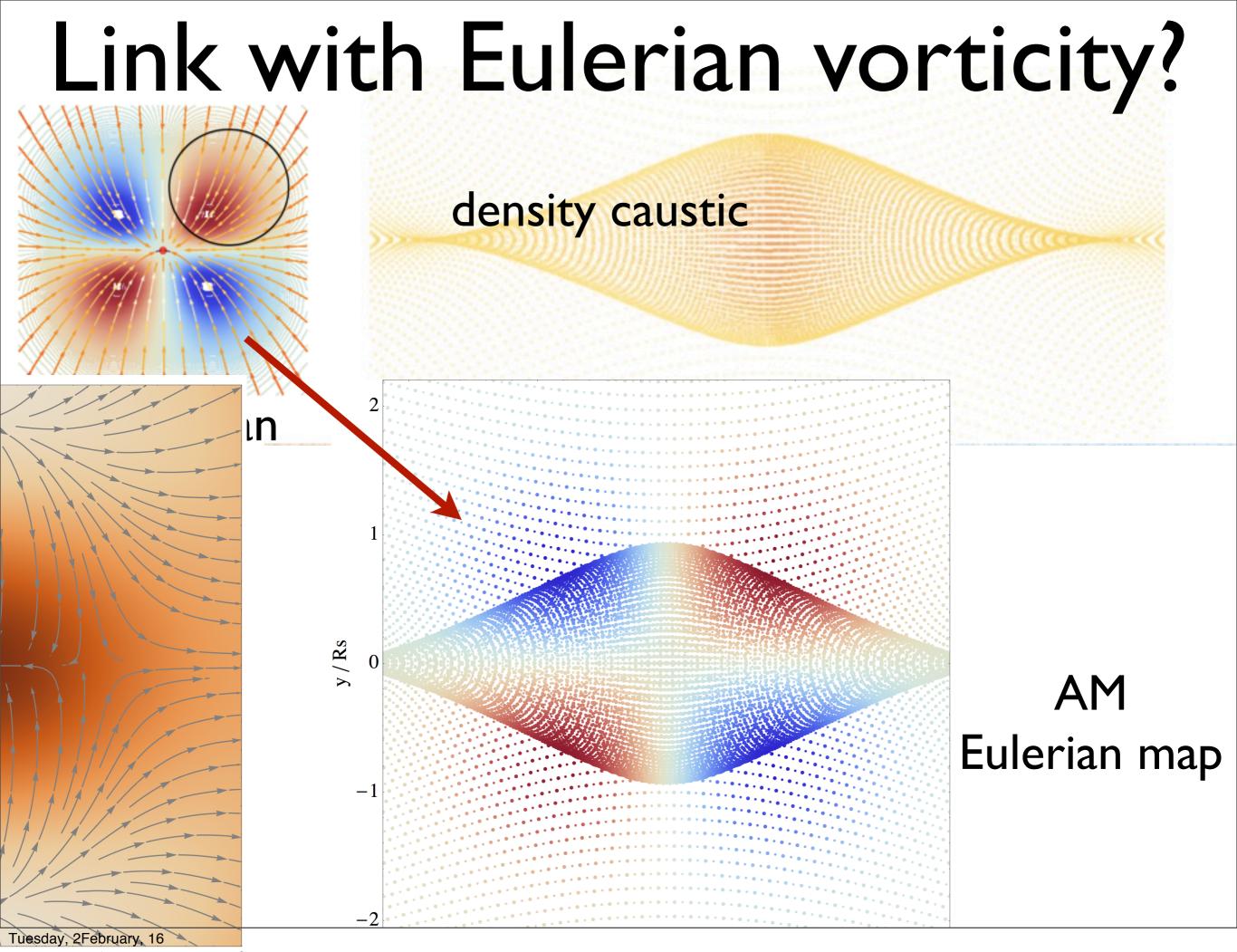


Only 2 ingredients: a) spin is spin one b) filaments flattened

Link with Eulerian vorticity?

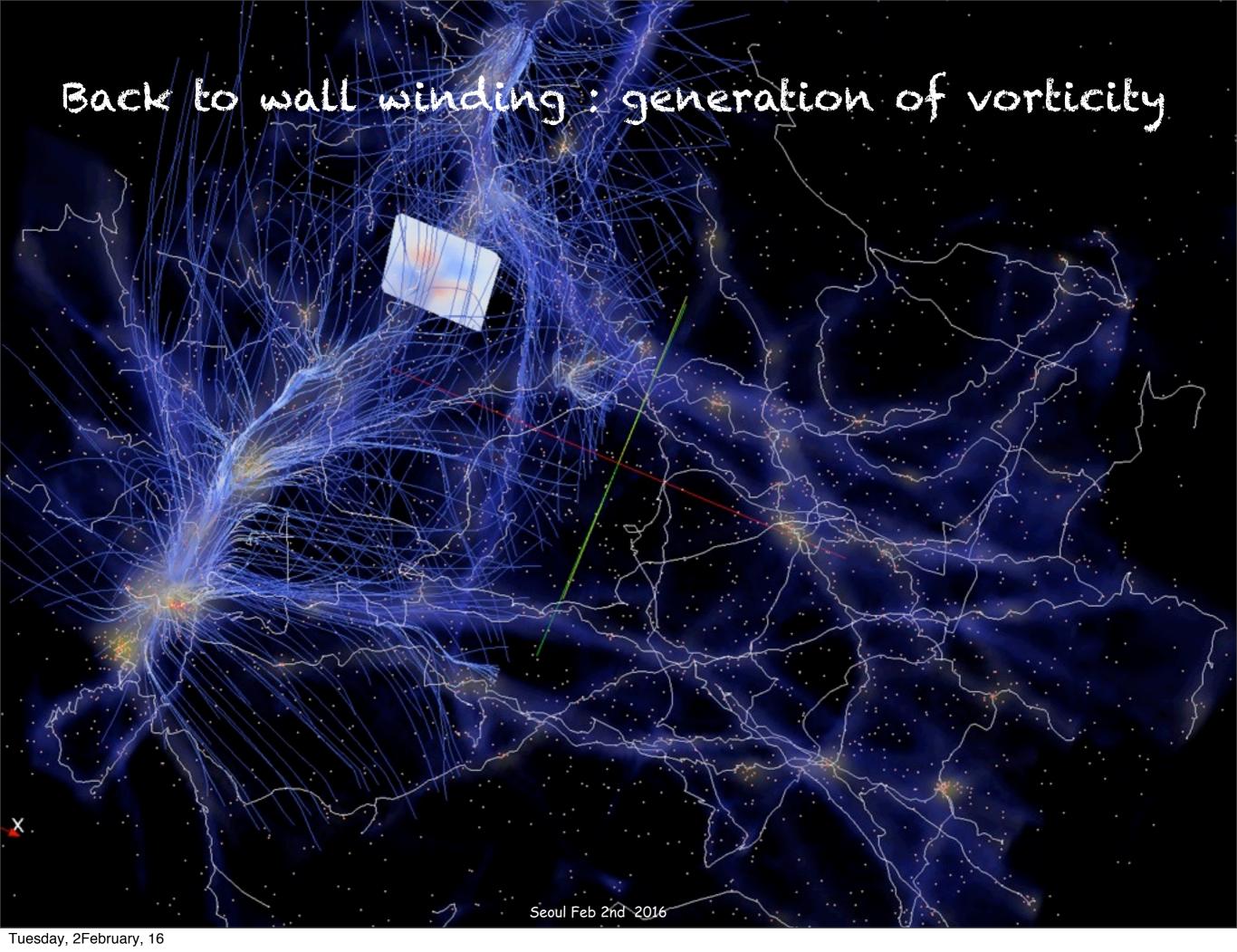


AM Eulerian map



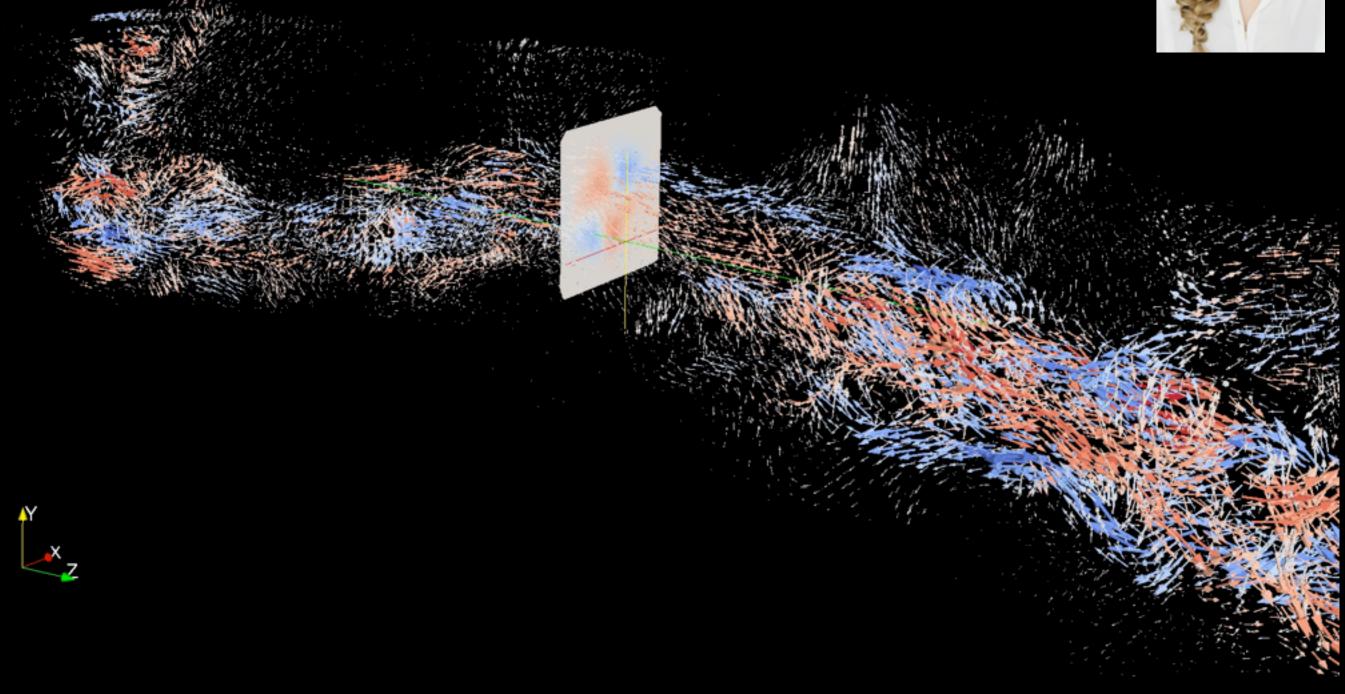
PART III

Link with Eulerian vorticity?



Alignement of vorticity with cosmic web





braids structure of vorticity.

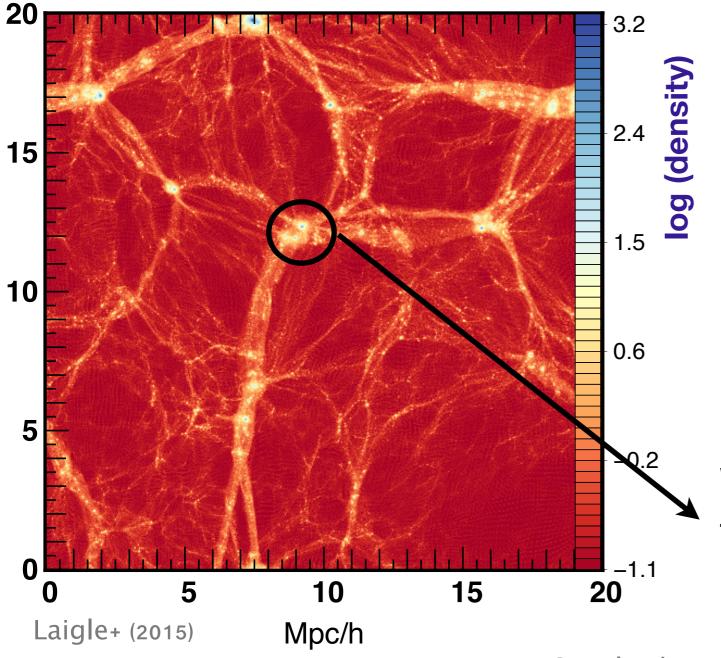
Seoul Feb 2nd 2016

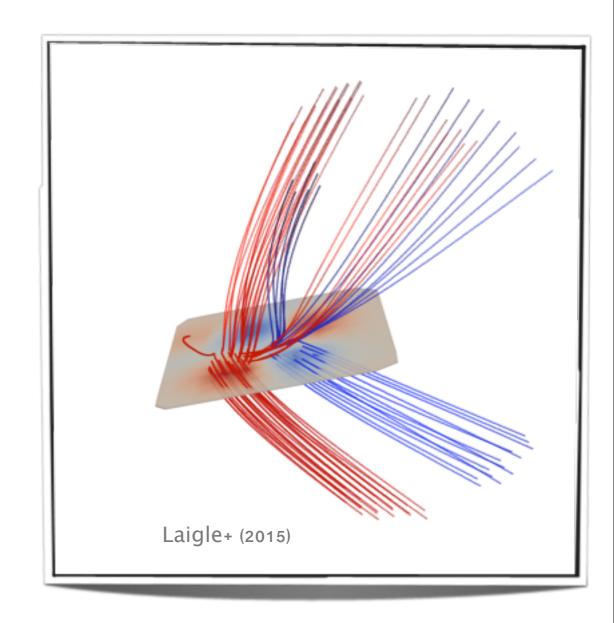
Growth of large-scale structure

In the initial phase of structure formation, flows are laminar and curl-free.

This is no longer valid at the shell-crossing.

Thin slice of a DM simulation at z=0.





What happens when cosmic flows cross?

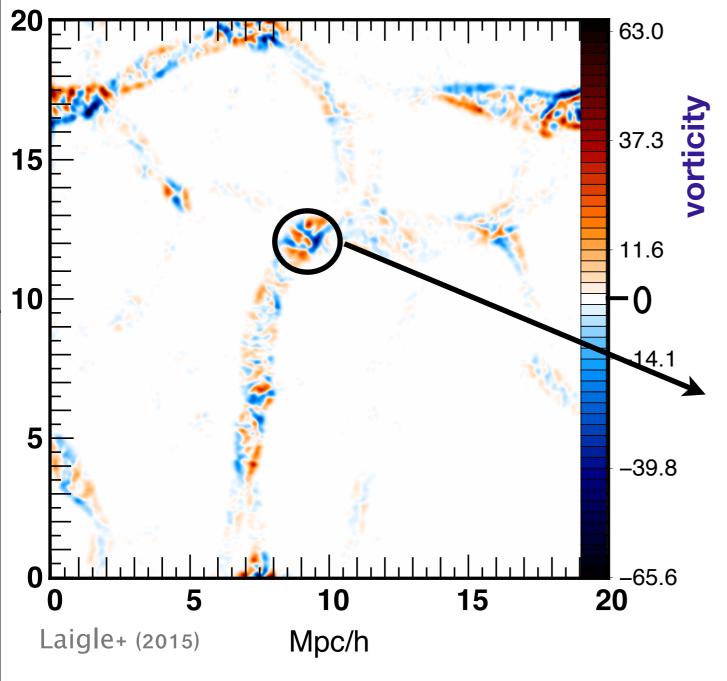
Seoul Feb 2nd 2016

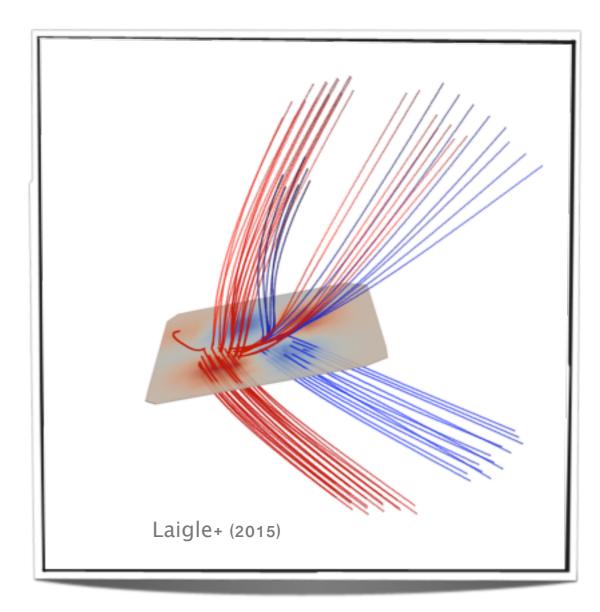
Vorticity generation

In the initial phase of structure formation, flows are laminar and curl-free.

This is no longer valid at the shell-crossing.

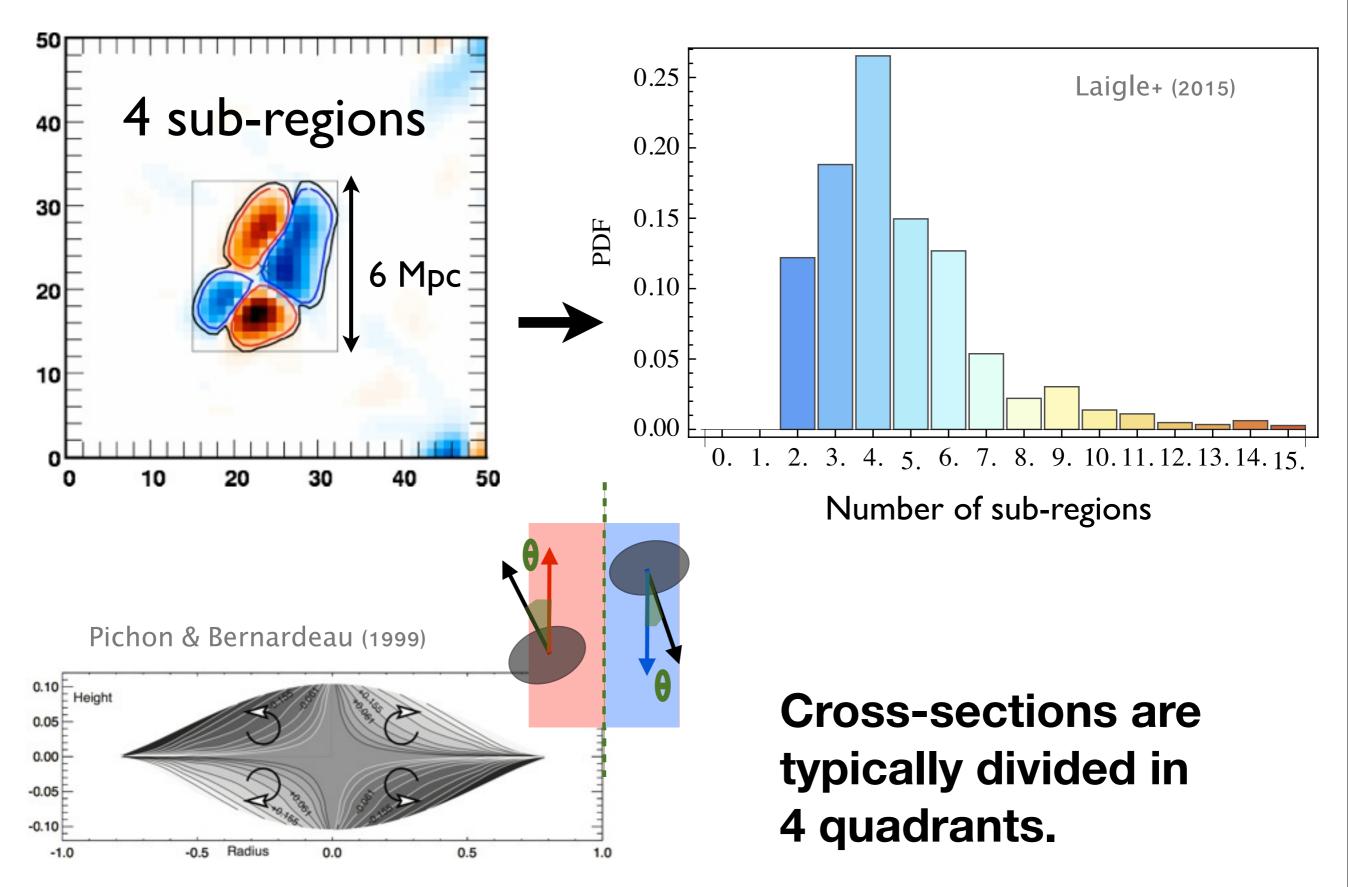
Thin slice of a DM simulation at z=0.





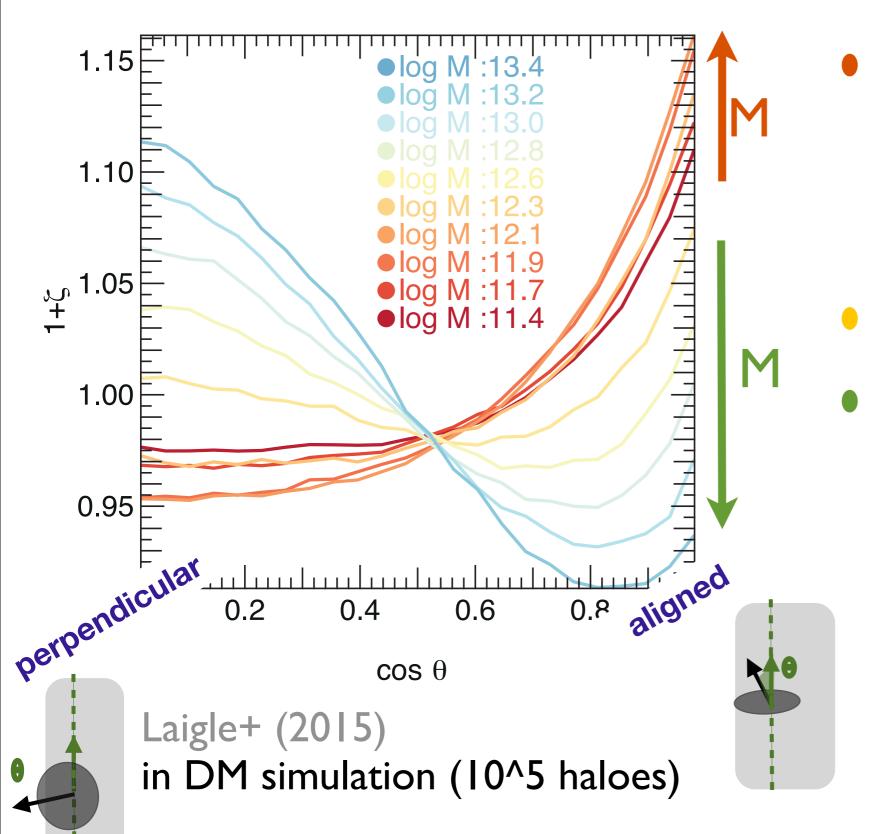
Vorticity is generated and is confined in the filaments.

Geometry of the vorticity cross-section



Theoretical prediction from Pichon & Bernardeau 1999

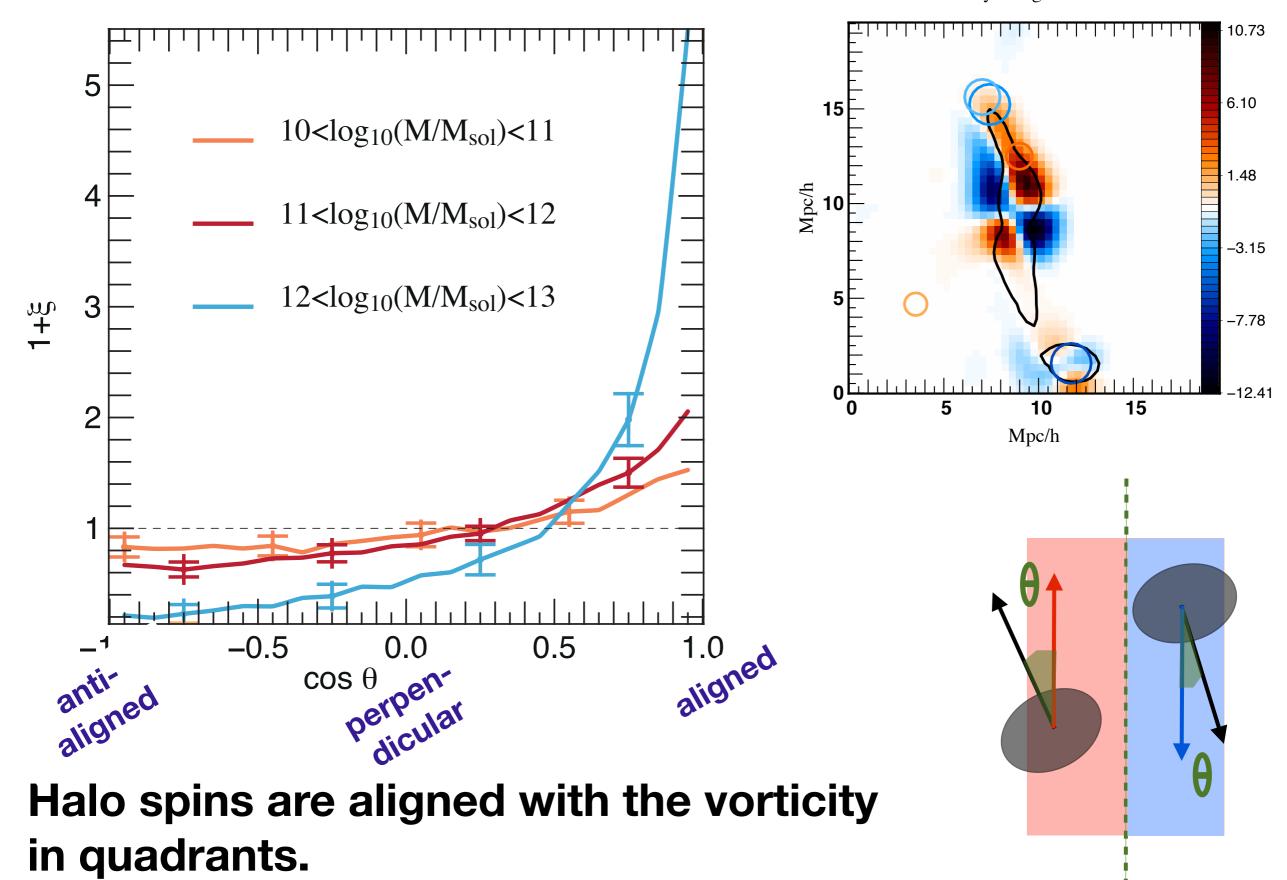
Mass dependent Halo spin - filament alignment



- Mhalo < Mcrit
 alignment of halo spin
 with filament increases
 with mass.
- Mcrit
- Mhalo > Mcrit
 halo spin tends to be
 perpendicular to the
 filament.

Halo-spin vorticity alignment

vorticity along the filament



22

Geometry of the vorticity cross-section Laigle+ (2015) 1.0 vorticity/max(vorticity) 0.8 0.6 Stacked profile 0.2 edge of the 0.0 0.0 filament 8.0 0.2 0.6 r /rmax Pichon & Bernardeau (1999) y position ocal vorticity

High vorticity regions are located at the edges of the filament.

0.2

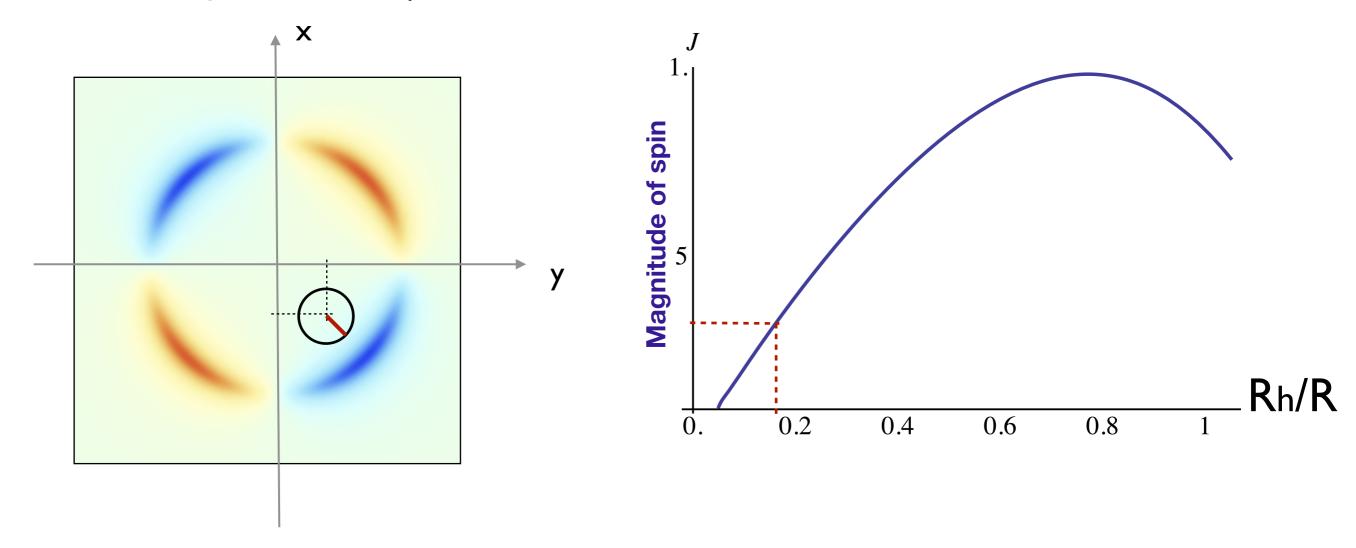
0.4

0.0

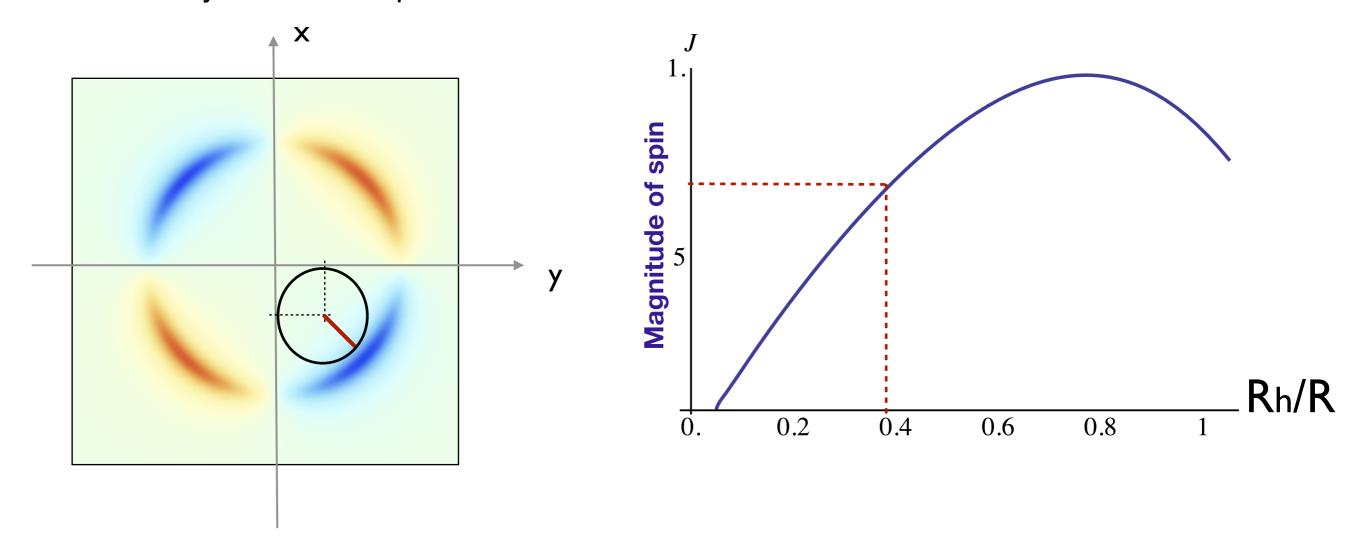
8.0

0.6

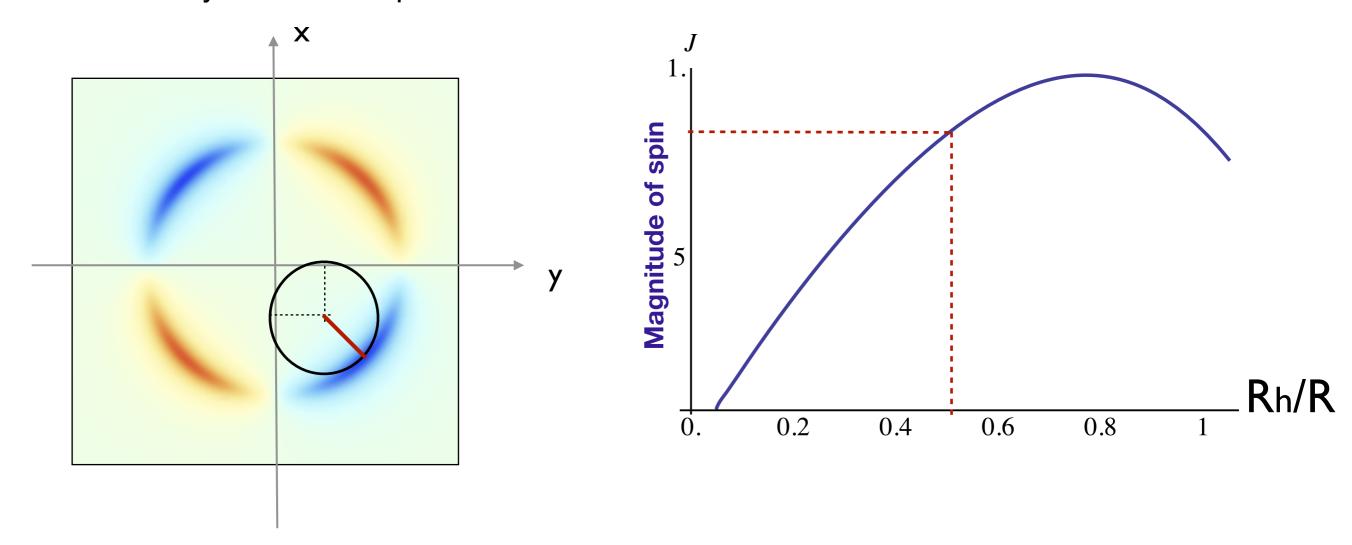
Idealized toy model: The position is fixed and the radius of the halo increases:



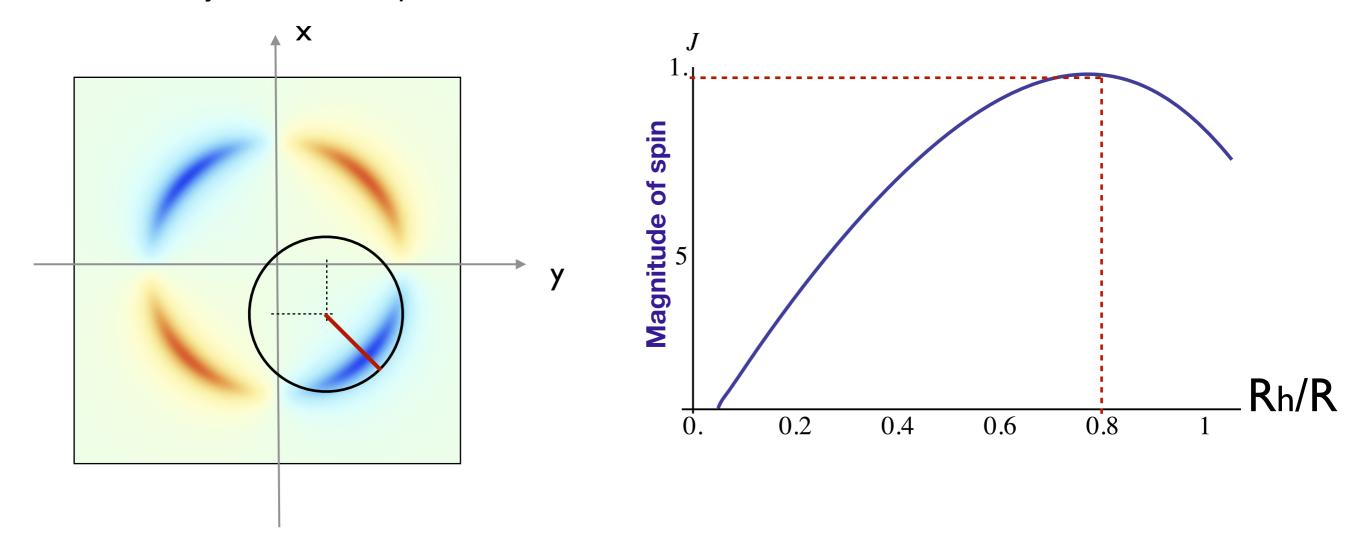
Idealized toy model: The position is fixed and the radius of the halo increases:



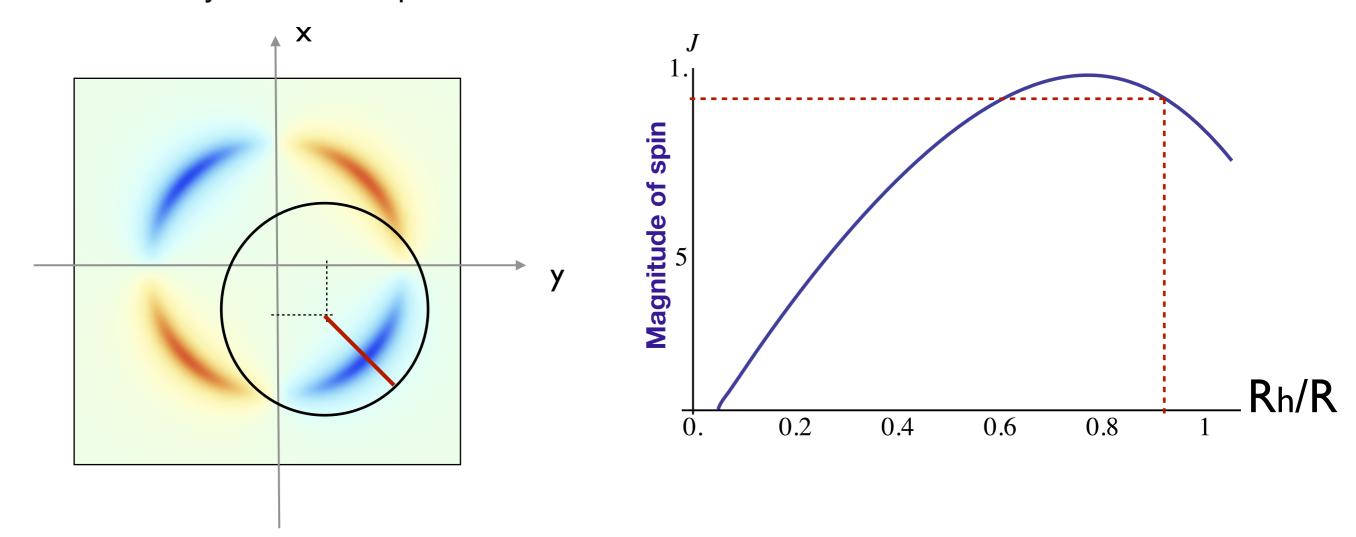
Idealized toy model: The position is fixed and the radius of the halo increases:



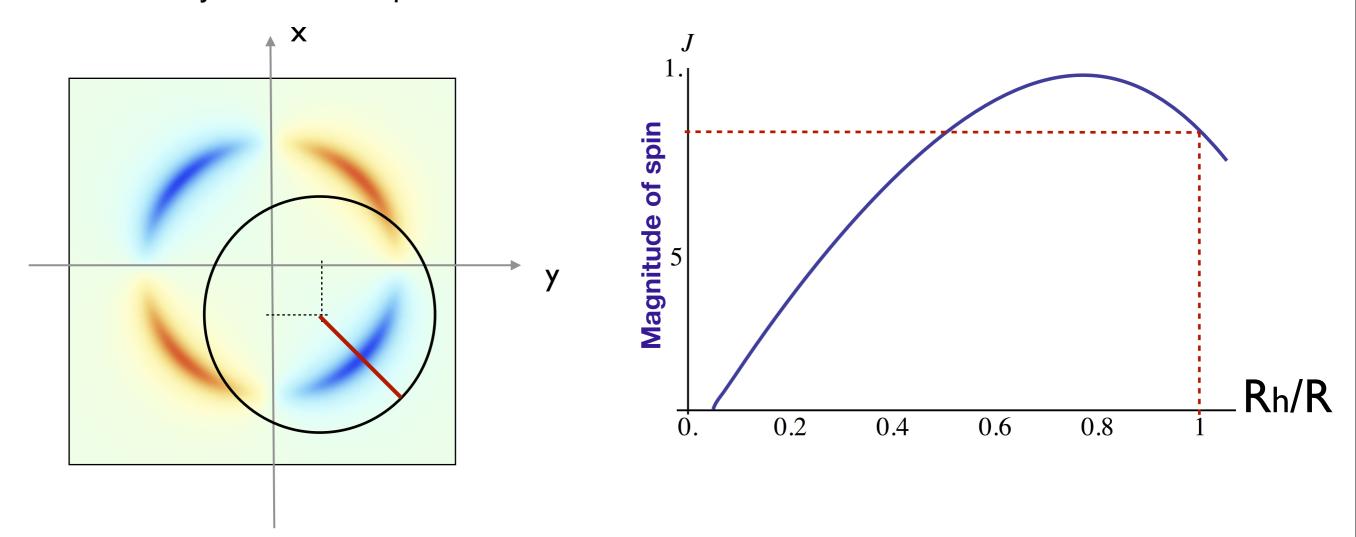
Idealized toy model: The position is fixed and the radius of the halo increases:



Idealized toy model: The position is fixed and the radius of the halo increases:

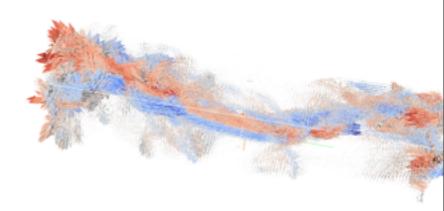


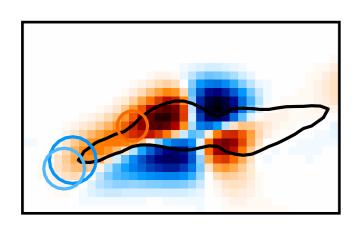
Idealized toy model: The position is fixed and the radius of the halo increases:



in short...

Vorticity is confined in the filaments, and aligned with them. The cross-section with a plane perpendicular to the filament is typically quadripolar.

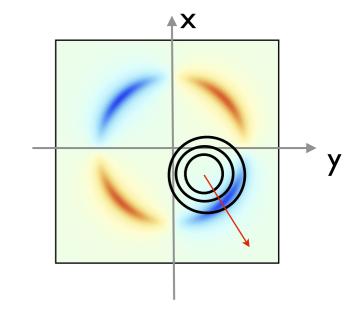






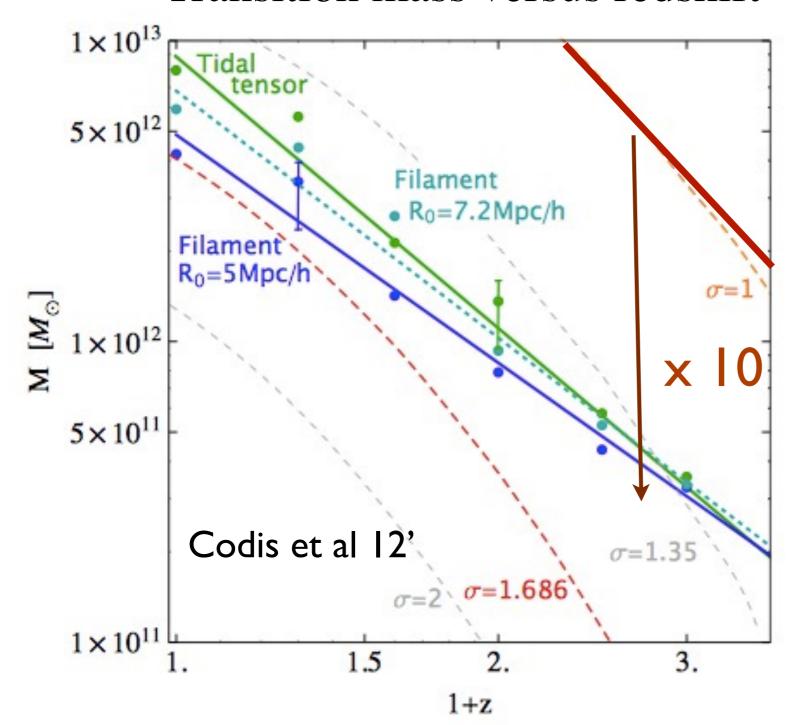
Halo spins are aligned with the same polarity as vorticity in quadrants.

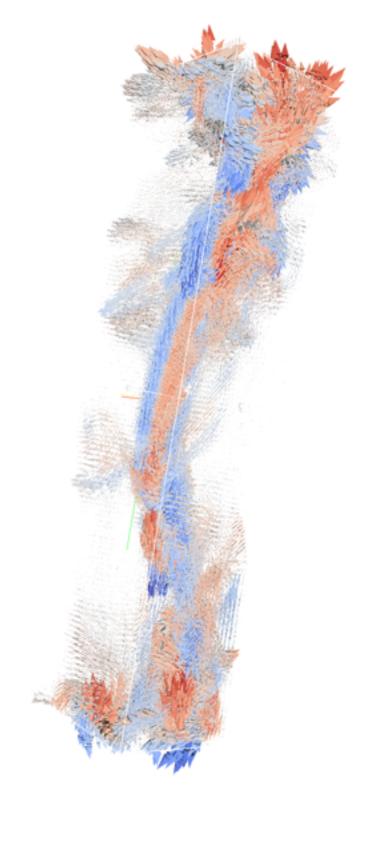
Qualitatively, the transition mass in the alignment is correlated with the size of the quadrant.



Explain transition mass? YES!

Transition mass versus redshift

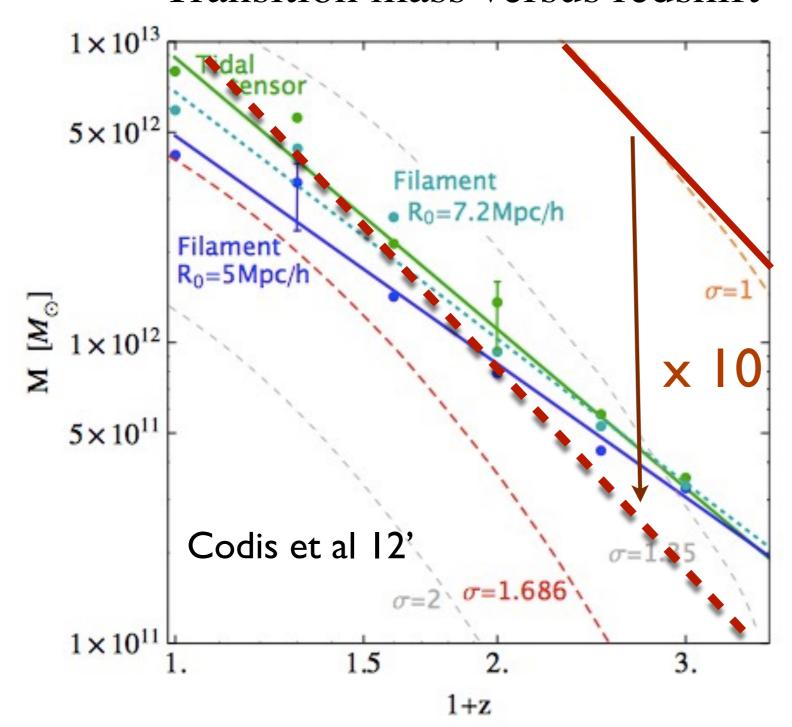


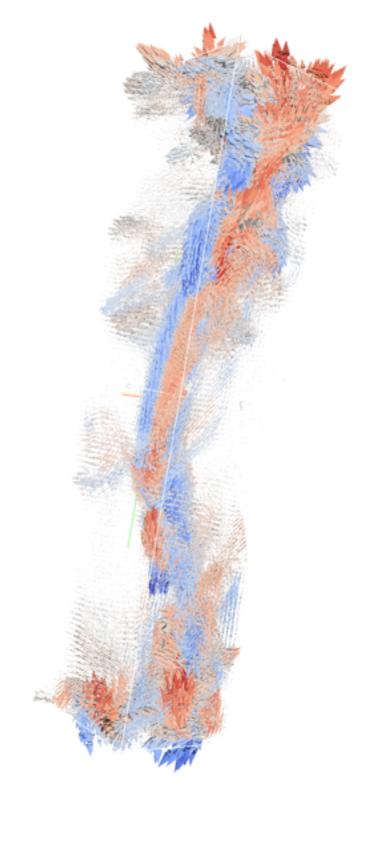


Only 2 ingredients: a) spin is spin one b) filaments flattened

Explain transition mass? YES!

Transition mass versus redshift





Only 2 ingredients: a) spin is spin one b) filaments flattened

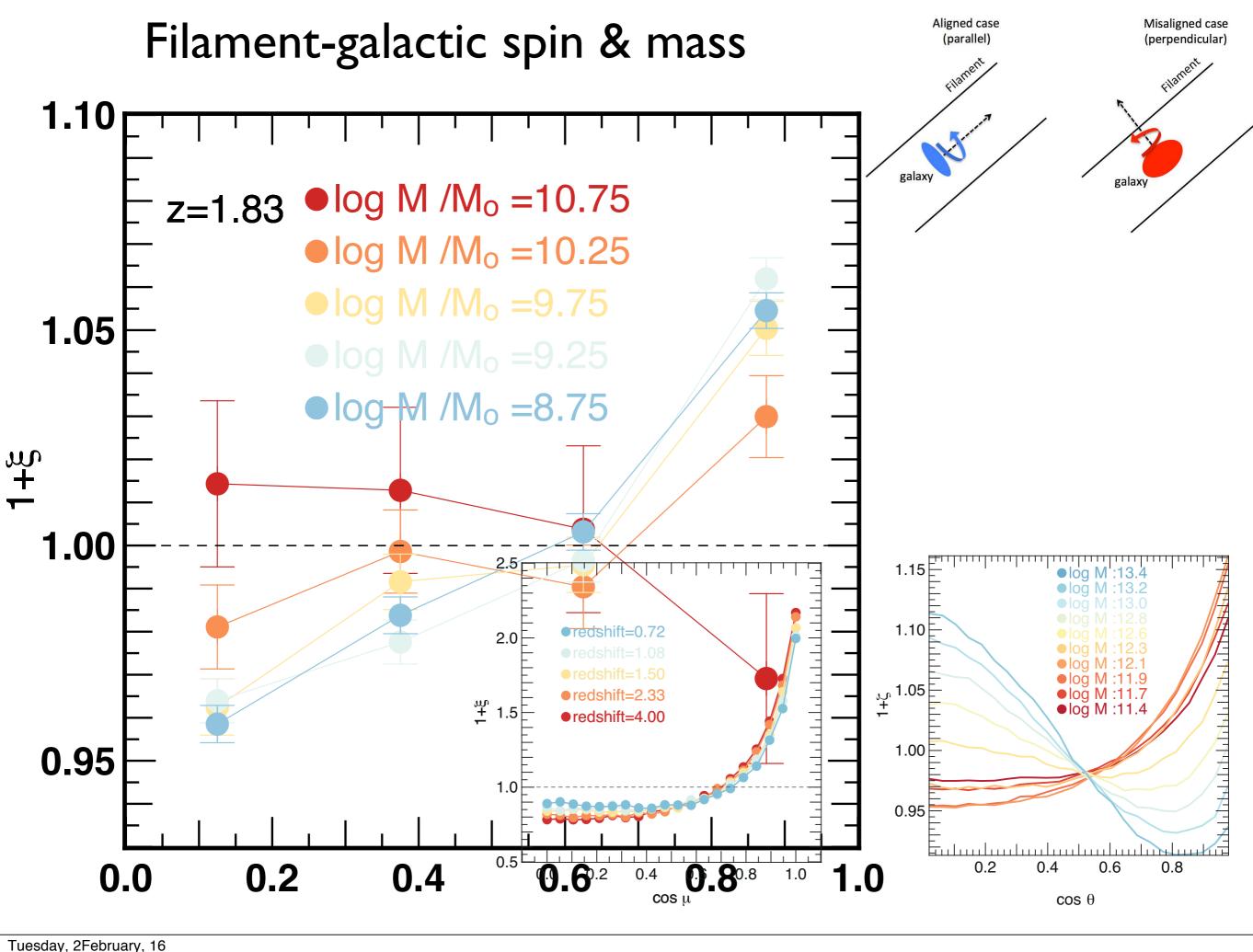
Take home message...

- Morphology (= AM stratification) driven by LSS in cosmic web: can explain Es & Sps where, how & why from ICs
- Signature in correlation between spin and internal kinematic structure of cosmic web on larger scales.
- Process driven by simple PBS/biassed clustering dynamics:
 - requires updating TTT to saddles: simple theory :-)
 - can be expressed into an Eulerian theory via vorticity

Where galaxies form does matter, and can be traced back to ICs
Flattened filaments generate point-reflection-symmetric AM/vorticity distribution:
they induce the observed spin transition mass

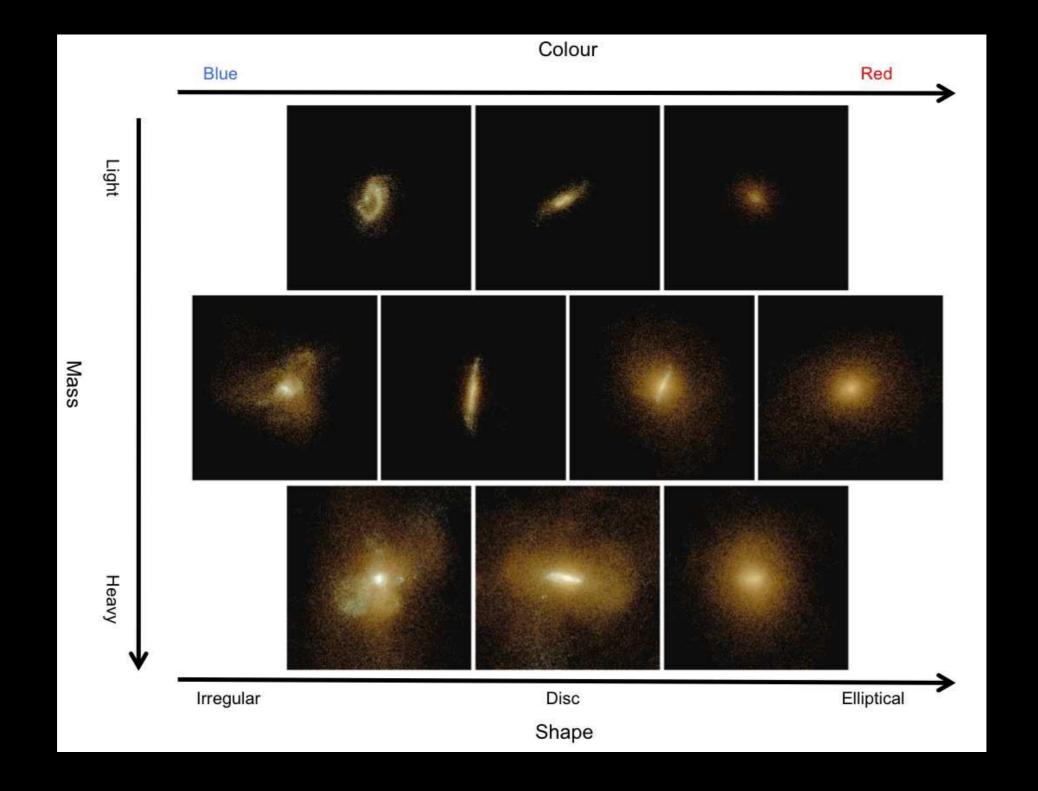
What about galaxies ?? Horizon-AGN simulation Jade (CINES) PART IV (PI Y. Dubois, Co-I J. Devriendt & C. Pichon) - L_{box}=100 Mpc/h 1024³ DM particles M_{DM.res}=8x10⁷ M_{sun} Finest cell resolution dx=1 kpc Gas cooling & UV background heating Low efficiency star formation Stellar winds + SNII + SNIa O, Fe, C, N, Si, Mg, H AGN feedback radio/quasar Outputs (backed up and analyzed on BEYOND) Simulation outputs Lightcones (1°x1°) performed on-the-fly Dark Matter (position, velocity) Gas (position, density, velocity, pressure, chemistry) Stars (position, mass, velocity, age, chemistry) Black holes (position, mass, velocity, accretion rate) z=1.5 using 3 Mhours on 4096 cores horizon-AGN.projet-horizon.fr Tuesday, 2February, 16

1 Mpc z = 38.305

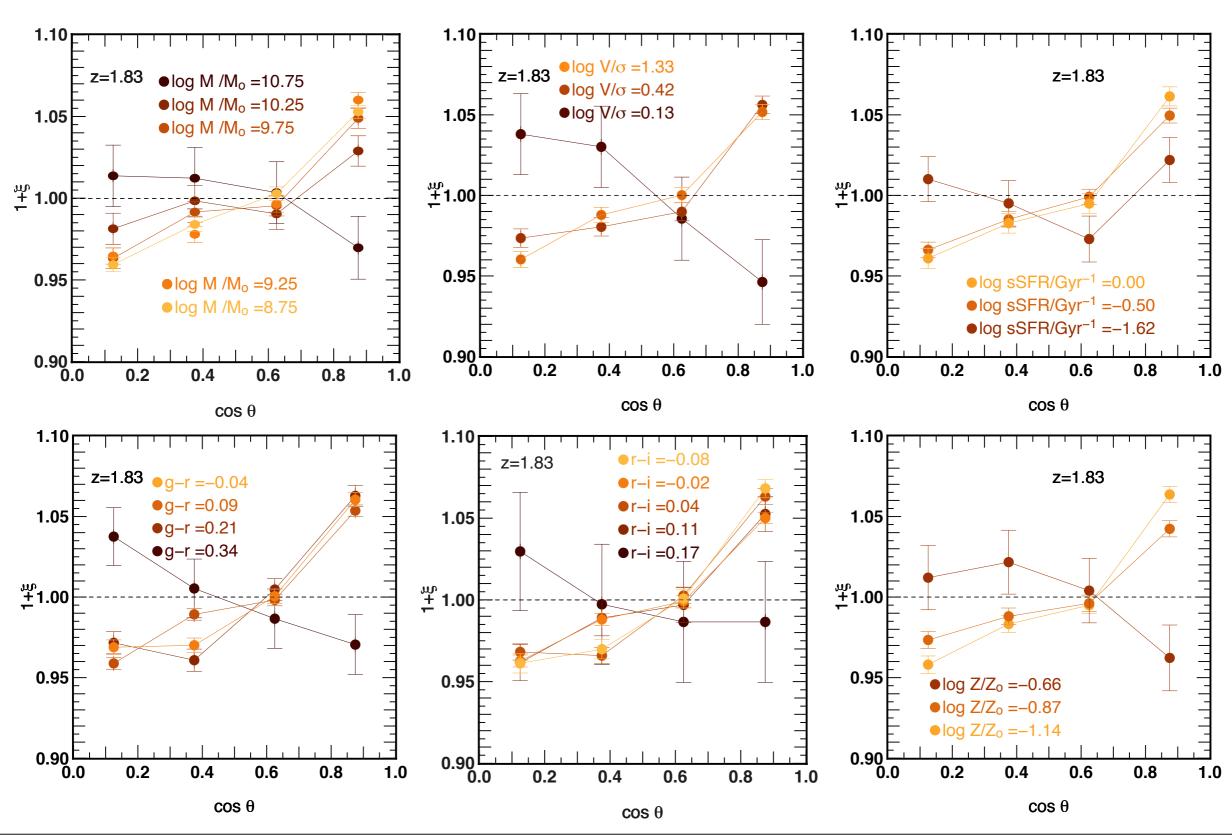


can morphology trace spin flip?

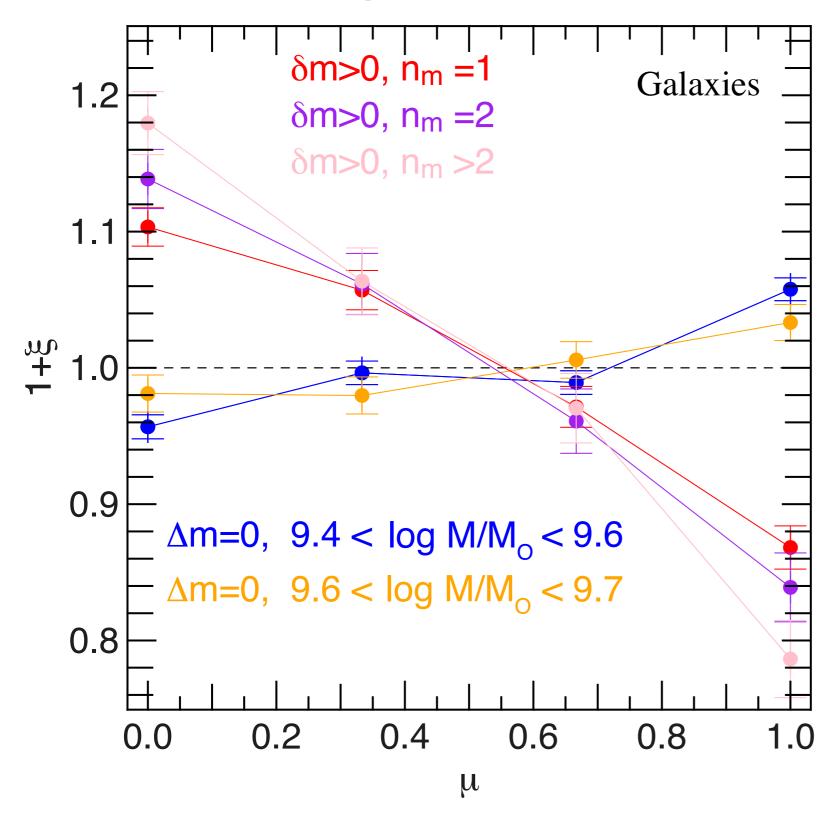
thanks to AGN feedback we have morphological diversity



Can morphological/physical properties of galaxies trace spin flip?

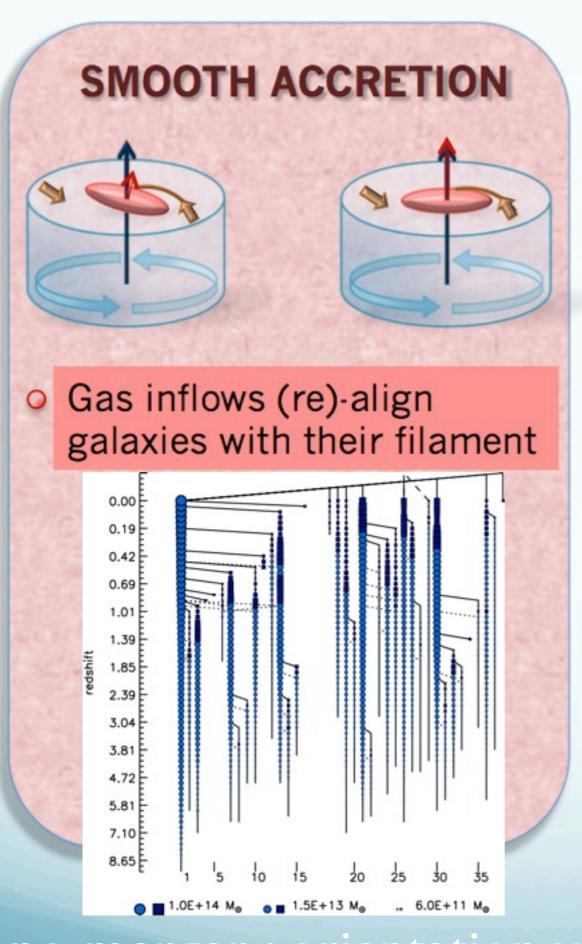


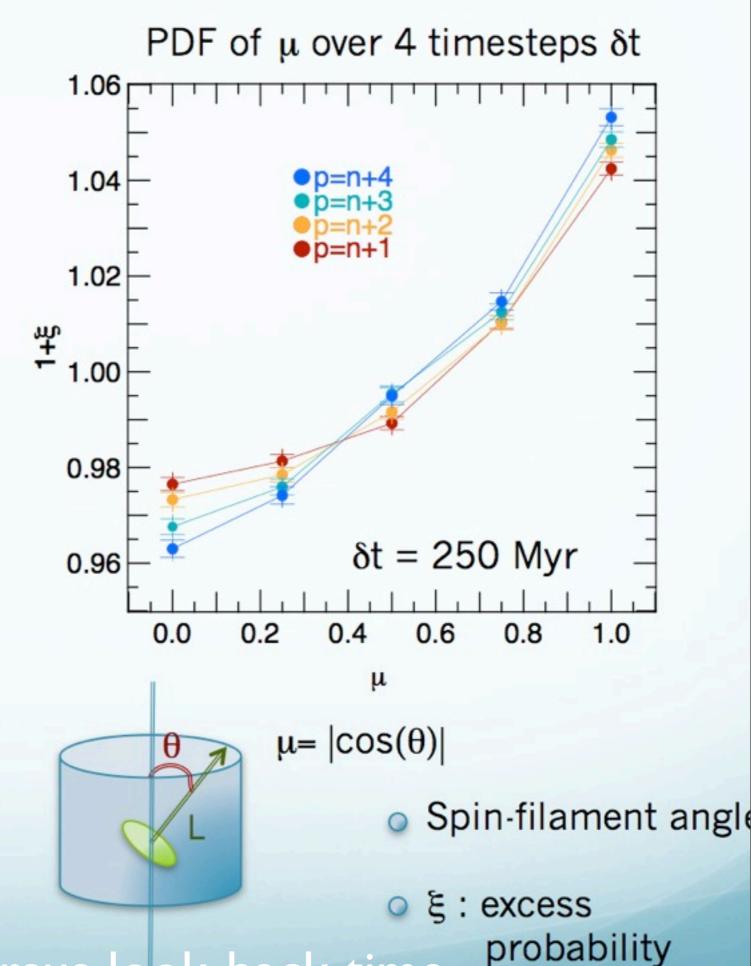
What is the *physical* origin of spin flip? high mass galaxies merge!





Transition mass versus merging rate for galaxies





no merger : orientation versus look-back time

Caught in the rhythm: satellites in their galactic plane

C. Welker^{1*}, Y. Dubois¹, C. Pichon^{1,2}, J. Devriendt^{3,4} and N. E. Chisari³

