

Metastability, Chaotic Inflation, and Primordial Black Holes

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Based on [1605.04974 \(PhysRevD.94.063509\)](#)

In collaboration with M.Kawasaki, T.T.Yanagida

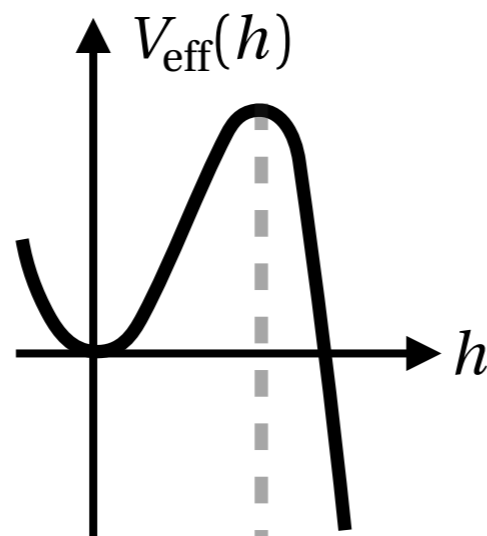
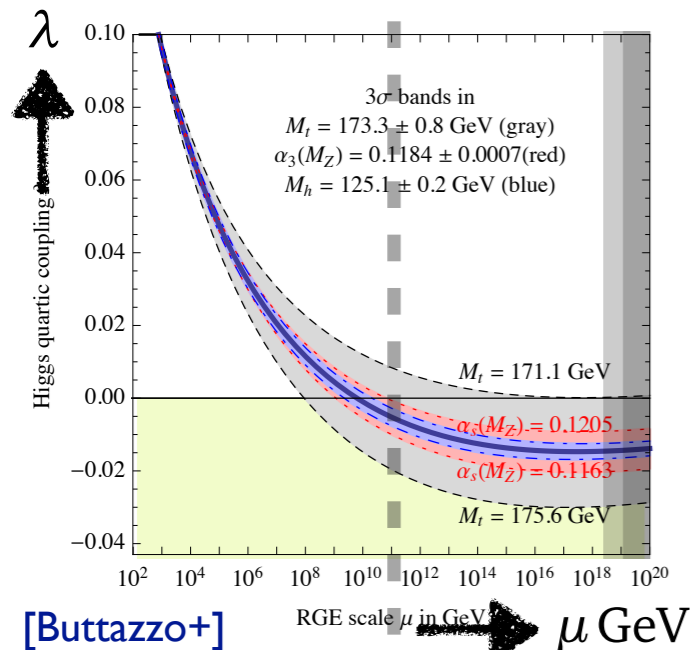


Introduction

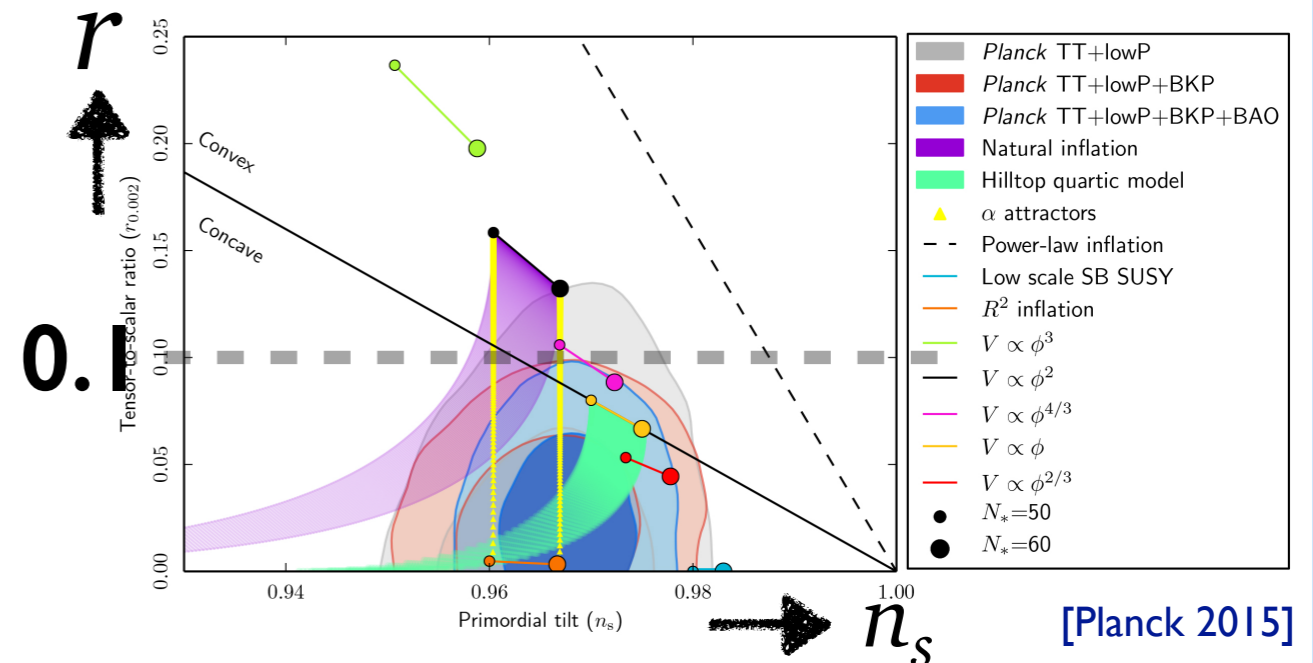
Metastability v.s. Inflation

Metastable Electroweak Vacuum v.s. Chaotic Inflation

- SM valid up to high energy scales
 - Our vacuum: likely to be metastable?
 - $\lambda < 0$ for $\mu > 10^{10}$ GeV @ best-fit of top Yukawa.



- Chaotic Inflation
 - Solve the *initial condition problem*. [See e.g. 1601.01918]
 - Large tensor-to-scalar ratio: r .



$$h_{\max} \sim 10^{10} \text{ GeV} \quad \text{v.s.} \quad H_{\text{inf}} \sim 10^{14} \text{ GeV} \sqrt{\frac{r}{0.1}}$$

© Hawking-Moss transition

- Higgs acquires large fluctuations of

$$T_{\text{GH}} = \frac{H_{\text{inf}}}{2\pi}$$



Severe Tension

$$H_{\text{inf}} \lesssim 10^9 \text{ GeV} \left(\frac{h_{\max}}{10^{10} \text{ GeV}} \right)$$

One order of magnitude severer bound is obtained if you look at e^{3N} patches.

Metastability v.s. Inflation

■ Curvature coupling of Higgs: $\xi R h^2$

- Stabilize the EW vacuum during inflation @ $\xi > \mathcal{O}(0.1)$

$$-\mathcal{L}_{\text{int}}(\phi, h) = \frac{1}{2} \xi R h^2$$

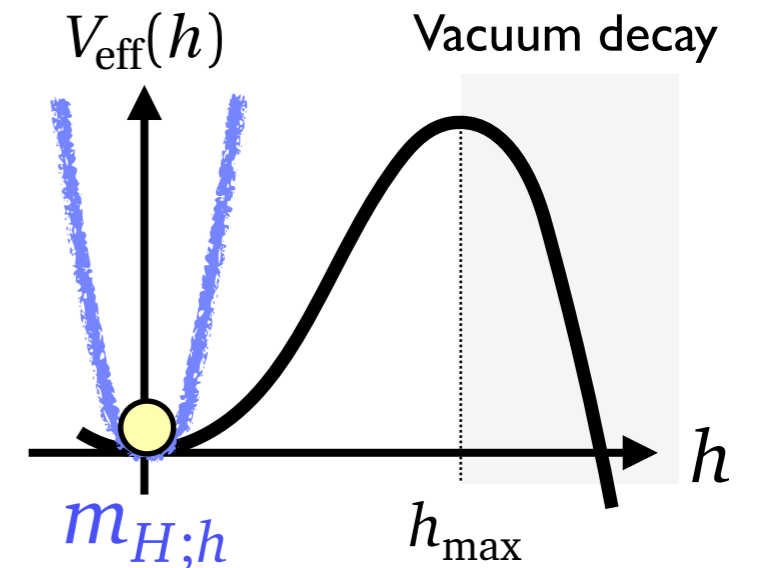


during inflation

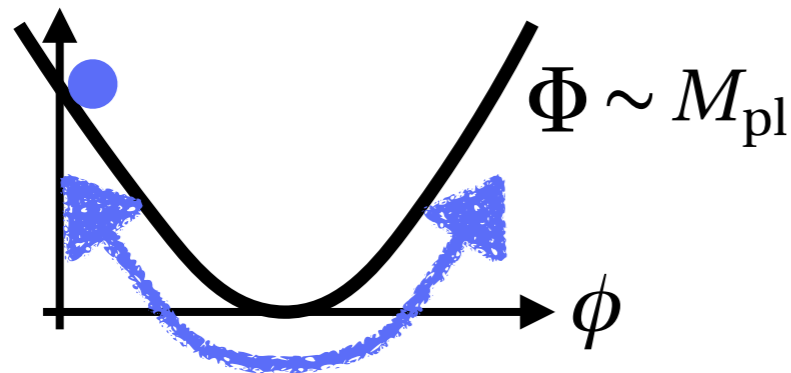
$$m_{H;h}^2 = 12\xi H_{\text{inf}}^2$$

stabilized for

$$\gtrsim H_{\text{inf}}^2$$



- However, the “tachyonic resonance” can destabilize it afterwards!



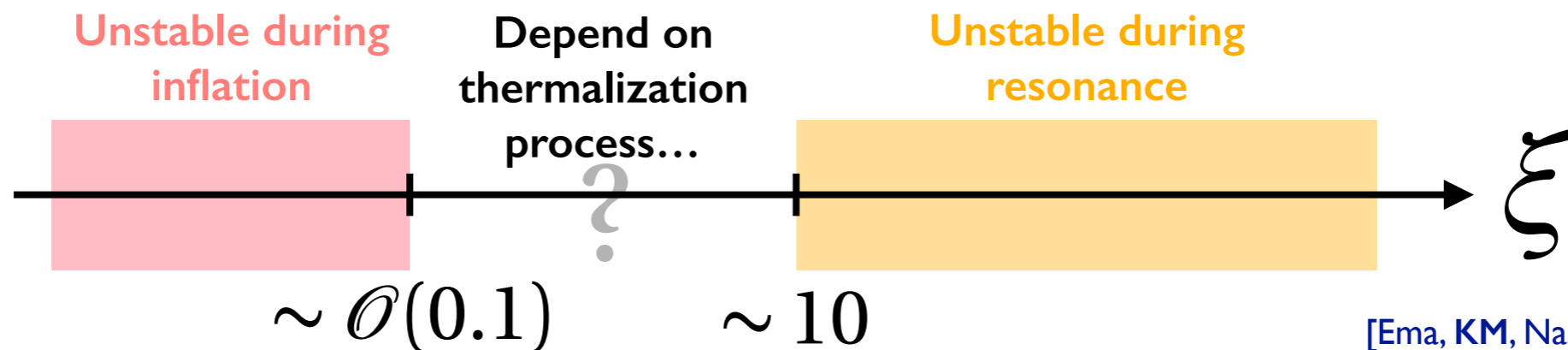
- Oscillating mass term

$$R = \frac{1}{M_{\text{pl}}^2} [4V(\phi) - \dot{\phi}^2]$$



Tachyonic Resonance

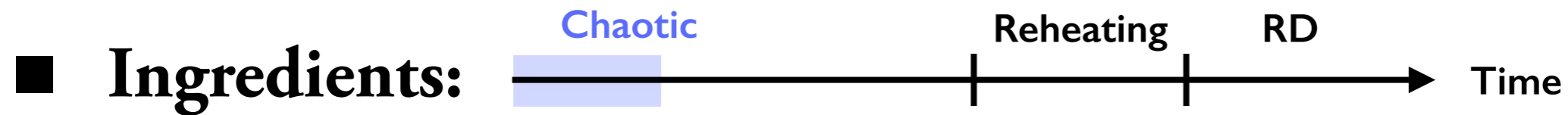
$$q \sim \frac{\xi \Phi^2}{M_{\text{pl}}^2} \gtrsim 1$$



[Ema, KM, Nakayama; Herranen+]

Our Scenario

What we have discussed



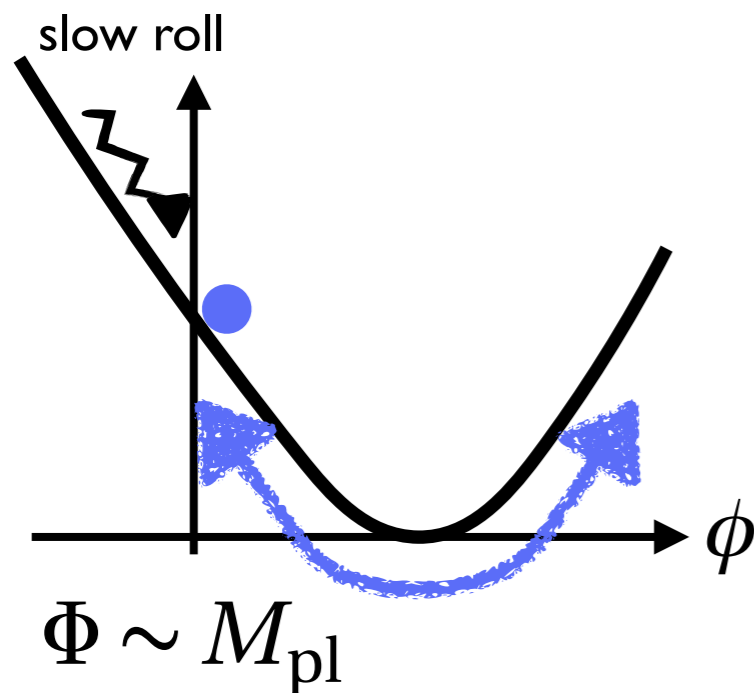
- **Chaotic inflation**

- Solve the initial condition problem + provide primordial density perturbations

- **Curvature coupling**

- Stabilize the EW vacuum during inflation(s) + universally couples to the trace of energy-momentum

- **However, the “resonance” can destabilize it afterwards!**



- End of slow roll

$$\epsilon_V = \frac{M_{\text{pl}}^2}{2} \left(\frac{V'}{V} \right)^2, \quad \eta_V = M_{\text{pl}}^2 \frac{V''}{V}$$

$$\max[\epsilon_V, |\eta_V|] = 1$$



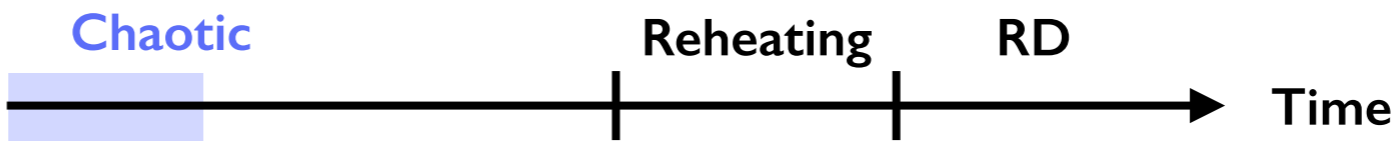
For chaotic inflation

$$\Phi \sim M_{\text{pl}}$$

Resonance is inevitable

$$q \sim \frac{\xi \Phi^2}{M_{\text{pl}}^2} \gtrsim 1$$

Our Scenario

■ **Ingredients:**  Chaotic Reheating RD Time

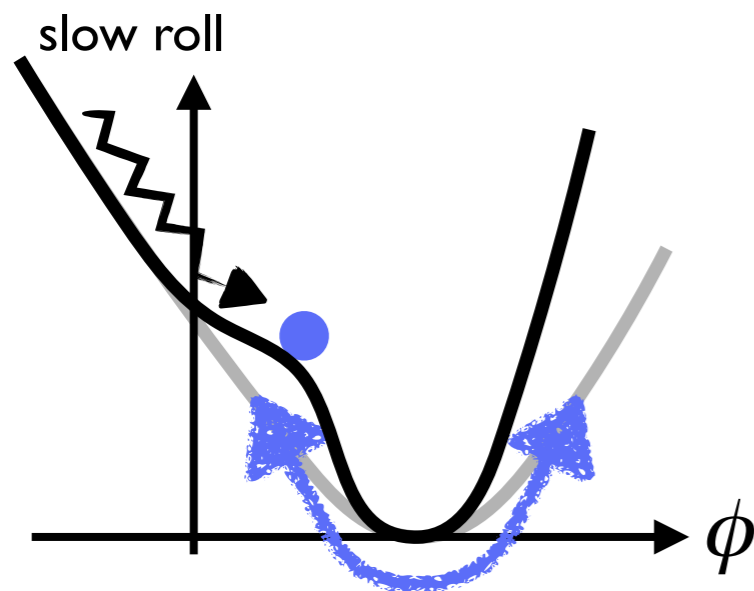
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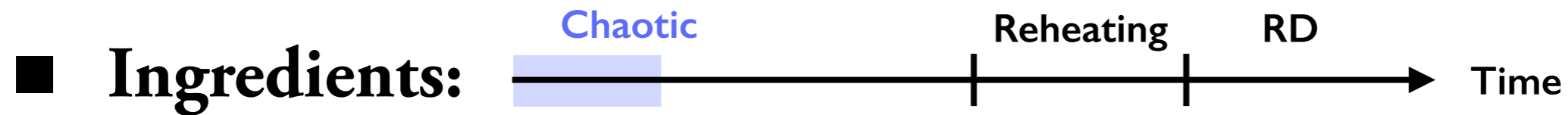
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- Stabilize the EW vacuum during inflation(s) + universally couples to the trace of energy-momentum

- If the potential is **flat** near the origin,...



Our Scenario



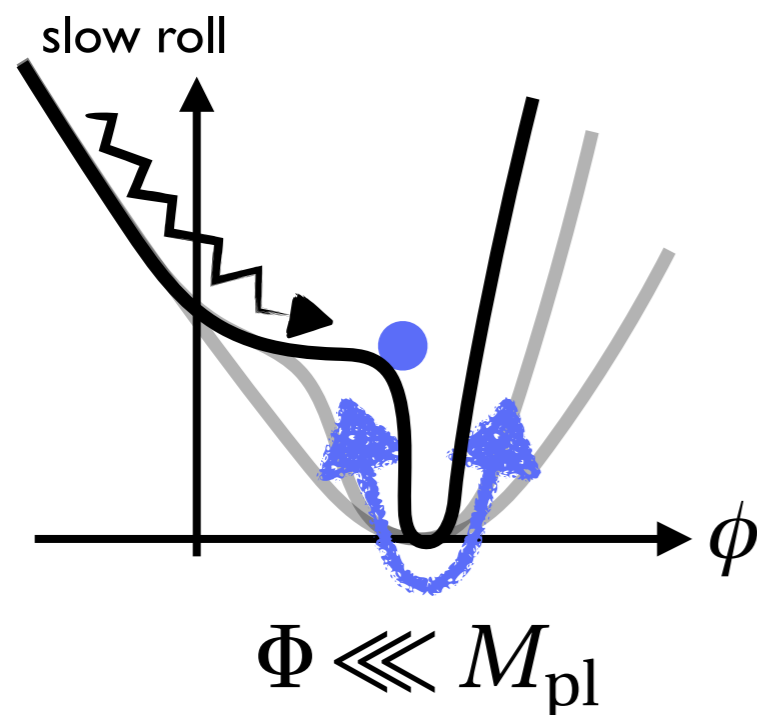
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No Resonance

$$q \sim \frac{\xi \Phi^2}{M_{pl}^2} \lll 1$$

Our Scenario

■ **Ingredients:**  Time

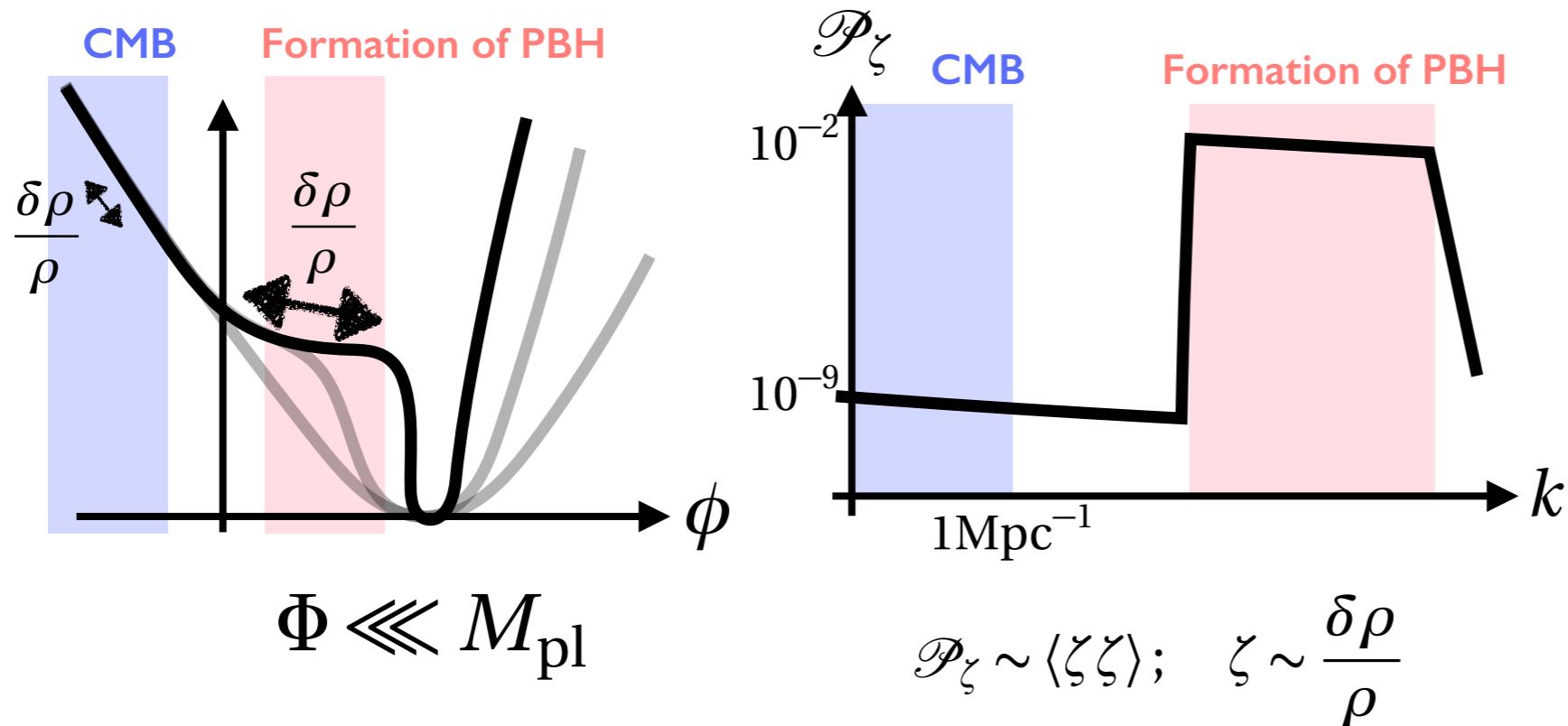
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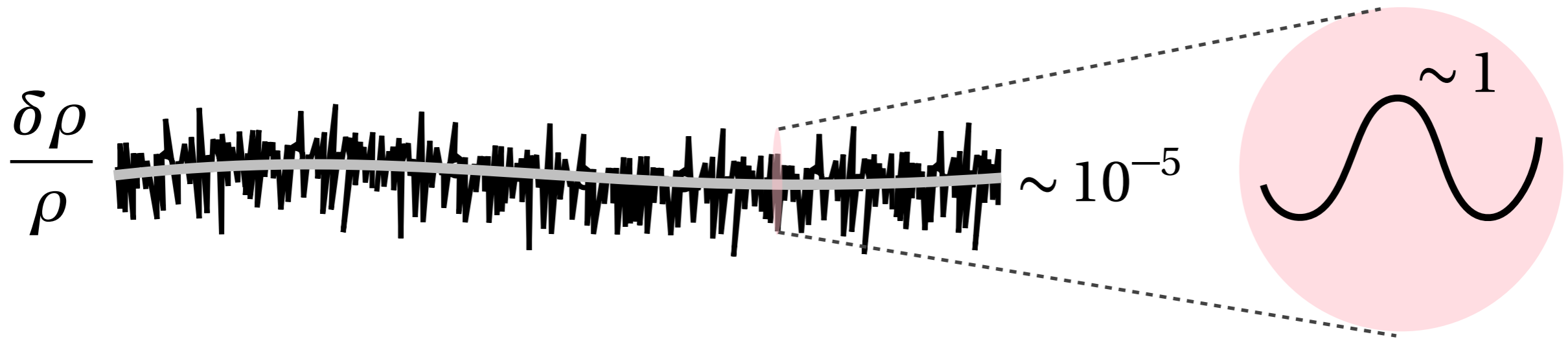
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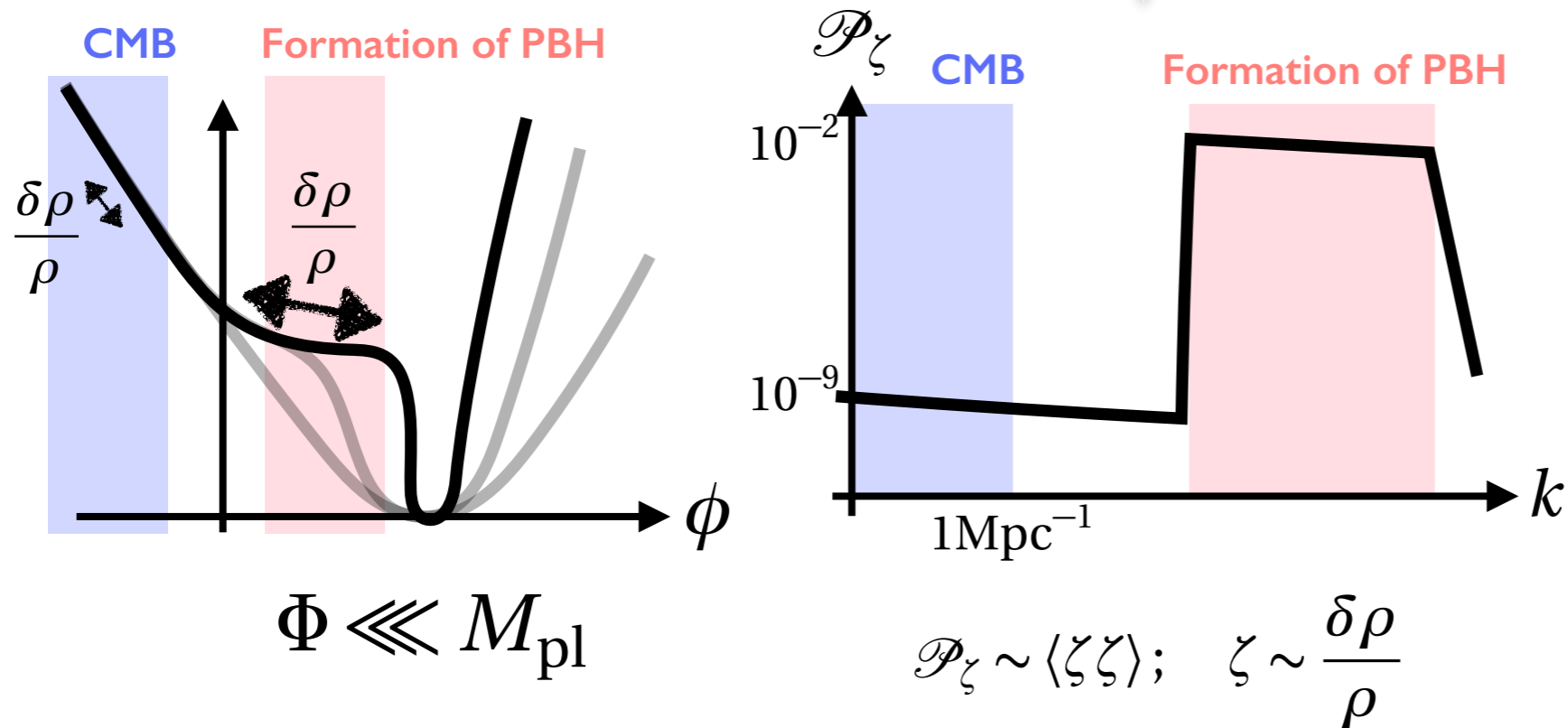
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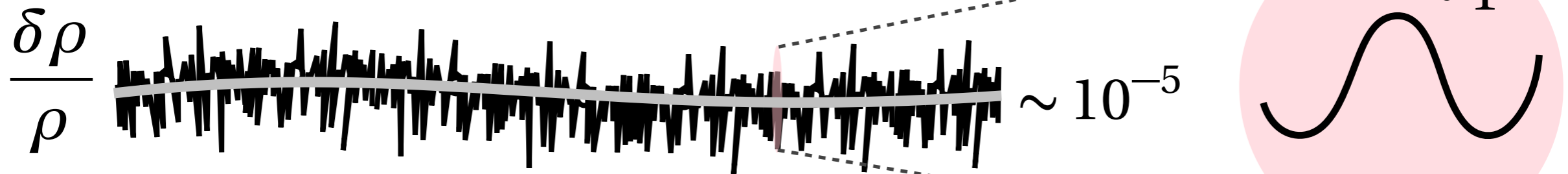
Our Scenario



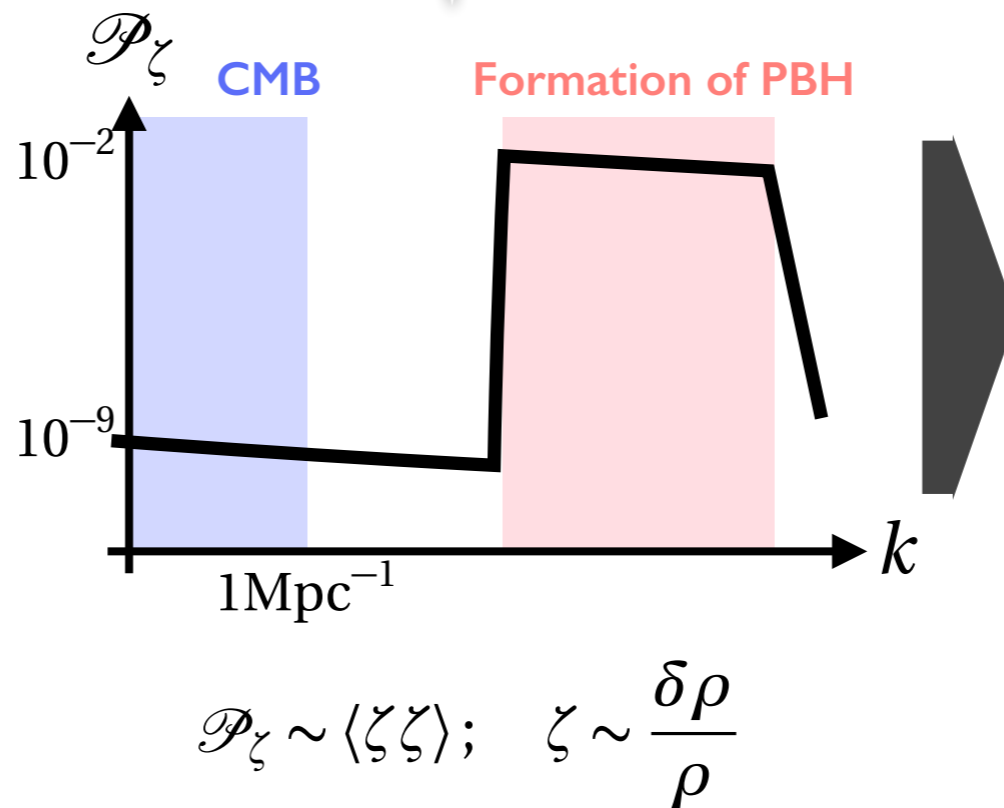
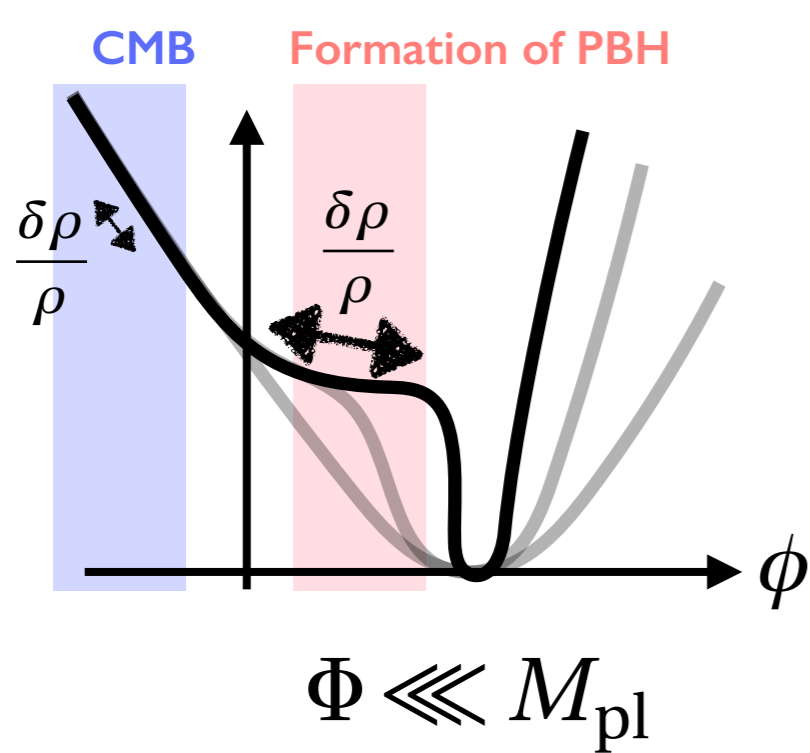
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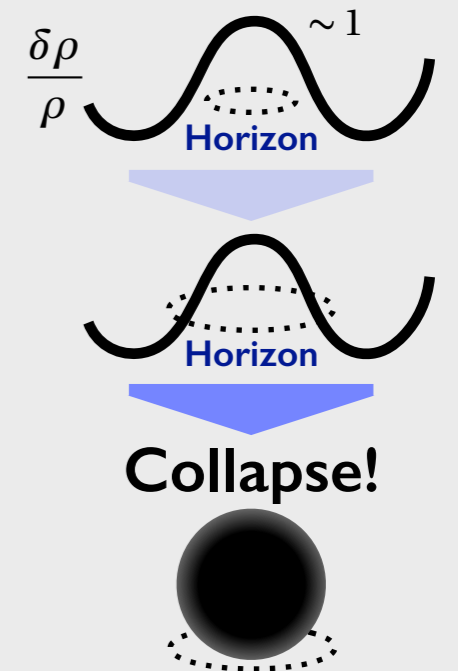
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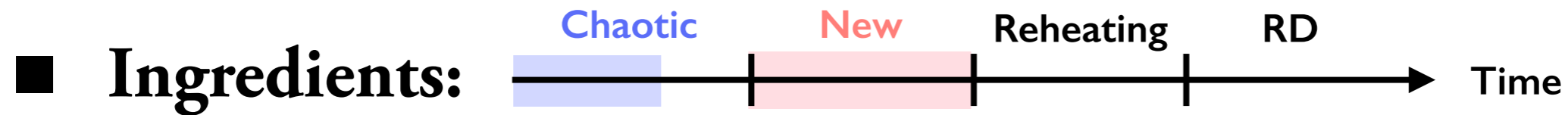
- If the potential is flat near the origin,...



PBH formation



Example: Double Inflation



- **Chaotic inflation**

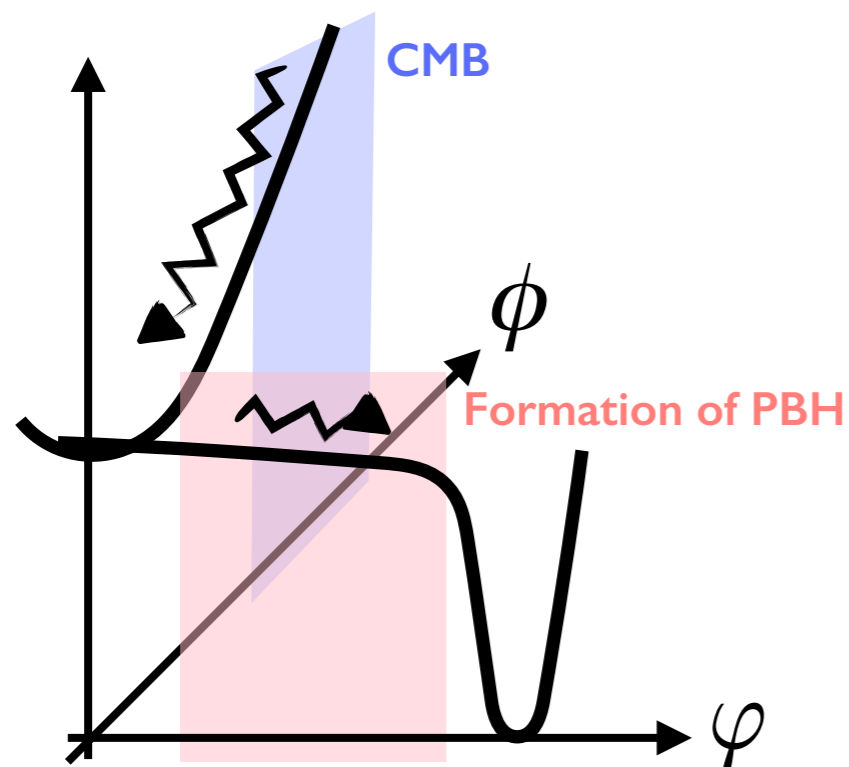
- (0) Solve the initial condition problem + (ii) provide primordial density perturbations.

- **Curvature coupling**

- Stabilize the EW vacuum during inflation(s) + universally couples to the trace of energy-momentum

- **New inflation**

- (i) Avoid the resonance after inflation + (ii) produce **PBHs** as a candidate of DM!



- Stabilize φ during chaotic inflation

$$-\mathcal{L}_{\text{int}} \propto \frac{V_{\text{ch}}(\phi)}{M_{\text{pl}}^2} \varphi^2$$

- Potential in the flat regime (new inflation)

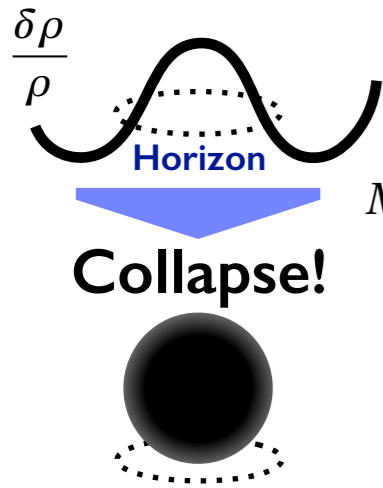
$$V_{\text{new}}(\varphi) = \left(v^2 - g \frac{\varphi^4}{M_{\text{pl}}^2} \right)^2 - \kappa v^4 \frac{\varphi^2}{2M_{\text{pl}}^2} - \epsilon v^4 \frac{\varphi}{M_{\text{pl}}}$$

Example: Double Inflation

■ PBHs as whole Dark Matter

- PBH is formed when the over-dense region enters the horizon.

- PBH mass \propto Horizon mass @ horizon reenter



$$M = \gamma \rho \frac{4\pi H^{-3}}{3} \Big|_{k=aH}$$

$$\simeq M_{\odot} \left(\frac{\gamma}{0.2} \right) \left(\frac{g_*}{3.36} \right)^{-\frac{1}{6}} \left(\frac{k}{2 \times 10^6 \text{ Mpc}^{-1}} \right)^{-2}$$

[Carr, Astrophys. J. 201, 1 (1975)]

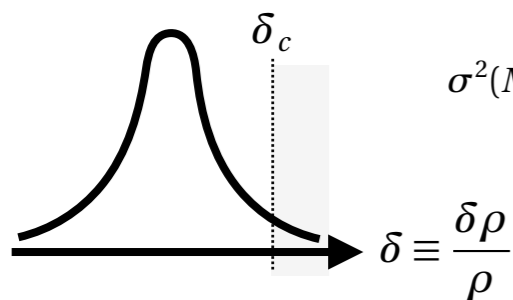
- PBH is formed if $\delta\rho/\rho > \delta_c (=1/3)$.

$$\frac{\Omega_{\text{PBH}}}{\Omega_c} \simeq \left(\frac{\beta(M)}{7 \times 10^{-9}} \right) \left(\frac{\gamma}{0.2} \right)^{1/2} \left(\frac{g_*}{106.75} \right)^{-1/4} \left(\frac{M}{M_{\odot}} \right)^{-1/2}$$

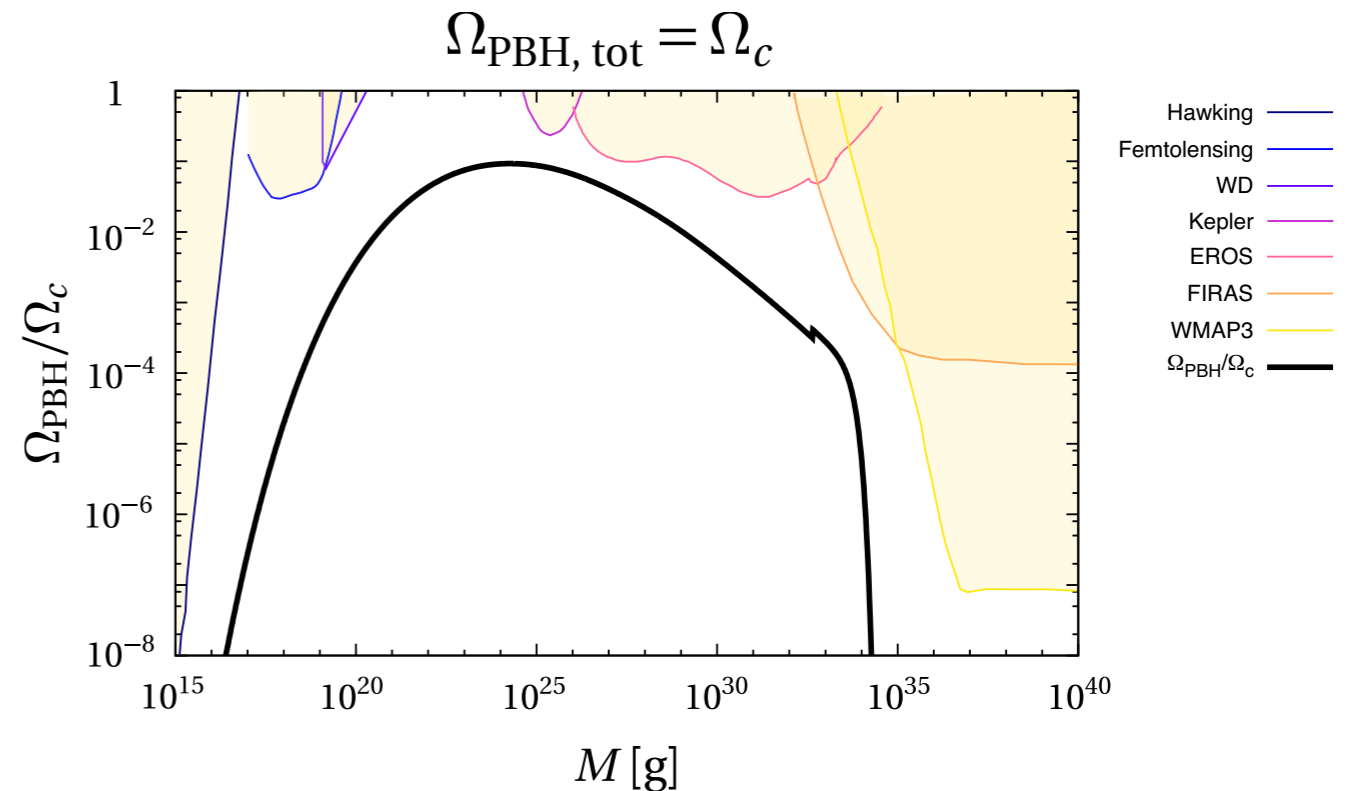
where $\beta(M) = \int_{\delta_c} d\delta \frac{1}{\sqrt{2\pi\sigma^2(M)}} e^{-\delta^2/2\sigma^2(M)}$

$$\sigma^2(M) = \frac{16}{81} \int d\log q W^2(qk^{-1})(qk^{-1})^4 \mathcal{P}_{\zeta}(q)$$

[Carr, Astrophys. J. 201, 1 (1975);
Young et al., JCAP 1407 (2014) 045]



- Abundance of PBHs as a function of mass



* Constraints from Neutron Star capture are evaded for a conservative value of DM inside the globular clusters.

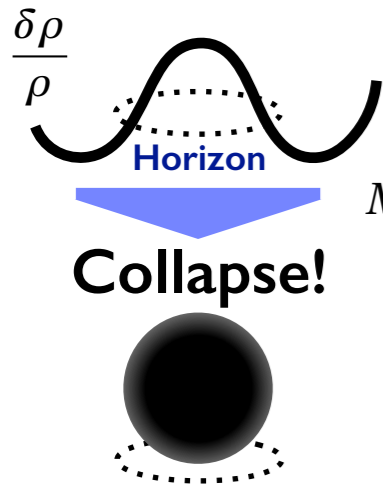
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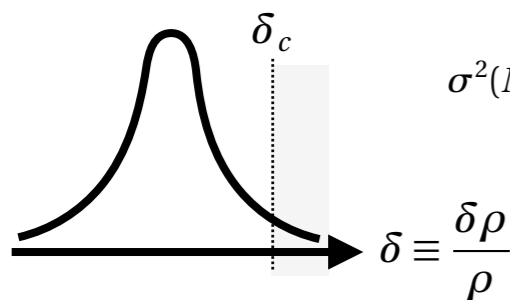
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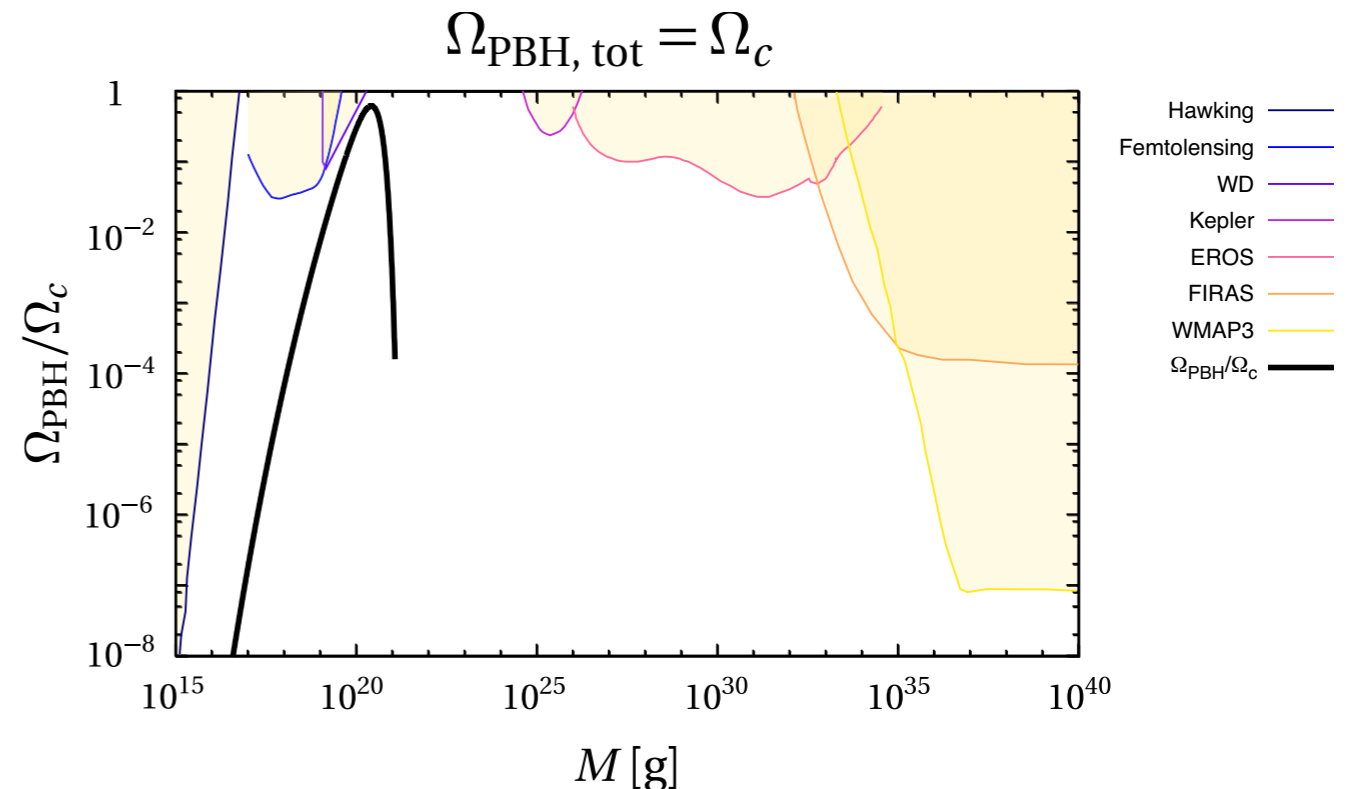
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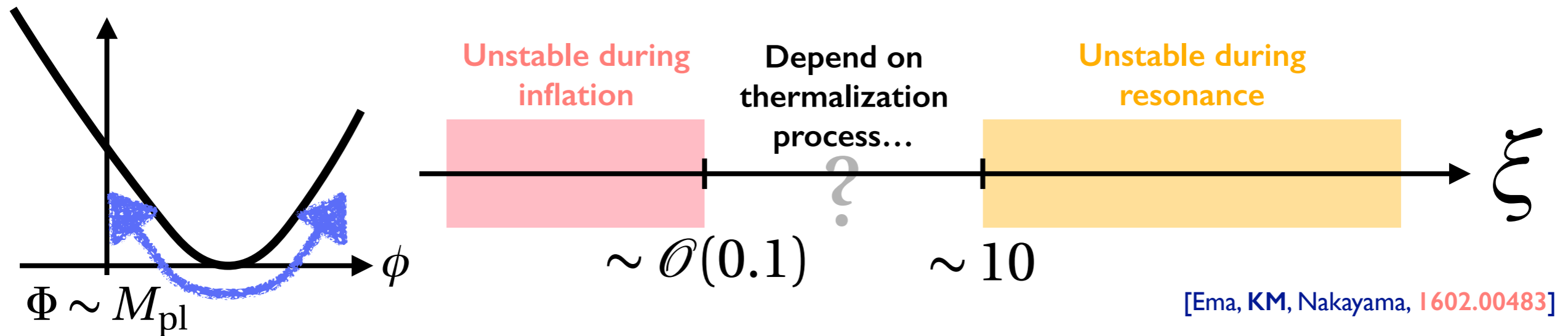
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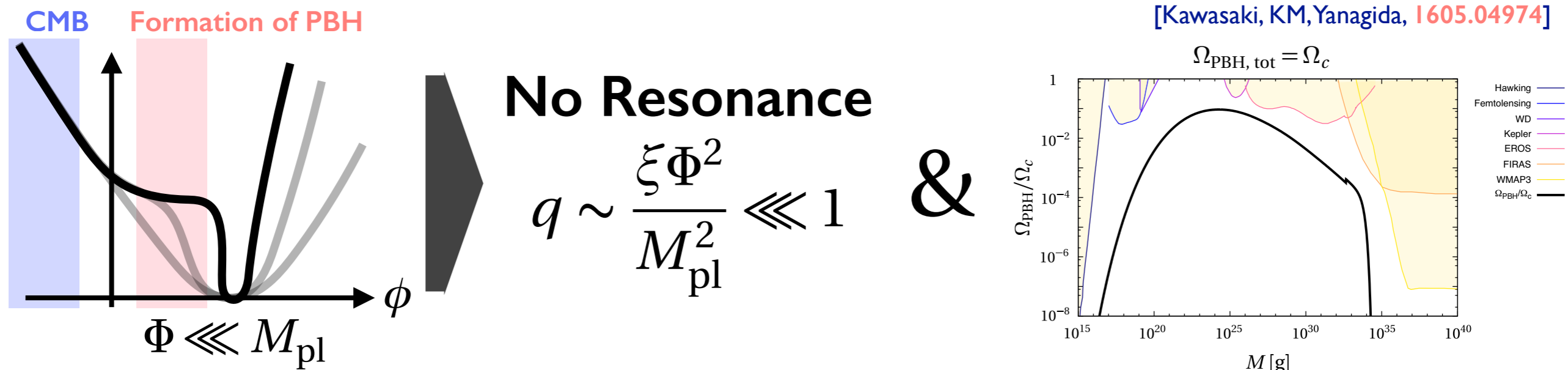
Summary

Summary

Chaotic inflation v.s. Metastable EW Vacuum:



Slight modification of inflaton potential can dramatically **relax the tension**. Moreover, it can generate **PBHs as all DM!**



Back up

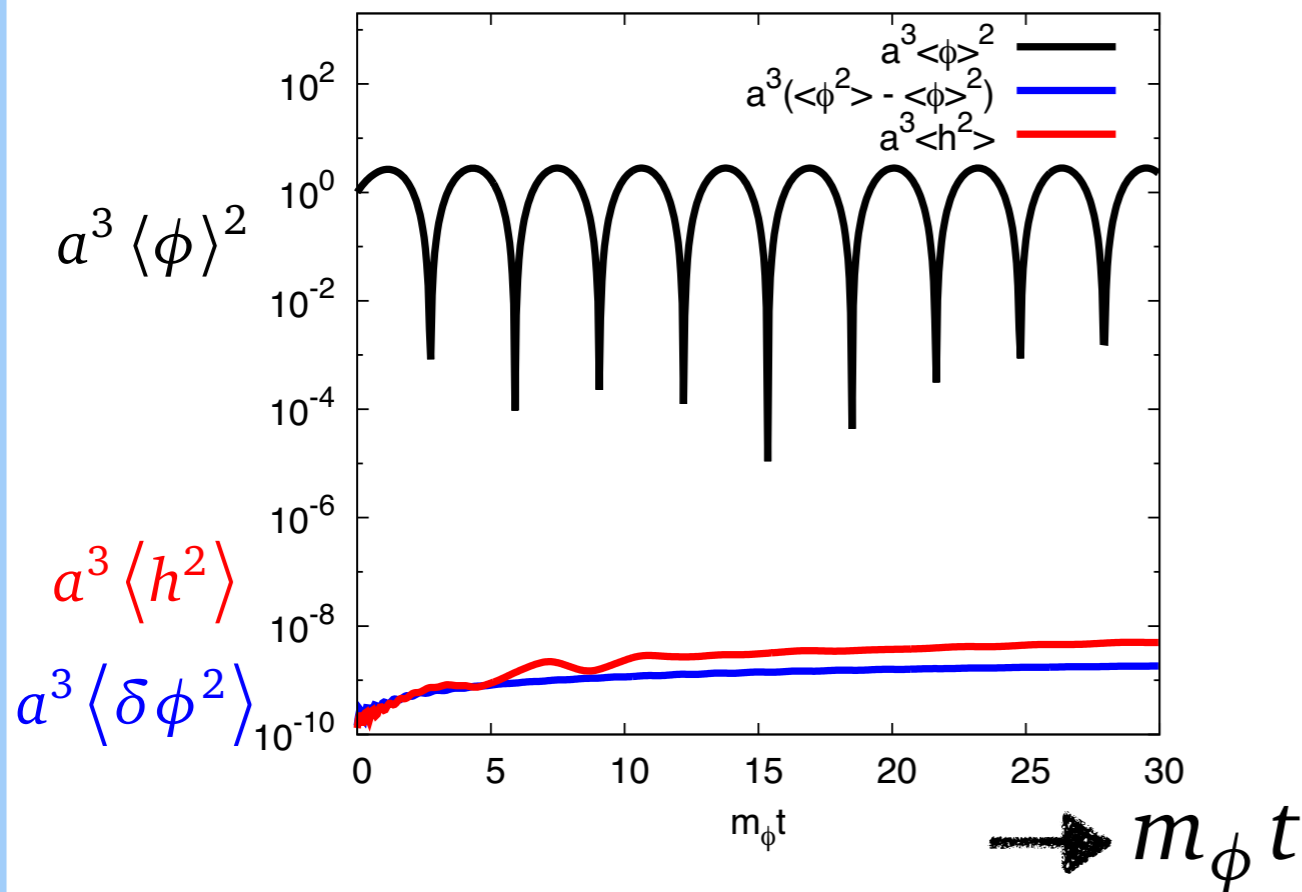
Numerical Simulation

[Ema, KM, Nakayama, [1602.00483](#)]

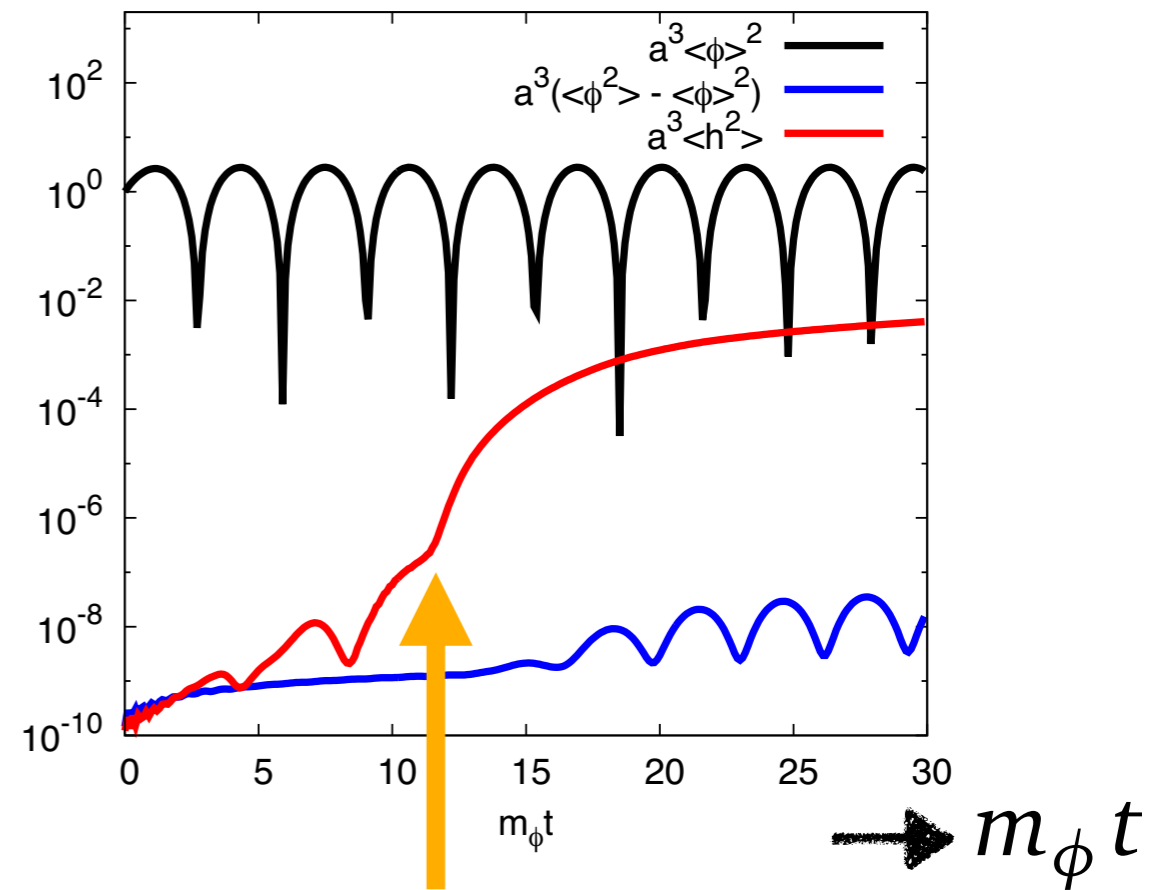
■ Vacuum decay via Tachyonic Resonance: $-\mathcal{L}_{\text{int}}(\phi, h) = \frac{1}{2} \xi R h^2$

- To check $\xi \lesssim 10 \times \left[\frac{1}{\mu_{\text{crv}}} \right]^2 \left[\frac{\sqrt{2} M_{\text{pl}}}{\Phi_{\text{ini}}} \right]^2$, we performed a classical lattice simulation.

- Stable: $\xi = 10$



- Unstable: $\xi = 20$



Vacuum Decay!

Gravitational Wave

■ GWs are produced via second order effects

[Saito, Yokoyama; Bugaev, Klimai]

- Perturbed metric:

$$ds^2 = -a^2(\eta) \left[e^{2\Phi} d\eta^2 - e^{-2\Psi} \left(\delta_{ij} + \frac{1}{2} h_{ij} \right) dx^i dx^j \right]$$

Scalar perturbs: $\Psi = \Phi$ (neglect anisotropic stress)

Tensor perturb

- Large scalar perturbations act as a source term in equation of motion for GWs.

$$h''_{ij} + 2\mathcal{H} h'_{ij} - \nabla^2 h_{ij} = -4 \hat{\mathcal{T}}_{ij;kl} S_{kl}$$

projection to transverse-traceless part

$$\text{Source term: } S_{ij} \equiv 4\Psi \partial_i \partial_j \Psi + 2\partial_i \Psi \partial_j \Psi - \frac{4}{3(1+w)} \partial_i \left(\frac{\Psi'}{\mathcal{H}} + \Psi \right) \partial_j \left(\frac{\Psi'}{\mathcal{H}} + \Psi \right)$$

- Abundance of GWs is roughly given by...

$$\Omega_{\text{GW}}(k) \sim 3 \times 10^{-8} \left(\frac{\mathcal{P}_\zeta(k)}{0.01} \right)^2$$