
Vector and Axial-vector Resonances in composite models of the Higgs boson

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Outline

- *A brief review of Composite Higgs Models*
- *Model implementation of Spin-1 resonances in $SU(4)/Sp(4)$*
- *Phenomenology at LHC and 100 TeV Collider*
- *Conclusion and future outlooks*

Composite Higgs Model

What is Composite Higgs? > PNGB from strong dynamics

Original one: $SU(5)/SO(5)$ gives 14 pNGBs; Higgs mass protected by “shift symmetry”;
EWSB triggered by vacuum misalignment.

[Georgi, Kaplan 1984]

Global symmetry broken at TeV scale with $f \gg v$, EWPT vs “Naturalness”

Top quark mass can be generated via partial compositeness

SM fermion couples to strong sector: $\lambda \psi_{SM} \mathcal{O}_{CFT}$

[Contino, Nomura, Pomarol 2003; Agashe, Contino, Pomarol, 2004]

Minimal CHM based on fundamental dynamics requires $SU(4)/Sp(4)$

Give rise to one Higgs doublet plus one singlet

Fundamental Theory

Underlying dynamics is $Sp(2N_c)_{TC}$ gauge theory with 4 Weyl techni-quarks:

[Galloway, Evans, Luty, Tacchi, 2010 ; Cacciapaglia, Sannino, 2014]

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}^a F^{a\mu\nu} + \bar{Q}_j (i\sigma^\mu D_\mu) Q_j - M^{ij} Q_i Q_j + h.c.$$

Minimal choice :

$$M_Q = \begin{pmatrix} \mu_L i\sigma_2 & 0 \\ 0 & \mu_R i\sigma_2 \end{pmatrix}, \quad \text{techni-quark mass}$$

$Sp(2) \sim SU(2)$

Bound states will form in the IR:

$$(\pi^a, \sigma) : \langle QQ \rangle = \mathbf{6}_{SU(4)} \rightarrow \mathbf{5}_{Sp(4)} \oplus \mathbf{1}_{Sp(4)} \quad \text{composite scalars}$$

$$(\rho_\mu^i, a_\mu^k) : \langle \bar{Q} \sigma^\mu Q \rangle = \mathbf{15}_{SU(4)} \rightarrow \mathbf{10}_{Sp(4)} \oplus \mathbf{5}_{Sp(4)} \quad \text{composite vectors}$$

For $N_c \geq 2$, add 6 techni-quarks $\chi_j \Rightarrow$ *coloured pNGBs* plus *top partners*.

[Barnard, Gherghetta, Ray, 2014; Ferretti, 2014; Cacciapaglia, Cai, Deandra, Flacke, Lee, Parolini, 2015]

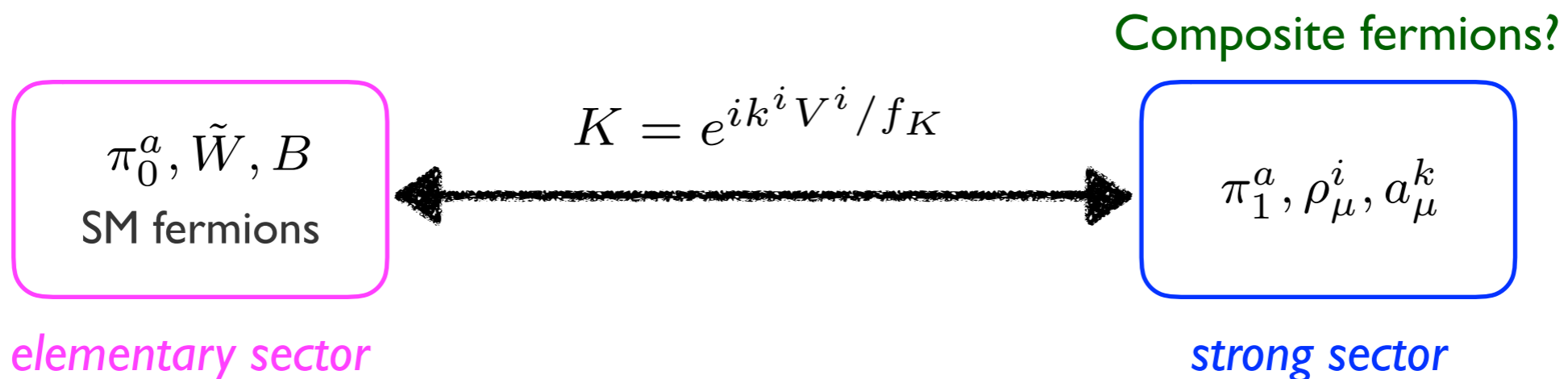
[Belyaev, Cacciapaglia, Cai, Flacke, Parolini, Serodio, 2015]

How to implement vector resonances in EFT ?

Hidden Symmetry

Using Hidden symmetry techniques, one can extend the global symmetry to be:

$$SU(4)_0 \times SU(4)_1 \rightarrow Sp(4)$$



π_0^a, π_1^a, k^i : 20 Nambu-Goldstone bosons, 15 eaten by V^i, A^a

3 eaten by W, Z , two physical scalars remain: h, η .

Model Setup

We adopt the **CCWZ** formalism and define *2 sets of pions* for enhanced global symmetry:

[Coleman, Wess, Zumino, 1969; Callan, Coleman, Wess, Zumino, 1969; Bando, Kugo, Yamawaki, 1988]

$$U_0 = \exp \left[\frac{i\sqrt{2}}{f_0} \sum_{a=1}^5 (\pi_0^a Y^a) \right]$$
$$U_1 = \exp \left[\frac{i\sqrt{2}}{f_1} \sum_{a=1}^5 (\pi_1^a Y^a) \right]$$

Project Maurer-Cartan forms into:

$$\text{broken direction} \Rightarrow p_{\mu i} = 2 \sum_a \text{Tr}(Y_a U_i^\dagger D_\mu U_i) Y_a$$
$$\text{unbroken direction} \Rightarrow v_{\mu i} = 2 \sum_a \text{Tr}(V_a U_i^\dagger D_\mu U_i) V_a$$

Thus $v_{\mu,i}$ transform like gauge bosons and $p_{\mu,i}$ transform homogeneously.

Effective Lagrangian

$$\mathcal{L} = -\frac{1}{2g^2} \text{Tr} W_{\mu\nu} W^{\mu\nu} - \frac{1}{2g'^2} \text{Tr} B_{\mu\nu} B^{\mu\nu} - \frac{1}{2\tilde{g}^2} \text{Tr} \mathcal{F}_{\mu\nu} \mathcal{F}^{\mu\nu}$$

$$+ \frac{1}{2} \kappa_{G_0}(\sigma) f_0^2 \text{Tr} p_{0\mu} p_0^\mu + \frac{1}{2} \kappa_{G_1}(\sigma) f_1^2 \text{Tr} p_{1\mu} p_1^\mu + r[\sigma] f_1^2 \text{Tr} p_{0\mu} K p_1^\mu K^\dagger$$

$$+ \frac{1}{2} \kappa_K(\sigma) f_K^2 \text{Tr} \mathcal{D}^\mu K \mathcal{D}_\mu K^\dagger + \frac{1}{2} \partial_\mu \sigma \partial^\mu \sigma - \mathcal{V}(\sigma) \quad \text{pion kinetic terms}$$

normal CCWZ terms



Vector partial compositeness

Axial partial compositeness

composite vectors: $\mathcal{F}_\mu = \sum_{a=1}^{10} \mathcal{V}_\mu^a V_a + \sum_{a=1}^5 \mathcal{A}_\mu^a Y_a.$

$$K = \exp [ik^i V^i / f_K] , \quad D_\mu K = \partial_\mu K - iv_{0\mu} K + iK v_{1\mu}$$

The K field is to break $Sp(4)_0 \times Sp(4)_1$ into the diagonal final $Sp(4)$.

Physical Pions

Due to the r term, we need to rotate *2 sets of pions* into orthogonal unitary basis,

$$\begin{aligned}\pi_0^a &= \pi_P^a \frac{1}{\sqrt{1 - r^2 f_1^2 / f_0^2}} \\ \pi_1^a &= \pi_U^a - \pi_P^a \frac{r f_1 / f_0}{\sqrt{1 - r^2 f_1^2 / f_0^2}}\end{aligned}$$

π_P is associated with physical scalars and π_U is NG boson eaten by x_0^μ and \tilde{x}_0^μ .

Unitary basis \Rightarrow no bilinear mixing in terms of $\partial_\mu h x_0^\mu$ and $\partial_\mu \eta \tilde{x}_0^\mu$

Since $v^2 = (f_0^2 - r^2 f_1^2) \sin^2 \theta$, with EWSB, there is no divergence in the pion rotation.

Model Spectrum

One charged state of exact mass M_V does not mix with \tilde{W} and \tilde{B} ; Neutral Sector gives a massless photon.

$$\begin{aligned}
 M_{W^\pm}^2 &= \frac{1}{4}g^2v^2 + \mathcal{O}\left(\frac{g}{\tilde{g}}\right)^4, & M_{S^\pm} &= M_V^2 & M_Z^2 &= \frac{1}{4}(g^2 + g'^2)v^2 + \mathcal{O}\left(\frac{g}{\tilde{g}}\right)^4 \\
 M_{A^\pm}^2 &= M_A^2 \left(1 + \frac{r^2 \left(\frac{g}{\tilde{g}}\right)^2 s_\theta^2}{2}\right) + \mathcal{O}\left(\frac{g}{\tilde{g}}\right)^4 & M_{A^0}^2 &= M_A^2 \left(1 + \frac{r^2 \left(\frac{g^2 + g'^2}{\tilde{g}^2}\right) s_\theta^2}{2}\right) + \mathcal{O}\left(\frac{g}{\tilde{g}}\right)^4 \\
 M_{V^\pm} &= \frac{1}{4}M_V^2 \left(\frac{g^2(\cos(2\theta) + 3)}{\tilde{g}^2} + 4\right) + \mathcal{O}\left(\frac{g}{\tilde{g}}\right)^4 & M_{V^0, S^0} &= M_V^2 \left[1 + \frac{g^2 + g'^2}{4\tilde{g}^2} (1 + c_\theta^2 \pm \mathcal{O}(1))\right] + \mathcal{O}\left(\frac{g}{\tilde{g}}\right)^4
 \end{aligned}$$

There are additional no mixing states $\tilde{s}_\mu^{\pm,0}$, \tilde{v}_μ^0 , x_μ^0 and \tilde{x}_μ^0 , with masses:

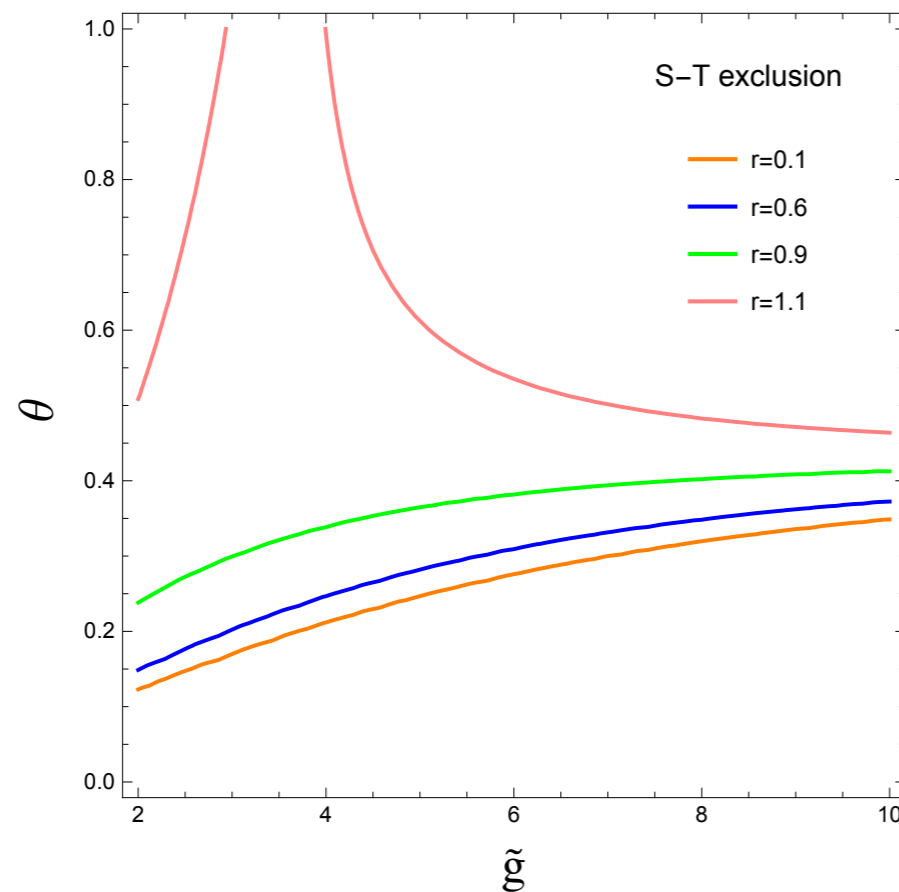
$$M_{\tilde{s}} = M_{\tilde{v}^0} = M_V \quad \text{and} \quad M_{x^0} = M_{\tilde{x}^0} = M_A.$$

Typical HVV couplings:

$$c_{hW^+W^-} \simeq \frac{2M_W^2}{v} c_\theta = c_{hW^+W^-}^{\text{SM}} c_\theta, \quad c_{hZZ} \simeq \frac{2M_Z^2}{v} c_\theta = c_{hZZ}^{\text{SM}} c_\theta$$

Electroweak Precision Tests

The S-T is exploited to exclude the unfavored region in the parameter space.



$$S = -\frac{4s_W^2}{\alpha_{EW}} \frac{g^2 (r^2 - 1) s_\theta^2}{2\tilde{g}^2 + g^2 [2 + (r^2 - 1)s_\theta^2]} + \frac{1}{6\pi} s_\theta^2 \log\left(\frac{\Lambda}{m_h}\right)$$

$$T = -\frac{3}{8\pi \cos^2 \theta_W} s_\theta^2 \ln \frac{\Lambda}{m_h}$$

$r \simeq 1$: a partial cancellation occurs in S parameter, in certain range of \tilde{g} , there is no bound for the θ angle.

$r < 1$: EWPT typically requires $\theta < 0.2$.

stronger than Higgs coupling constraint !

Fermion Currents

| Field | Fermion currents | P | C | G | GP |
|--|--|---|---|---|----|
| Massive spin-1 \mathcal{V}_μ (unbroken generators) | | | | | |
| v^+ | $\bar{D}\gamma^\mu U$ | | | | |
| v^0 | $\frac{1}{\sqrt{2}} (\bar{U}\gamma^\mu U - \bar{D}\gamma^\mu D)$ | - | - | - | + |
| v^- | $\bar{U}\gamma^\mu D$ | | | | |
| \tilde{v}^0 | $\sqrt{2} \cos \theta \Im (U^T C \gamma^\mu D) + \frac{1}{\sqrt{2}} \sin \theta (\bar{U}\gamma^\mu U + \bar{D}\gamma^\mu D)$ | - | - | + | - |
| s^+ | $\cos \theta (\bar{D}\gamma^\mu \gamma^5 U) + \frac{i}{2} \sin \theta (U^T C \gamma^\mu \gamma^5 U - \bar{D}\gamma^\mu C \gamma^5 \bar{D}^T)$ | | | | |
| s^0 | $-\frac{1}{\sqrt{2}} \cos \theta (\bar{U}\gamma^\mu \gamma^5 U - \bar{D}\gamma^\mu \gamma^5 D) - \sqrt{2} \sin \theta \Im (U^T C \gamma^\mu \gamma^5 D)$ | + | + | + | + |
| s^- | $\cos \theta (\bar{U}\gamma^\mu \gamma^5 D) + \frac{i}{2} \sin \theta (\bar{U}\gamma^\mu C \gamma^5 \bar{U}^T - D^T C \gamma^\mu \gamma^5 D)$ | | | | |
| \tilde{s}^+ | $\frac{i}{2} (U^T C \gamma^\mu \gamma^5 U + \bar{D}\gamma^\mu C \gamma^5 \bar{D}^T)$ | | | | |
| \tilde{s}^0 | $\sqrt{2} \Re (U^T C \gamma^\mu \gamma^5 D)$ | + | - | - | - |
| \tilde{s}^- | $\frac{i}{2} (\bar{U}\gamma^\mu C \gamma^5 \bar{U}^T + D^T C \gamma^\mu \gamma^5 D)$ | | | | |
| Massive spin-1 \mathcal{A}_μ (broken generators) | | | | | |
| a^+ | $\frac{i}{2} \cos \theta (U^T C \gamma^\mu \gamma^5 U - \bar{D}\gamma^\mu C \gamma^5 \bar{D}^T) - \sin \theta (\bar{D}\gamma^\mu \gamma^5 U)$ | | | | |
| a^0 | $-\sqrt{2} \cos \theta \Im (U^T C \gamma^\mu \gamma^5 D) + \frac{1}{\sqrt{2}} \sin \theta (\bar{U}\gamma^\mu \gamma^5 U - \bar{D}\gamma^\mu \gamma^5 D)$ | + | + | + | + |
| a^- | $\frac{i}{2} \cos \theta (\bar{U}\gamma^\mu C \gamma^5 \bar{U}^T - D^T C \gamma^\mu \gamma^5 D) - \sin \theta (\bar{U}\gamma^\mu \gamma^5 D)$ | | | | |
| x^0 | $\sqrt{2} \Re (U^T C \gamma^\mu D)$ | - | + | - | + |
| \tilde{x}^0 | $\frac{1}{\sqrt{2}} \cos \theta (\bar{U}\gamma^\mu U + \bar{D}\gamma^\mu D) - \sqrt{2} \sin \theta \Im (U^T C \gamma^\mu D)$ | - | - | + | - |

P-Parity : $U \xrightarrow{P} i\gamma^0 U, \quad D \xrightarrow{P} i\gamma^0 D$

C-Parity : $U \xrightarrow{C} -i\gamma^2 U^*, \quad D \xrightarrow{C} -i\gamma^2 D^*$

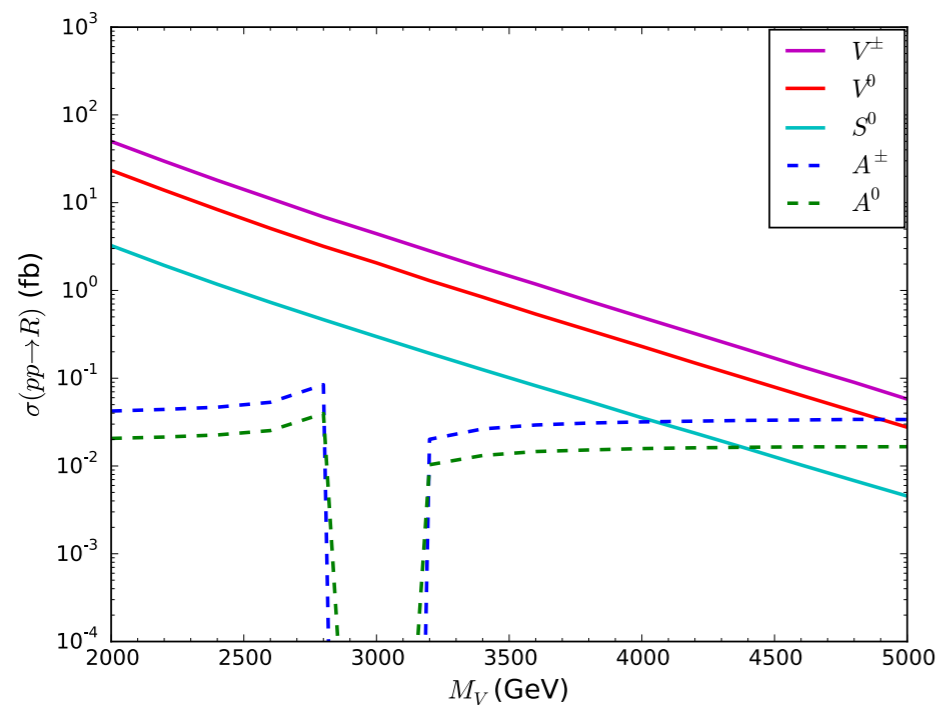
G-Parity : $U \xrightarrow{G} -\gamma^2 D^*, \quad D \xrightarrow{G} \gamma^2 U^*$

Under the parity operation: a vector fermion-current has $CP = +$; and a pseudo-vector fermion-current has $CP = -$.

The GP is a good symmetry and being selection rule for decays. Only the tilded fields and η are odd under this parity.

Cross Section @ LHC Run II

Drell-Yan production



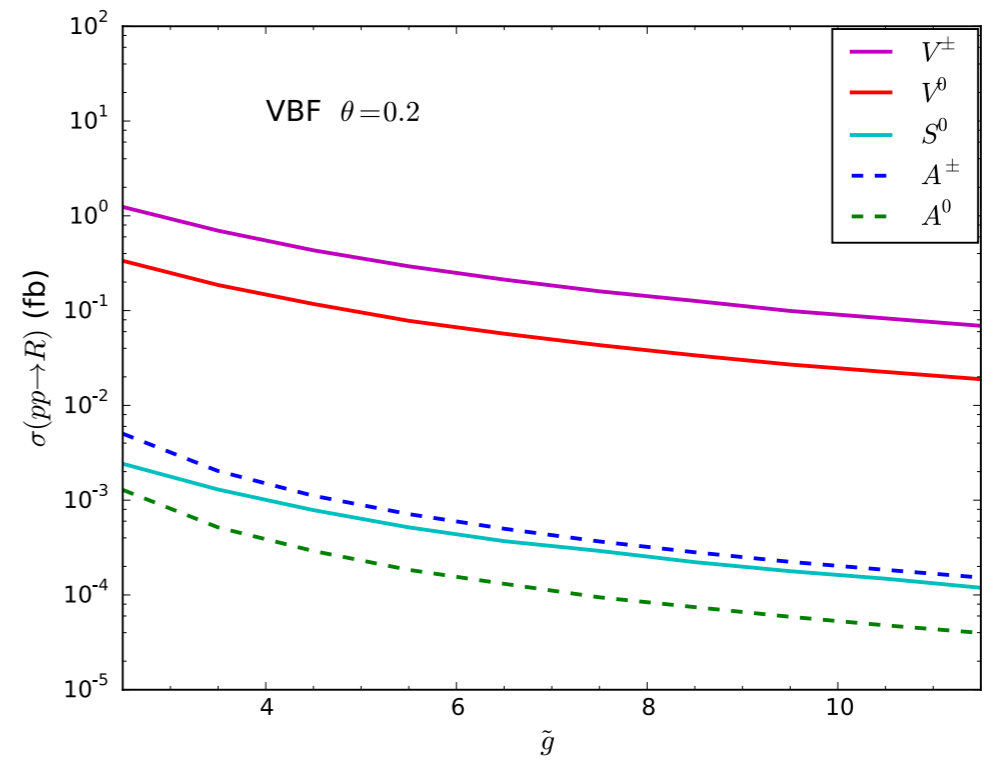
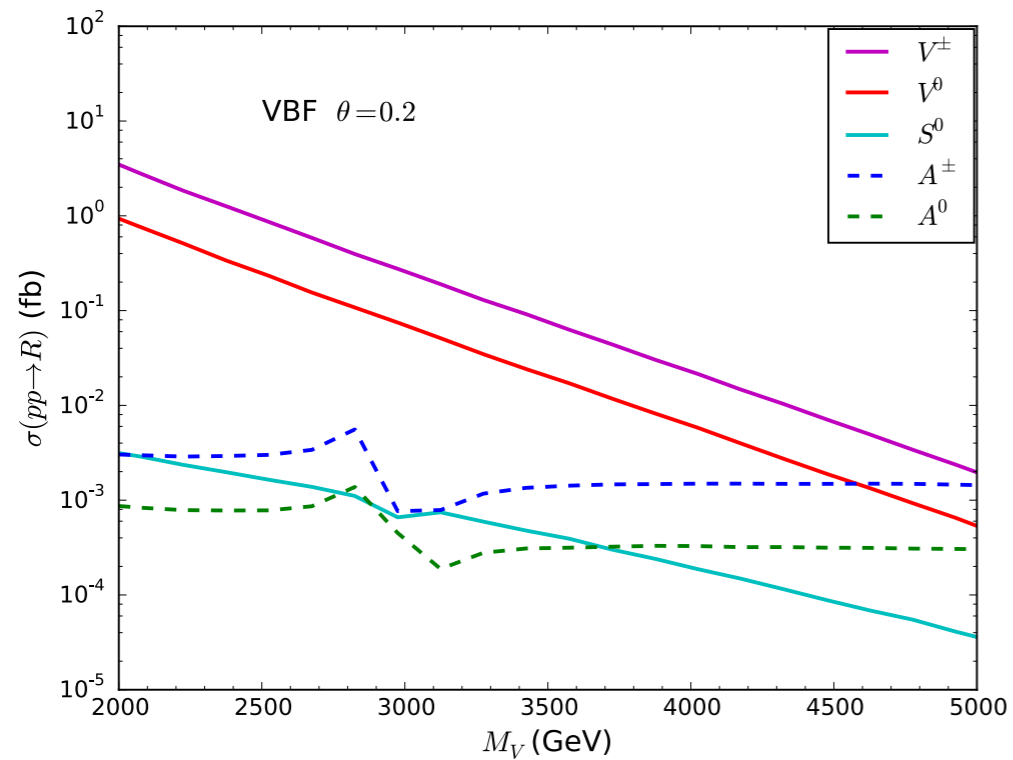
The benchmark point: $M_A = 3$ TeV, $\tilde{g} = 3.0$, $r = 0.6$ and $\theta = 0.2$.

No S^+ state can be directly produced since it is purely composite.

For $M_V = M_A$, cross sections of axial resonances turn out to be zero.

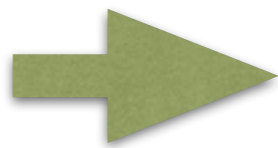
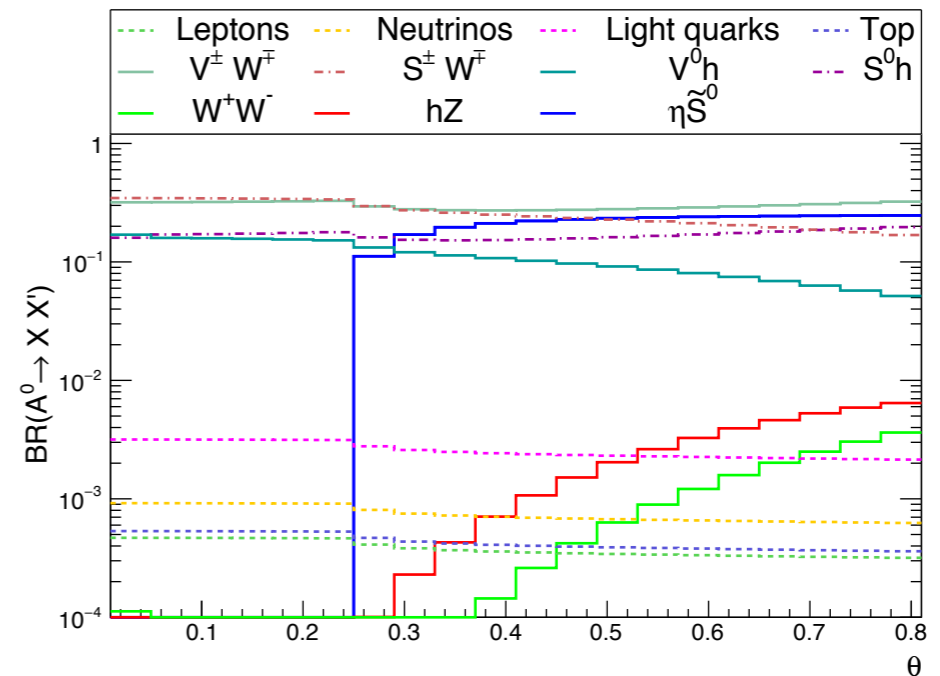
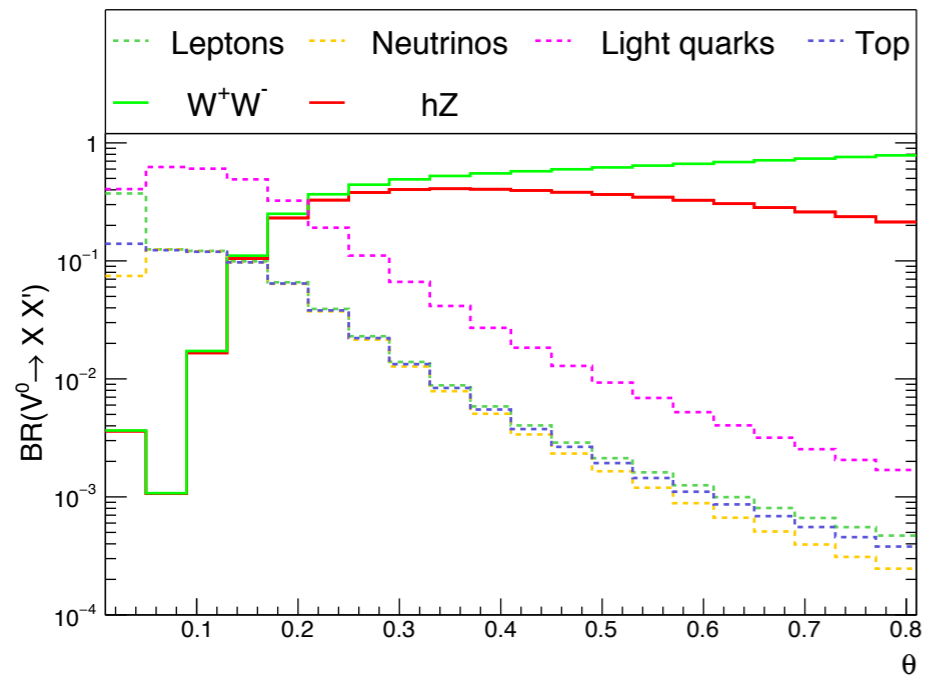
One Feynrule Model is implemented for this $SU(4)/Sp(4)$ model, available at <http://hepmdb.soton.ac.uk/hepmdb:0416.0200>

we consider normal VBF topology + t -channel radiation diagrams as a gauge invariant set.



In LHC Run-II, VBF is subdominant and the cross section decreases with \tilde{g} .

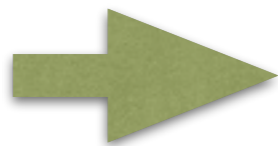
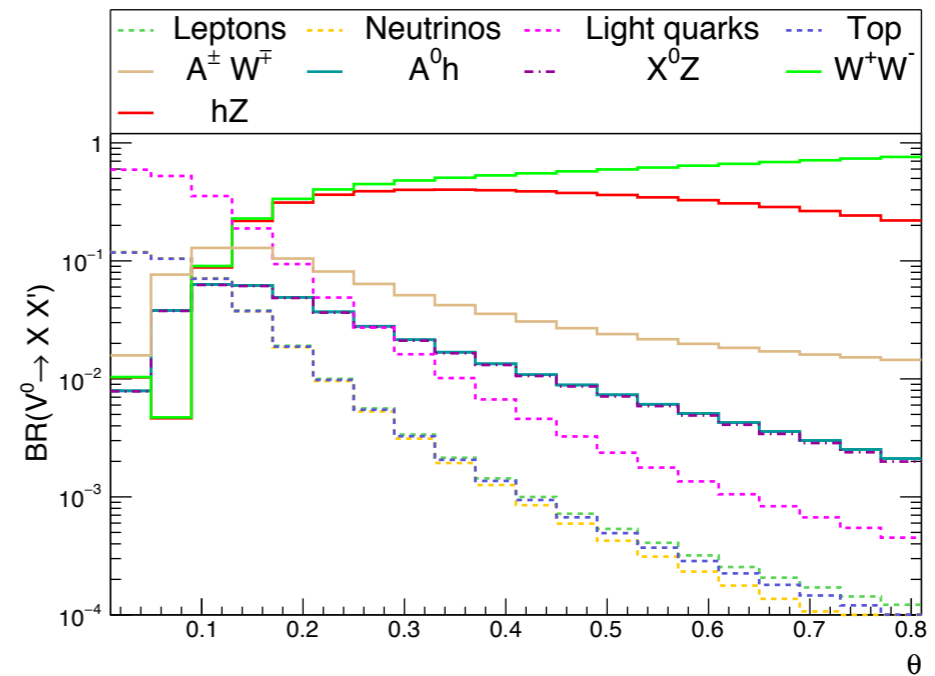
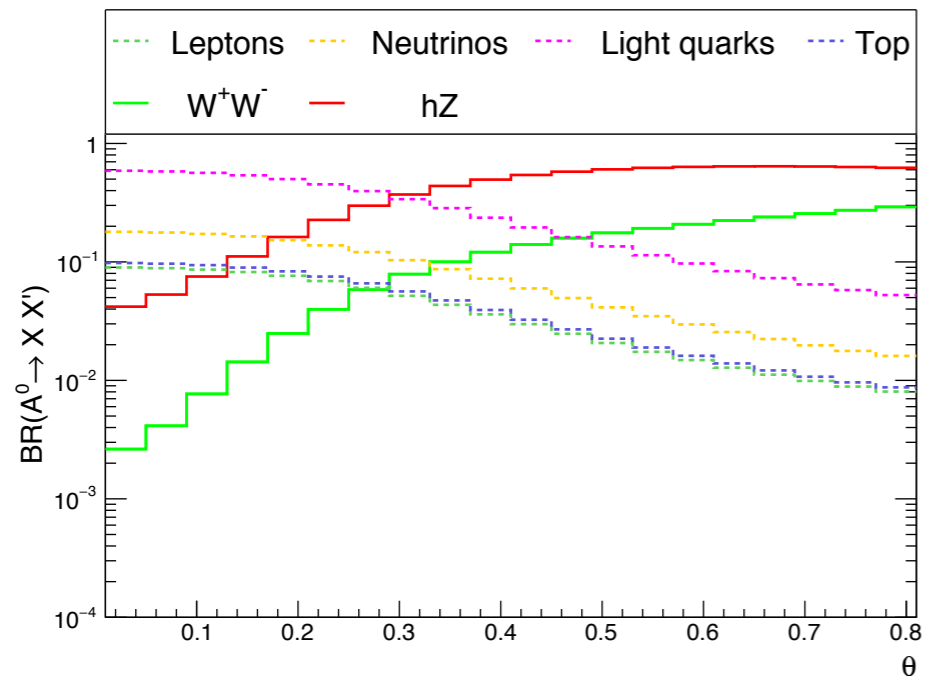
$M_V < M_A$ Scenario



V^0 mainly decays into SM fermions and dibosons and Higgs.

Cascade decay: $A^0 \rightarrow \eta \tilde{S}^0 \rightarrow 2\eta + Z$, $\eta \rightarrow t\bar{t}$. **multi-tops events.**

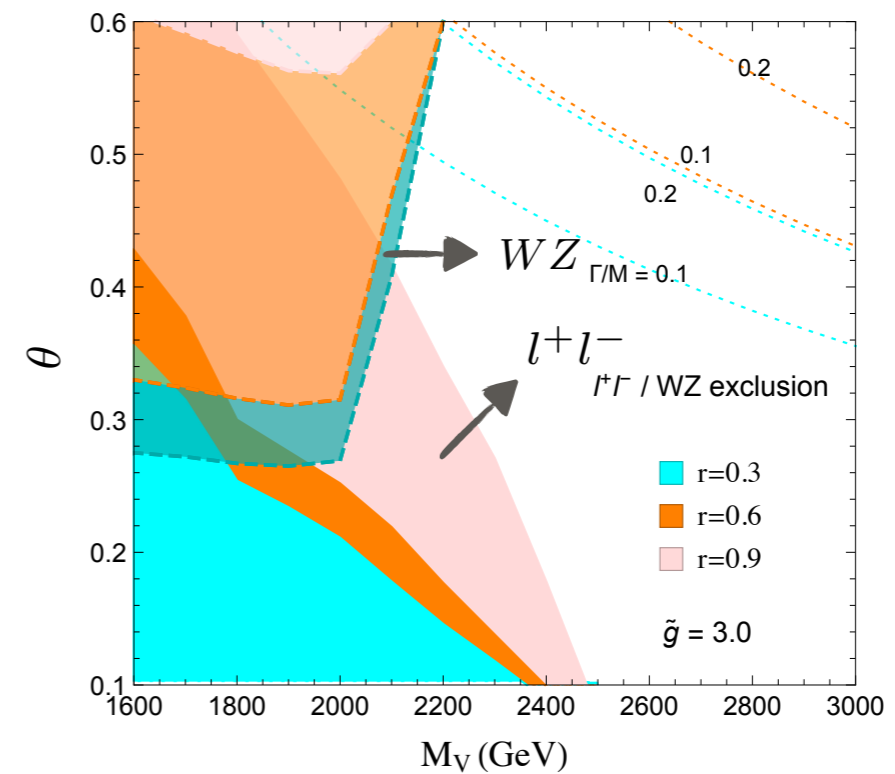
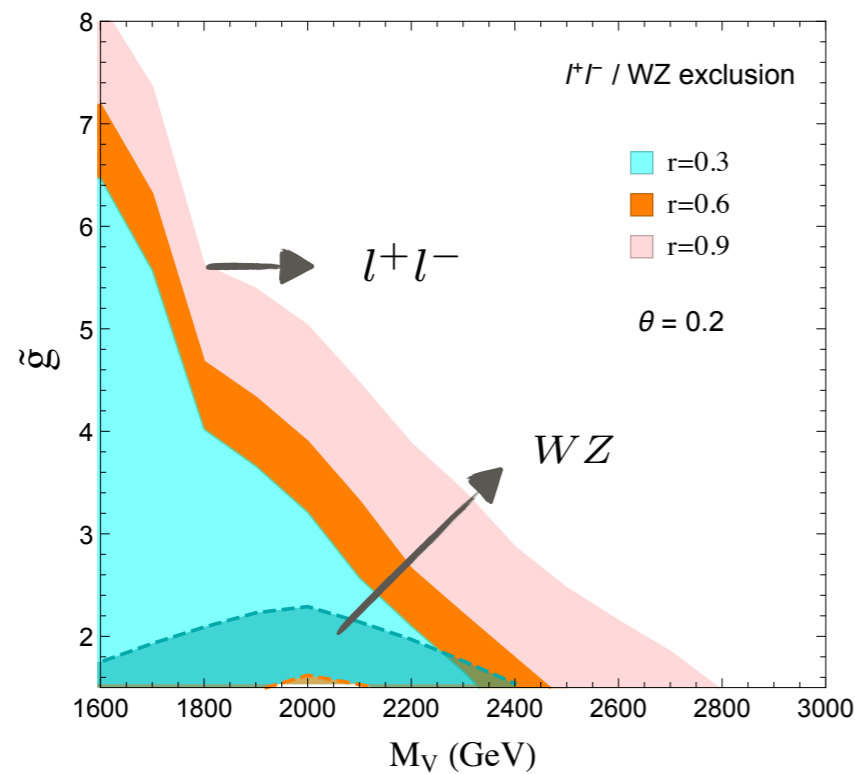
$M_A < M_V$ Scenario



A^0 mainly decays into SM fermions and dibosons and Higgs.

Direct Bounds - LHC Run II

Recasted from ATLAS measurement, with dilepton bound in solid line and WZ bound in dashed line.



The l^+l^- and WZ are complementary to each other.

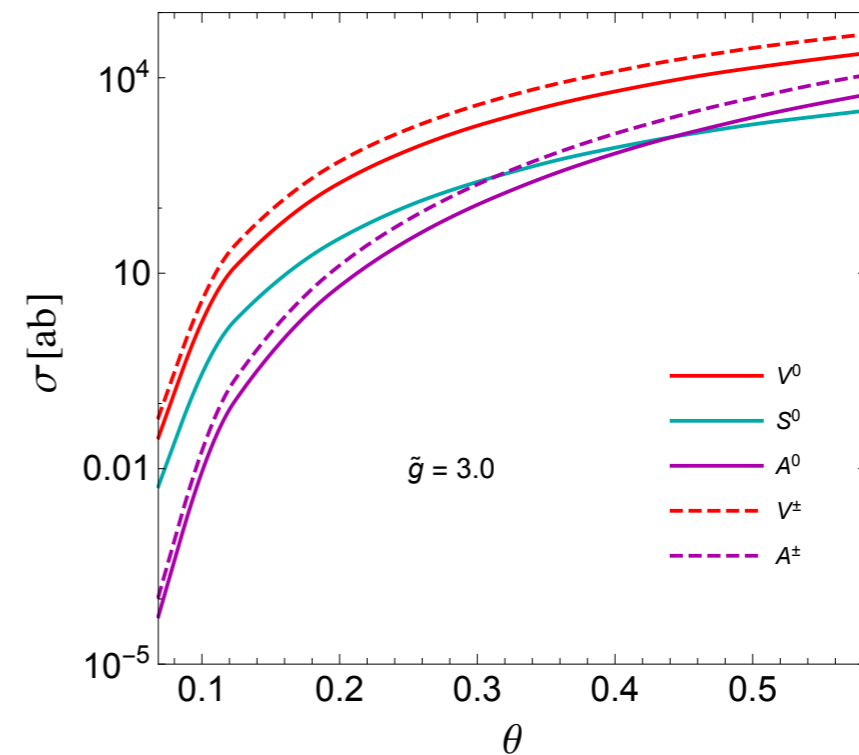
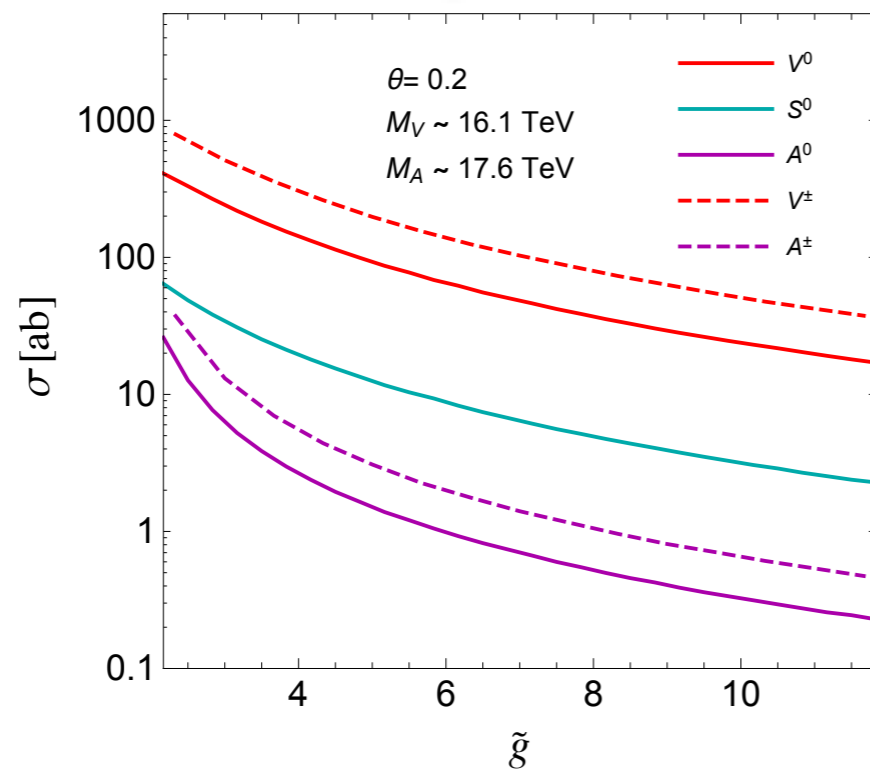
The dilepton exclusion imposes quite strong bound $\Rightarrow M_V \gtrsim 2.5$ TeV !

Future 100 TeV Collider

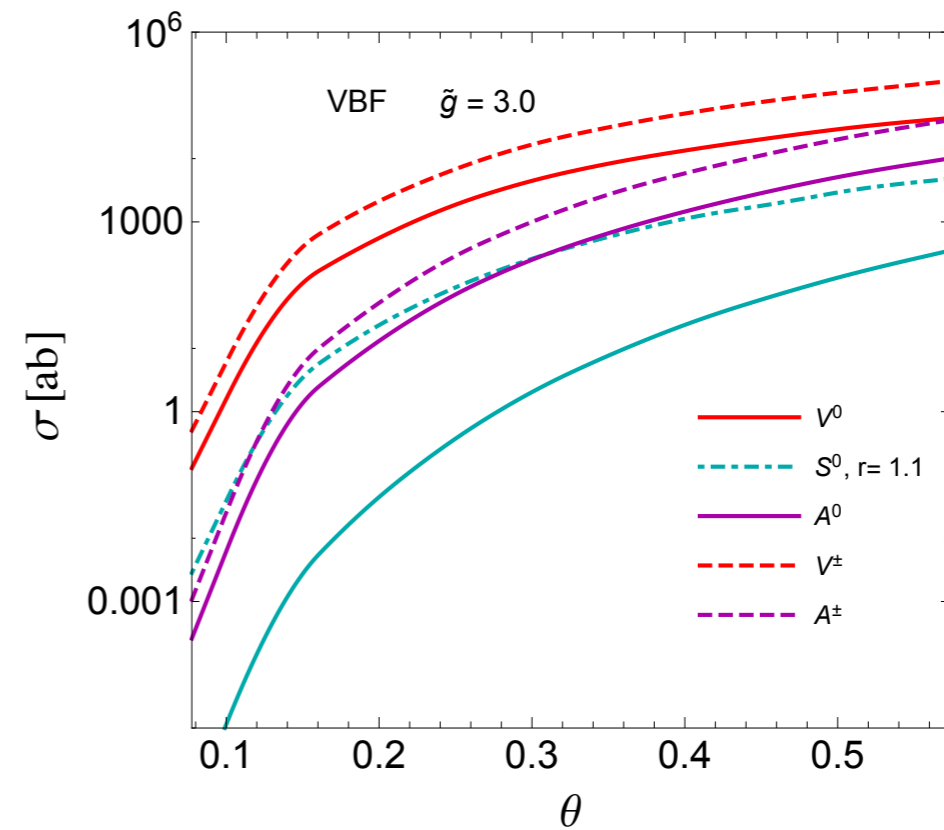
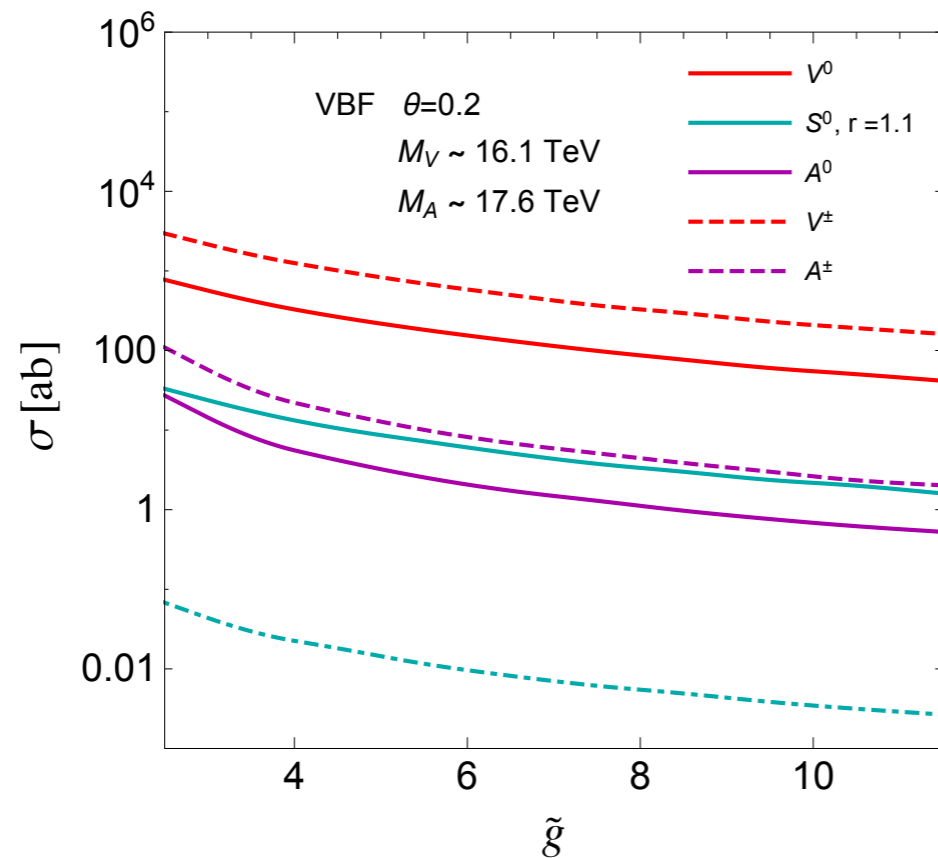
Using Lattice benchmark point: $M_V = 3.2/\sin\theta$ TeV, $M_A = 3.5/\sin\theta$ TeV.
[Arthur, Drach, Hansen, Pica, Sannino 2016]

$\sigma_R \lesssim \mathcal{O}(1)$ fb for $\theta \sim 0.2$, with an integrated luminosity $3 - 30 ab^{-1}$ per year.
[Richter, 2014; Rizzo, 2015]

Drell-Yan production



At 100 TeV, Vector Boson Fusion plays an important role due to the collinear enhancement, with $\sigma_{VBF} > \sigma_{Drell-Yan}$ for $V^{\pm,0}$ and $A^{\pm,0}$ resonances.



Conclusion and Outlook

- Spin-1 resonances are implemented in a $SU(4)/Sp(4)$ CHM using Hidden symmetry techniques; Composite fermions not included yet.
- S parameter can be well protected due to a partial cancellation.
- The CP parities are illustrated in terms of fermion currents from a fundamental gauge theory.
- At LHC Run-II, the Drell-Yan process imposes a stringent bound. However at 100 TeV collider, some VBF channels become dominant.
- Searching for signatures related to such resonances is possible to unveil EWSB mechanism.

Back up Slides

UV theory and IR Bound States

| | Sp(2N _c) | SU(3) _c | SU(2) _L | U(1) _Y | SU(4) | SU(6) | U(1) |
|----------------|----------------------|--------------------|--------------------|-------------------|----------|----------|--------------------------------------|
| Q | □ | 1 | 2 | 1 | 4 | 0 | -3(N _c - 1)q _χ |
| Q [†] | □ | 1 | 1 | 1/2 -1/2 | | | |
| χ | □ □ | 3 | 1 | x | 1 | 6 | q _χ |
| χ [†] | □ □ | 3̄ | 1 | -x | | | |

| | spin | SU(4)×SU(6) | Sp(4)×SO(6) | names |
|-------------------|------|-----------------|----------------------------------|---|
| QQ | 0 | (6, 1) | (1, 1) (5, 1) | σ π |
| χχ | 0 | (1, 21) | (1, 1) (1, 20) | σ _c π _c |
| χQQ | 1/2 | (6, 6) | (1, 6) (5, 6) | ψ ₁ ¹ ψ ₁ ⁵ |
| χQ [†] Q | 1/2 | (6, 6) | (1, 6) (5, 6) | ψ ₂ ¹ ψ ₂ ⁵ |
| Qχ [†] Q | 1/2 | (1, 6̄) | (1, 6) | ψ ₃ |
| Qχ [†] Q | 1/2 | (15, 6̄) | (5, 6) (10, 6) | ψ ₄ ⁵ ψ ₄ ¹⁰ |
| Qσ ^μ Q | 1 | (15, 1) | (5, 1) (10, 1) | a ρ |
| χσ ^μ χ | 1 | (1, 35) | (1, 20) (1, 15) | a _c ρ _c |

$$\frac{1}{\Lambda^2} \bar{t}_L \chi Q Q$$

Top partial compositeness