

# Redshift Distortion as a probe for cosmology: improving theoretical modeling

Yipeng Jing (景益鹏)

Center for Astronomy and Astrophysics  
Shanghai Jiao Tong University

**Pengjie Zhang** (张鹏杰) ; **Yi Zheng** (郑逸)

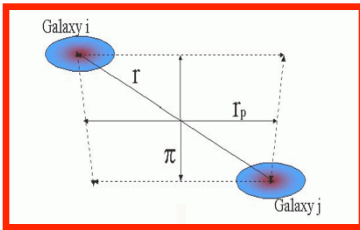
Y. Zheng, P. Zhang, Y. Jing, W. Lin, and J. Pan, Phys. Rev. D 88, 103510 (2013), 1308.0886

P. Zhang, Y. Zheng, Y. Jing, (2014, **paperSI**), PRD

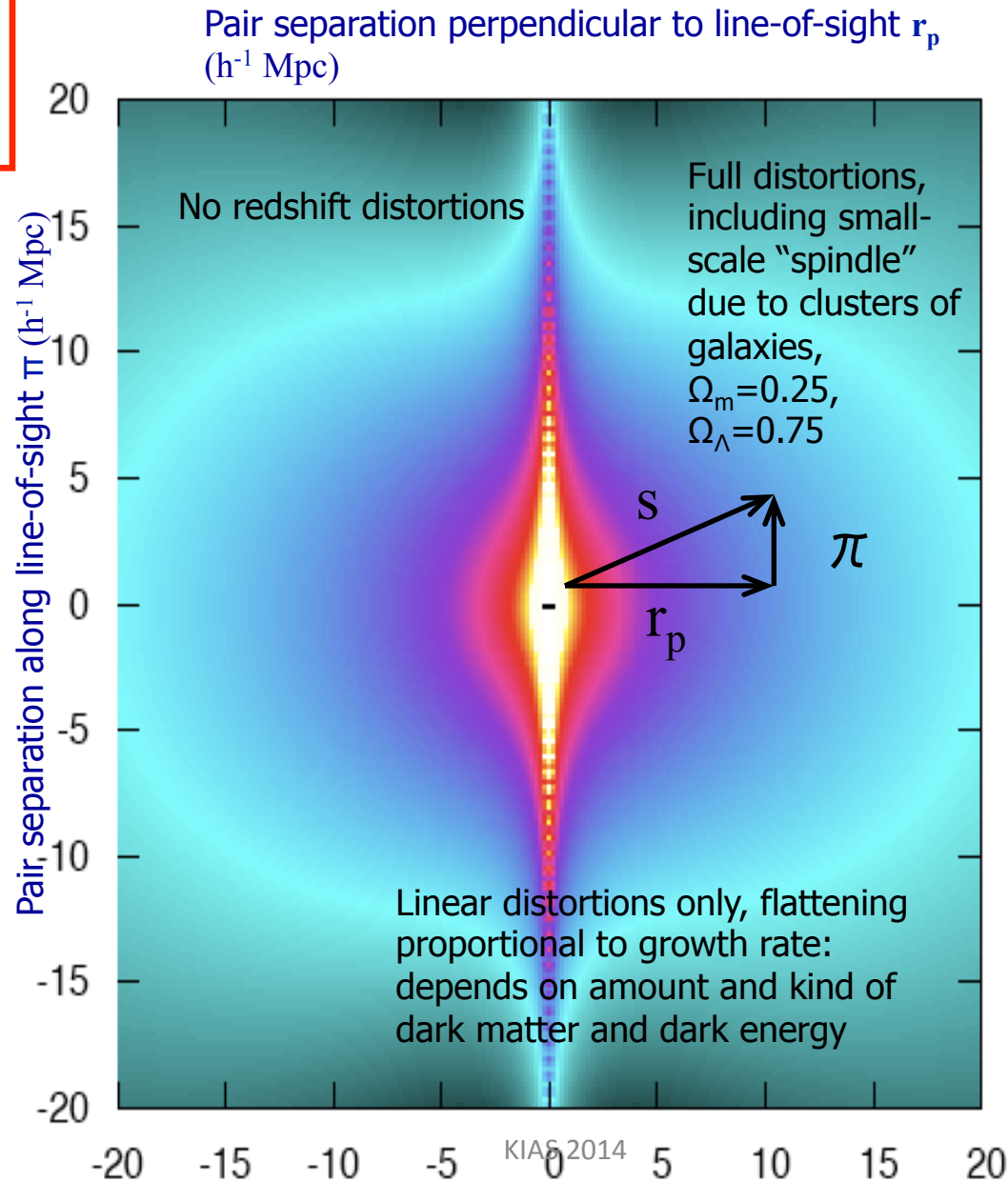
Y. Zheng, P. Zhang, Y. Jing, (2014, **paperSII**), PRD

Y. Zheng, P. Zhang, Y. Jing, (2014, **paperB**), PRD, submitted

# Redshift-space galaxy-galaxy correlation function $\xi(r_p, \pi)$



Line of sight to observer



But we need to look at both sides of the story...

$$R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R = -\frac{8\pi G}{c^2} T_{\mu\nu} + \Lambda g_{\mu\nu}$$

Modify gravity theory [e.g.  $R \rightarrow f(R)$  ]



Add dark energy



“...the Force be with you”

# Probing Gravity at Cosmological Scales by Measurements which Test the Relationship between Gravitational Lensing and Matter Overdensity

Pengjie Zhang,<sup>1,2,\*</sup> Michele Liguori,<sup>3</sup> Rachel Bean,<sup>4</sup> and Scott Dodelson<sup>5,6</sup>

<sup>1</sup>Shanghai Astronomical Observatory, Chinese Academy of Science, 80 Nandan Road, Shanghai, China, 200030

<sup>2</sup>Joint Institute for Galaxy and Cosmology (JOINGC) of SHAO and USTC, Shanghai, China

<sup>3</sup>Department of Applied Mathematics and Theoretical Physics, Centre for Mathematical Sciences, University of Cambridge, Wilberforce Road, Cambridge, CB3 0WA, United Kingdom

<sup>4</sup>Department of Astronomy, Cornell University, Ithaca, New York 14853, USA

<sup>5</sup>Center for Particle Astrophysics, Fermi National Accelerator Laboratory, Batavia, Illinois 60510-0500, USA

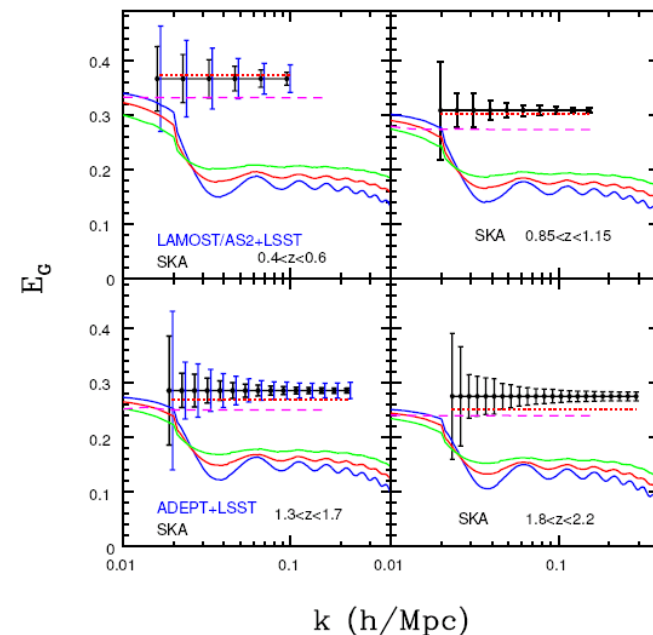
<sup>6</sup>Department of Astronomy & Astrophysics, The University of Chicago, Chicago, Illinois 60637-1433, USA

(Received 15 April 2007; revised manuscript received 31 May 2007; published 4 October 2007)

The standard cosmology is based on general relativity (GR) and includes dark matter and dark energy and predicts a fixed relationship between the gravitational potentials responsible for gravitational lensing and the matter overdensity. Alternative theories of gravity often make different predictions. We propose a set of measurements which can test this relationship, thereby distinguishing between dark energy or matter models and models in which gravity differs from GR. Planned surveys will be able to measure  $E_G$ , an observational quantity whose expectation value is equal to the ratio of the Laplacian of the Newtonian potentials to the peculiar velocity divergence, to percent accuracy. This will easily separate alternatives such as the cold dark matter model with a cosmological constant, Dvali-Gabadadze-Porrati, TeVeS  $f(R)$  gravity.

4个引力模型: GR,  
 $f(R)$ , DGP,  
TeVeS

张鹏杰等提出在宇宙学  
尺度上检验广义相对论与其  
他引力论的 $E_G$ 方法



# Designing a space-based galaxy redshift survey to probe dark energy

Yun Wang<sup>1\*</sup>, Will Percival<sup>2</sup>, Andrea Cimatti<sup>3</sup>, Pia Mukherjee<sup>4</sup>, I

- We also consider the dependence on the information used: the full galaxy power spectrum  $P(k)$ ,  $P(k)$  marginalized over its shape, or just the Baryon Acoustic Oscillations (BAO). We find that the inclusion of growth rate information (extracted using redshift space distortion and galaxy clustering amplitude measurements) **leads to a factor of 3 improvement in the FoM**, assuming general relativity is not modified. This inclusion partially compensates for the loss of information when only the BAO geometrical constraints, rather than the full  $P(k)$ , are used.

$$P_{obs}(k_{\perp}^{ref}, k_{\parallel}^{ref}) = \frac{[D_A(z)^{ref}]^2 H(z)}{[D_A(z)]^2 H(z)^{ref}} b^2 (1 + \beta \mu^2)^2 \cdot \left[ \frac{G(z)}{G(0)} \right]^2 P_{matter}(k)_{z=0}$$

**Key assumption:**

$K_{max}=0.1$  Mpc/h for  $z=0$  and  $k_{max}=0.2$  for  $z>1$

# Challenge

**to model RSD at 1% accuracy  
at  $k < 0.1\text{--}0.3 \text{ h/Mpc}$**

# A nominal way in Literature

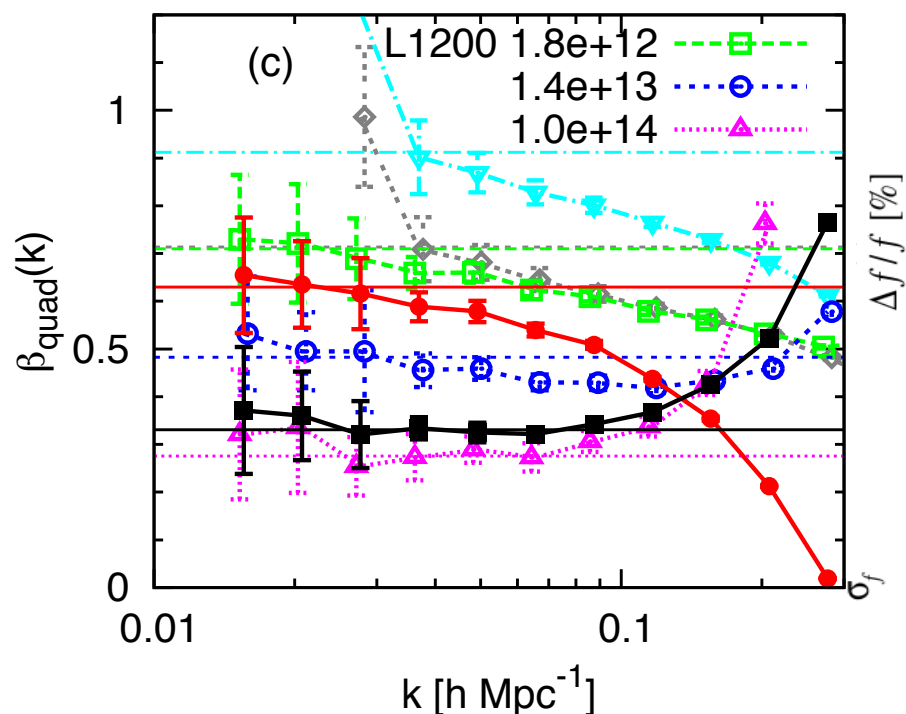
$$P_{\delta\delta}^s(k, u) \simeq P_{\delta\delta}(k) (1 + f u^2)^2 D^{\text{FOG}}(ku)$$

$$f \equiv d \ln D / d \ln a$$

$$u \equiv k_{\parallel} / k$$

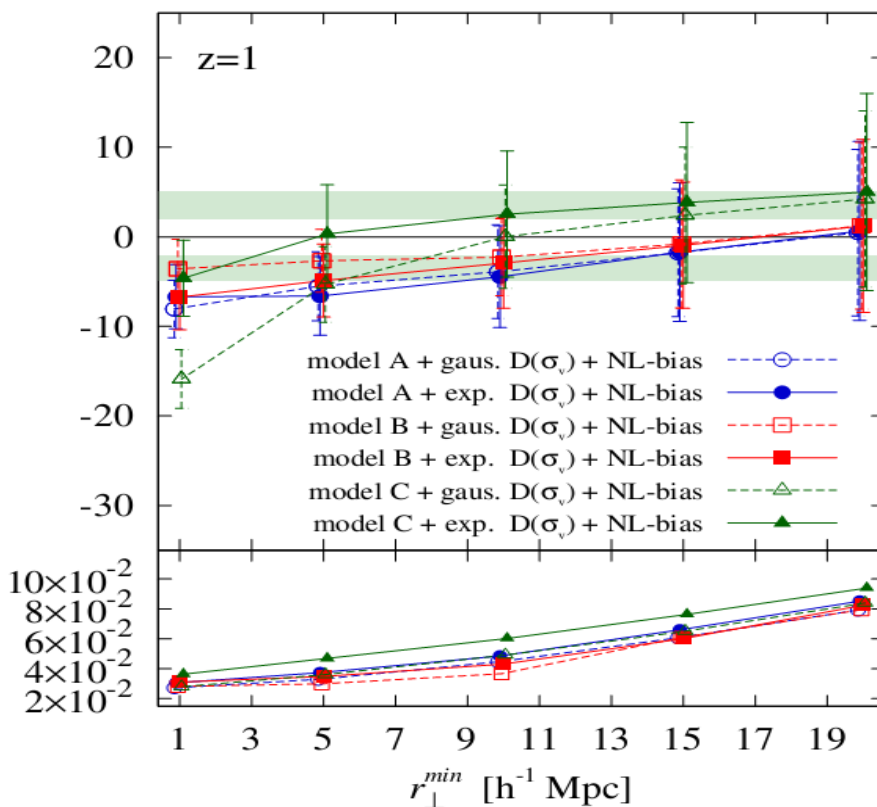
One can change this easily for a deterministic linear bias  $b$

# Systematic error detected at **10%** level



Okumura & Jing, 2010

Beta=f/b



Torre & Guzzo, 1202.5559

And many more works

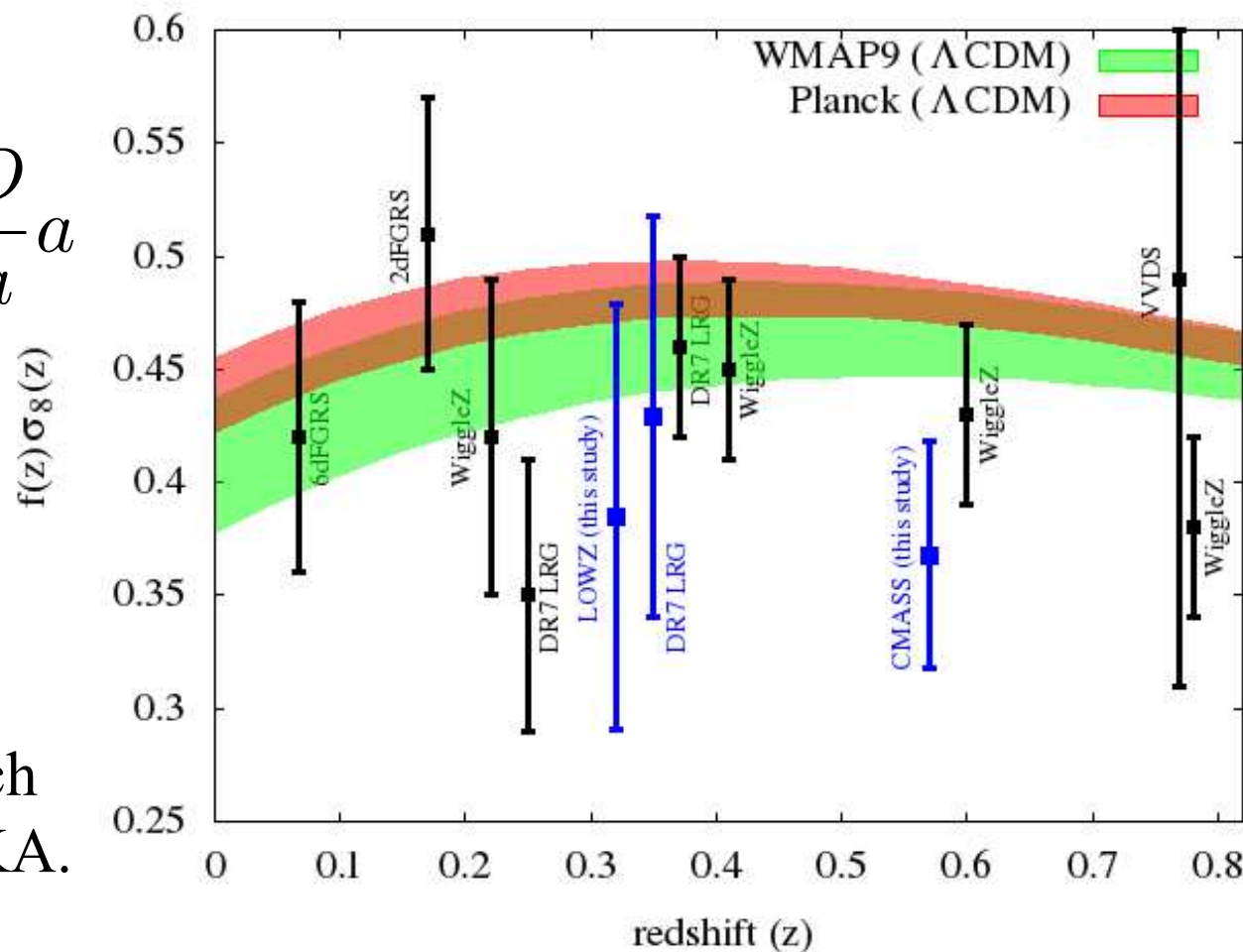


# Often further compressed into a single number

$$f(z)\sigma_8(z) \propto \frac{dD}{da}a$$

$$f \equiv \frac{d \ln D}{d \ln a}$$

Can achieve 1% for  
stage IV surveys such  
as MS-DESI and SKA.



Chuang et al. 1312.4889

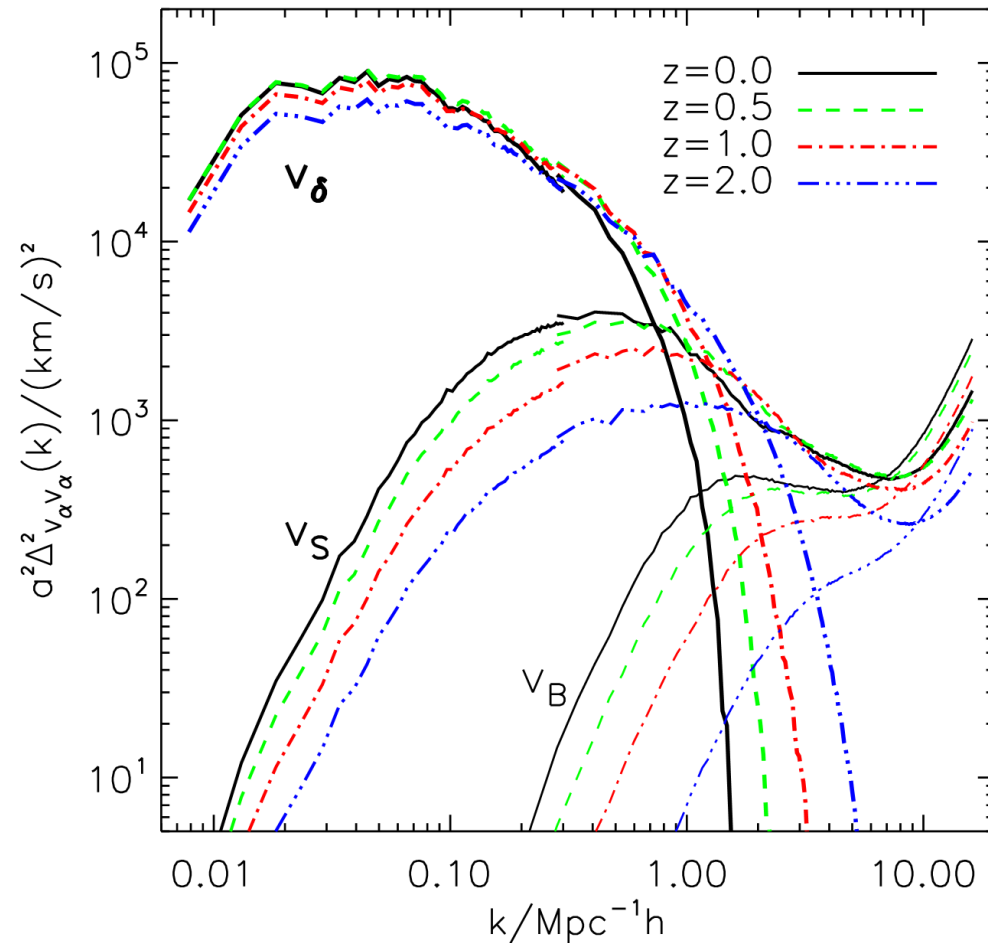
# Challenging to achieve 1% accuracy

- Many works to improve RSD model
  - e.g. Peebles 1980,..., Kaiser 1987,..., Hamilton 1992,..., Scoccimarro, 2000, ..., White 2001,..., Yang et al. 2002,..., Kang et al. 2002,..., Szapudi 2004,..., Zu et al. 2007,..., Tinker 2007, ..., Matsubara 2008,..., Taruya et al. 2010,..., Kwan et al. 2011,..., Seljak & McDonald, 2011,..., Reid & White 2011,..., Jennings et al. 2012,...
- Entangled complexities
  - **Nonlinear mapping between real and redshift space**
    - Redshift space 2pt is the sum of all N-pt in real space
  - **Nonlinearity in the dark matter density and velocity statistics**
    - Non-Gaussianity, no compact expression of redshift space ps
    - Stochastic velocity-density relation
  - **Nonlinear galaxy-dark matter relation**
    - Stochastic scale dependence density bias
    - Velocity bias
- Disentangle them!
  - ZPJ, Pan & Zheng, 2012; Zheng et al. 2013; ZPJ, Zheng & Jing, 2014, Zheng et al. in preparation,...
  - **Pengjie Zhang (SJTU), Yi Zheng (SHAO, Shanghai; Daejeong, Korea)**

# Disentangle RSD:

## A generic velocity decomposition

- Velocity decomposition into three eigen-modes:
  - Gradient part  $v_E$ 
    - $v_\delta$ : correlated with density: mostly linear, dominant at large scale
    - $v_S$ : uncorrelated: significant at intermediate scale
  - Curl part  $v_B$ 
    - Highly nonlinear, small scale
- Different origins
- Different scale/ $z$  dependence
- Different RSD



Zhang,, Pan, Zheng, 2013

Zheng et al. 2013

# The way to measure the three components in simulation

$$\mathbf{v}_E(\mathbf{k}) = \frac{(\mathbf{k} \cdot \mathbf{v}(\mathbf{k}))}{k^2} \mathbf{k}, \quad (7)$$

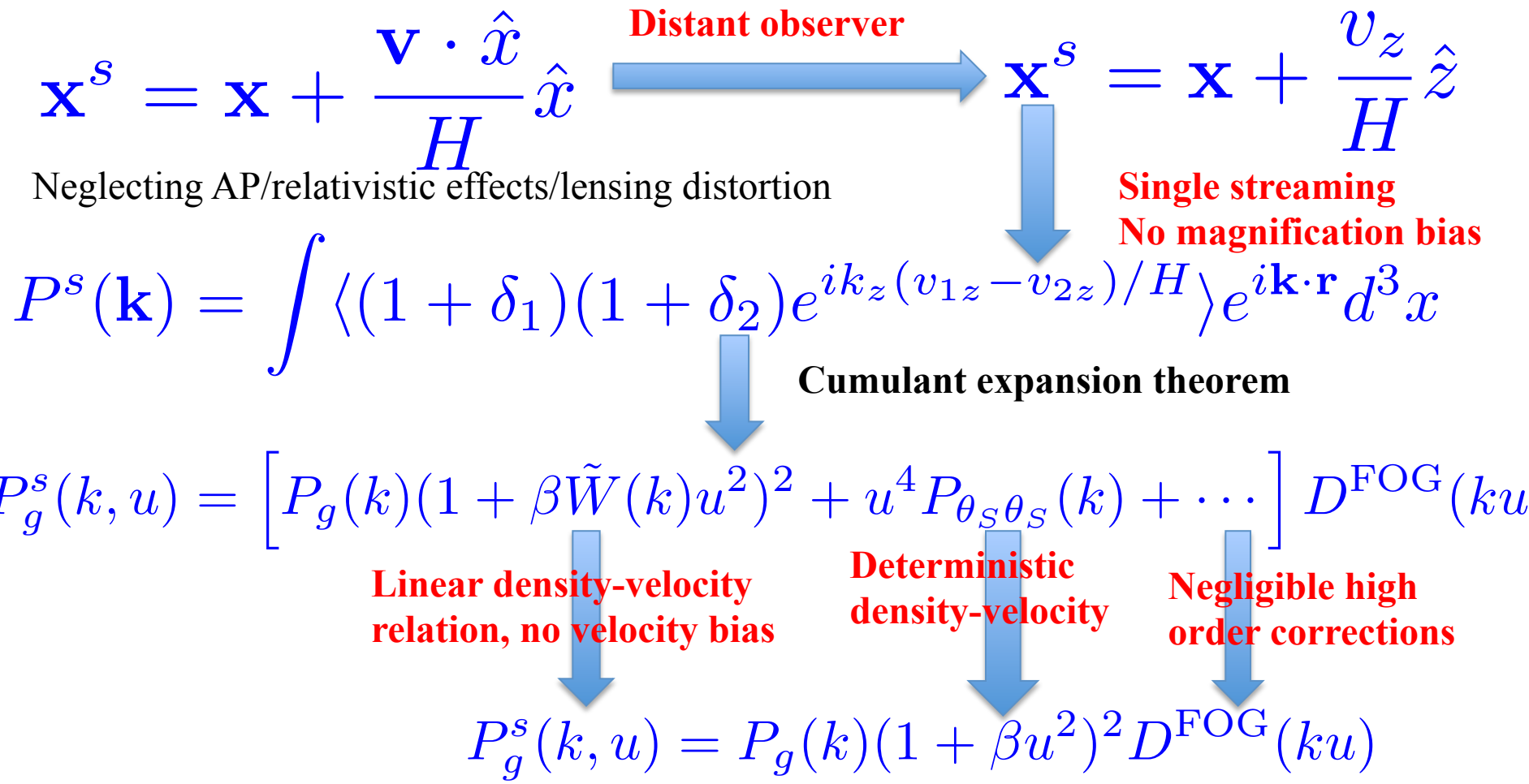
$$\mathbf{v}_B(\mathbf{k}) = \mathbf{v}(\mathbf{k}) - \mathbf{v}_E(\mathbf{k}) .$$

compose  $\mathbf{v}_E$  into  $\mathbf{v}_\delta$  and  $\mathbf{v}_S$  [ Eq. (3)],

$$\mathbf{v}_\delta(\mathbf{k}) = -i \frac{\delta(\mathbf{k}) W(k)}{k^2} \mathbf{k} , \quad (8)$$

$$\mathbf{v}_S(\mathbf{k}) = \mathbf{v}_E(\mathbf{k}) - \mathbf{v}_\delta(\mathbf{k}) .$$

# Incomplete list of approximations/simplifications in RSD modeling



Further approximations often used in observations

- **Scale independent galaxy density bias**
- **D<sup>FOG</sup>**: Gaussian, Lorentz, more complicated? Meaning of  $\sigma_v$ ?

# Challenging to achieve 1% accuracy

- Many works to improve RSD model
  - e.g. Peebles 1980,..., Kaiser 1987,..., Hamilton 1992,..., Scoccimarro, 2000, ..., White 2001,..., Yang et al. 2002,..., Kang et al. 2002,..., Szapudi 2004,..., Zu et al. 2007,..., Tinker 2007, ..., Matsubara 2008,..., Taruya et al. 2010,..., Kwan et al. 2011,..., Seljak & McDonald, 2011,..., Reid & White 2011,..., Jennings et al. 2012,...
- Entangled complexities
  - **Nonlinear mapping between real and redshift space**
    - Redshift space 2pt is the sum of all N-pt in real space
  - **Nonlinearity in the dark matter density and velocity statistics**
    - Non-Gaussianity, no compact expression of redshift space ps
    - Stochastic velocity-density relation
  - **Nonlinear galaxy-dark matter relation**
    - Stochastic scale dependence density bias
    - Velocity bias
- Disentangle them!
  - ZPJ, Pan & Zheng, 2012; Zheng et al. 2013; ZPJ, Zheng & Jing, 2014, Zheng et al. in preparation,...
  - **Pengjie Zhang (SJTU), Yi Zheng (SHAO, Shanghai; Daejeong, Korea)**

# A formula of Zhang et al.(2013)

$$P_{\delta\delta}^s(k, u) = \left\{ P_{\delta\delta}(k)(1 + f\tilde{W}(k)u^2)^2 + u^4 P_{\theta_S\theta_S}(k) \right. \\ \left. + C_{NG}(k, u) + C_G(k, u) + C_S(k, u) \right\} \\ \times D_{\delta}^{\text{FOG}}(ku) D_S^{\text{FOG}}(ku) D_B^{\text{FOG}}(ku) . \quad (26)$$

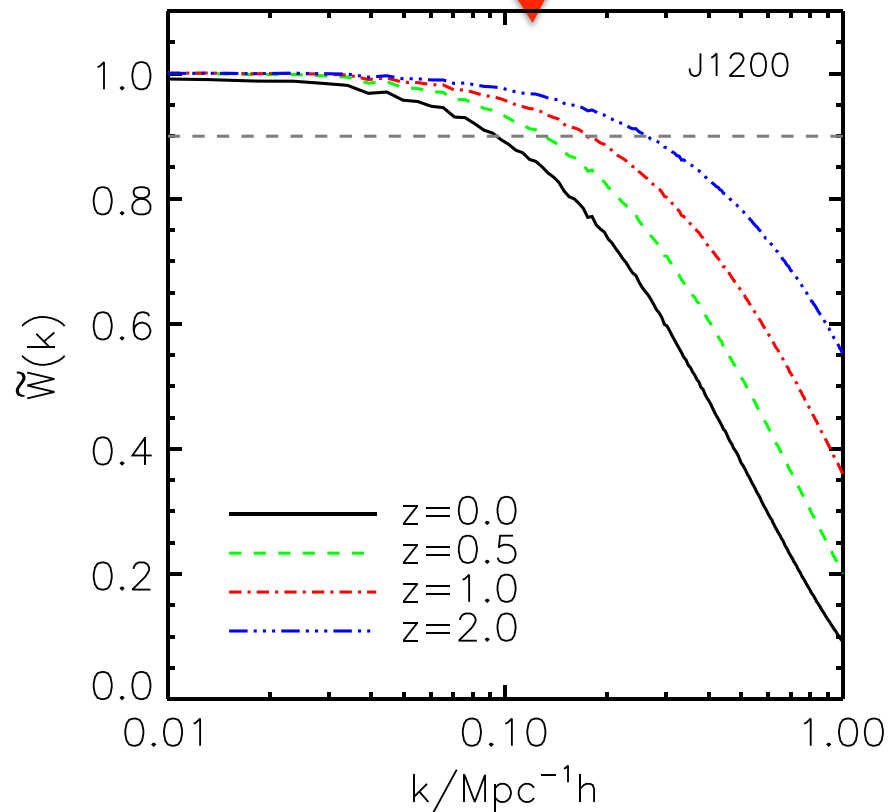
$$\theta(\mathbf{x}) \equiv -\nabla \cdot \mathbf{v}(\mathbf{x}) / \dot{H} \equiv -\nabla \cdot \mathbf{v}_E(\mathbf{x}) / H.$$

$$W(\mathbf{k}) = W(k) = \frac{P_{\delta\theta}(k)}{P_{\delta\delta}(k)}$$

$$\tilde{W}(k) \equiv \frac{W(k)}{W(k \rightarrow 0)} = \frac{W(k)}{f} = \frac{1}{f} \frac{P_{\delta\theta}(k)}{P_{\delta\delta}(k)}$$

# Disentangle RSD: nonlinear velocity-density

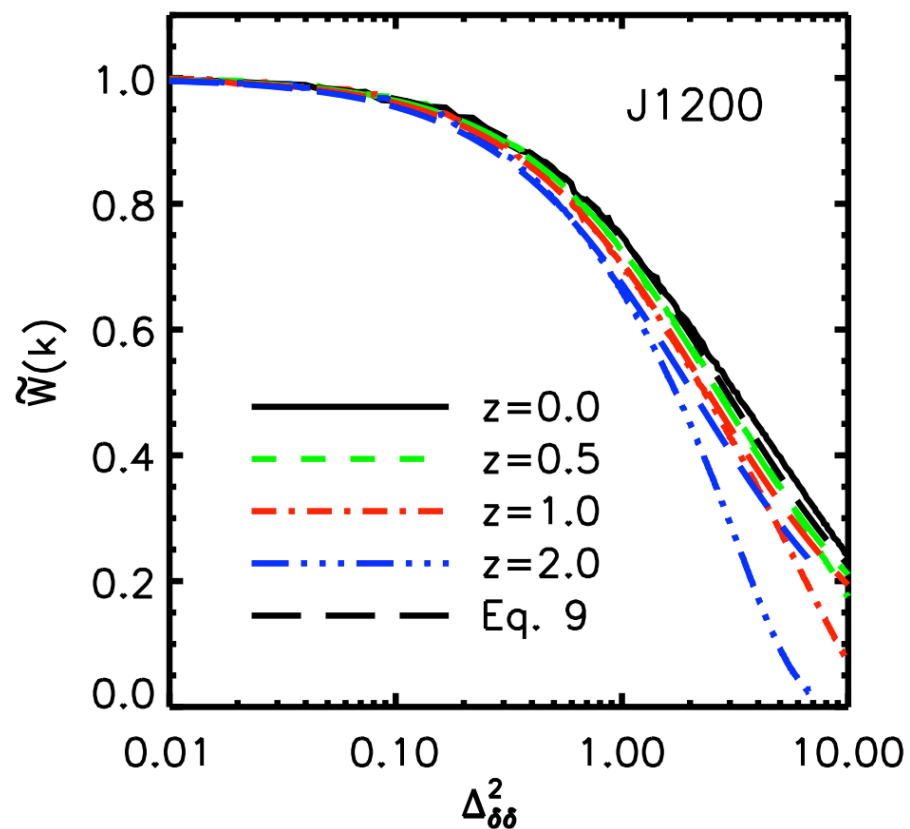
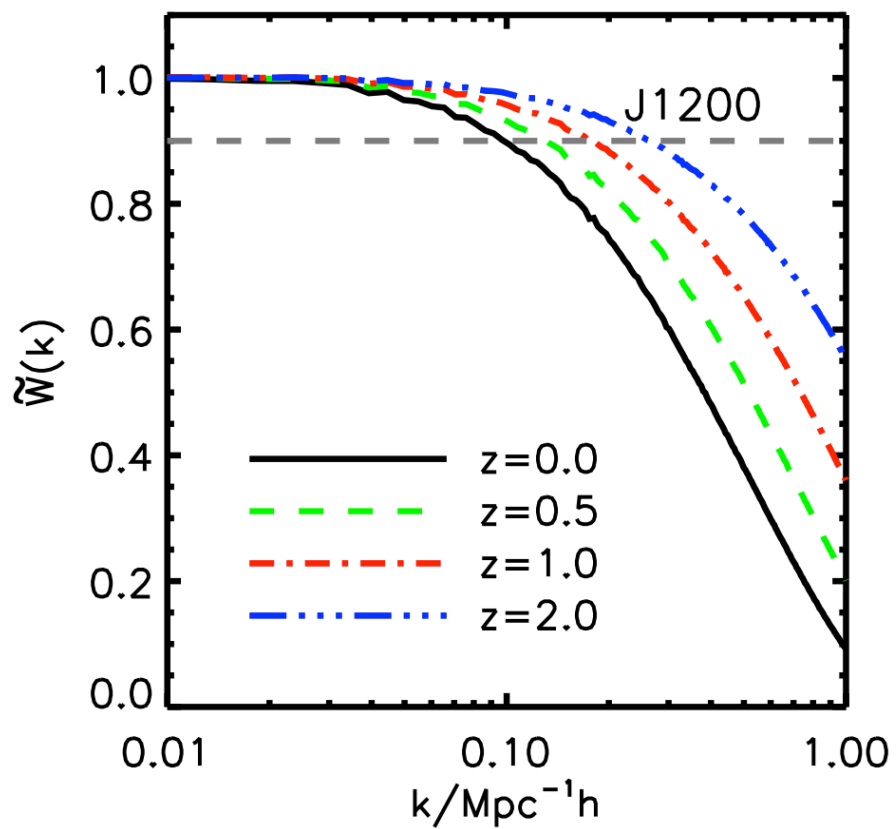
$$P^s(k, u) = \left[ P(k)(1 + f\tilde{W}(k)u^2)^2 + P_{\theta_s\theta_s}(k)u^4 + C_G(k, u) + C_{NG,3}(k, u) \right] D^{\text{FOG}}(ku)$$



Zheng et al. 2013

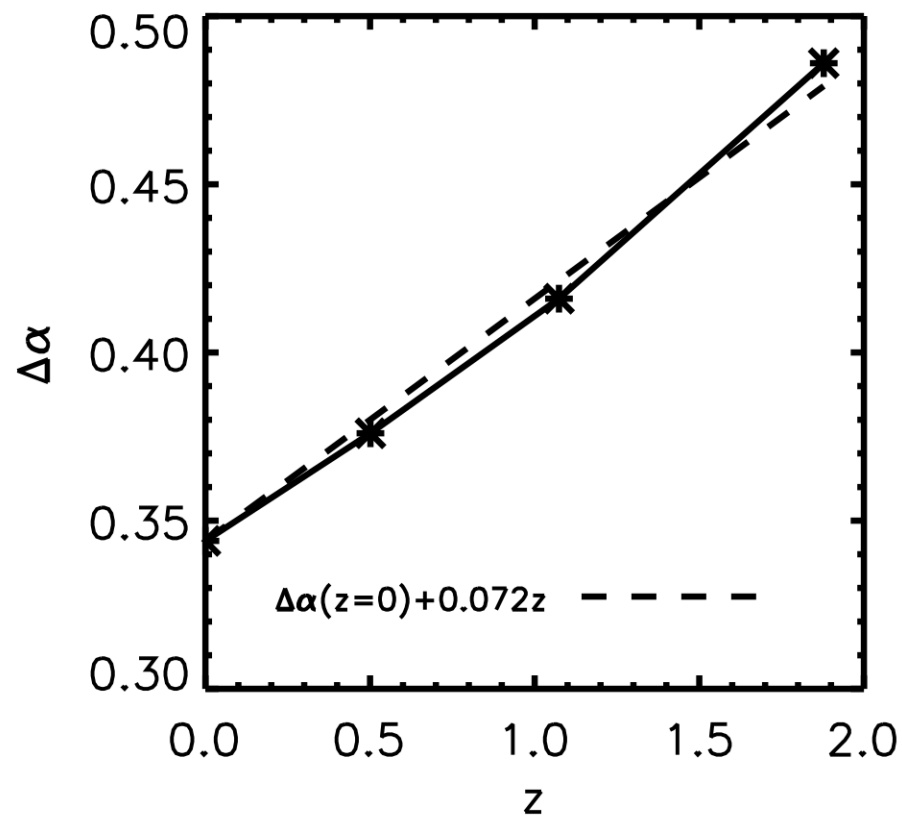
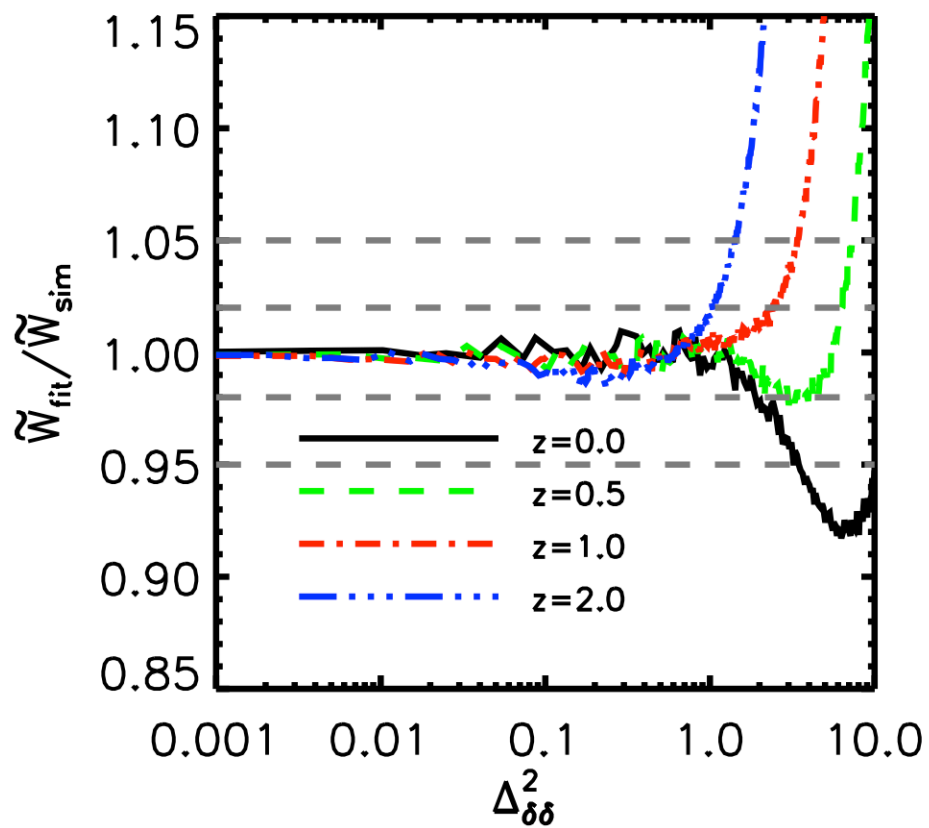
- Velocity growth is suppressed w.r.t density.
- Leading order correction to the Kaiser formula
- **10% at  $k=0.1h/\text{Mpc}$  and  $z=0$**





$$\begin{aligned}
\tilde{W}(k, z) &= \frac{1}{1 + \Delta\alpha(z)\Delta_{\text{NL}}^2(k, z)} \\
&\equiv \frac{1}{1 + \Delta\alpha(z)\Delta_{\delta\delta}^2(k, z)} .
\end{aligned}
\tag{13}$$

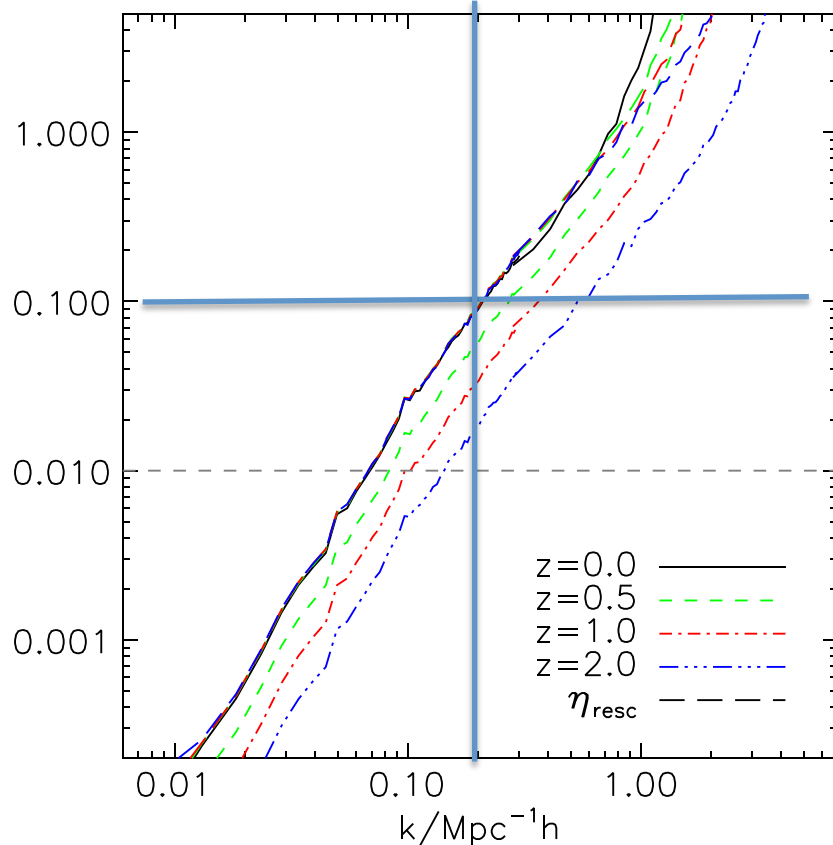
Redshift	$\Delta\alpha$	$\chi^2$	$\chi_{dof}^2$	$N_{\text{data}}$
$z = 0$	0.344	1.001	0.026	38
$z = 0.5$	0.376	1.0	0.019	54
$z = 1$	0.416	1.001	0.012	82
$z = 2$	0.486	1.01	0.007	145



# Disentangle RSD: stochastic velocity-density

$$P^s(k, u) = \left[ P(k)(1 + f\tilde{W}(k)u^2)^2 + P_{\theta_s\theta_s}(k)u^4 + C_G(k, u) + C_{NG,3}(k, u) \right] D^{\text{FOG}}(ku)$$

$$P_{\theta_s\theta_s} / P_{\theta_\delta\theta_\delta}$$



Zheng et al. 2013

- Stochastic velocity  $v_s$  has a leading order contribution with  $\mathbf{u}^4$  directional dependence

- **O(1%) effect at  $k=0.1h/\text{Mpc}$  and  $z=0-2$ .**

# Disentangle RSD: Finger of God

$$D_B(k_z, \mathbf{r}) \equiv \left\langle \exp \left( i \frac{k_z (v_{1z,B} - v_{2z,B})}{H} \right) \right\rangle$$

Similarly for s and delta velocity components

# One-point distribution function

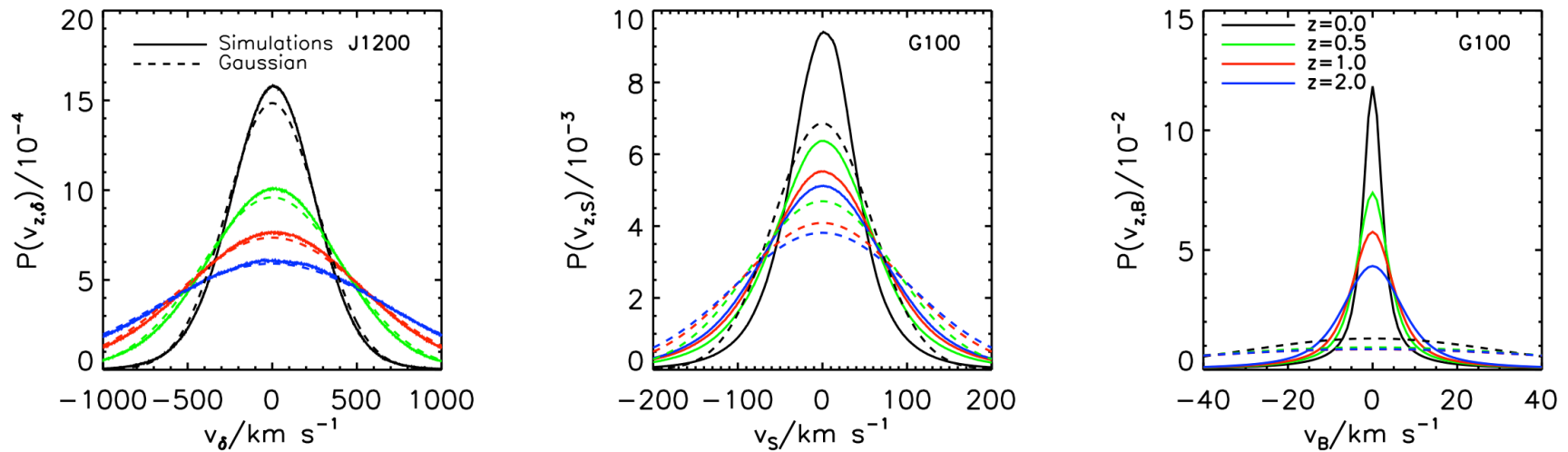


FIG. 8: The PDFs of  $\mathbf{v}_{\delta,S,B}$  along the  $z$  axis are shown by solid lines. The dashed lines show Gaussian distributions with the same velocity mean and dispersion of corresponding velocity PDFs. Different line colors represent different redshifts. Apparently,  $\mathbf{v}_{\delta}$  is the most Gaussian velocity component since it mainly correlates with linear matter density field and the window function  $\tilde{W}$  suppresses non-Gaussianities from small scales. In contrast,  $\mathbf{v}_B$  is strongly non-Gaussian, consistent with the fact that most contribution comes from strongly nonlinear and non-Gaussian scales.

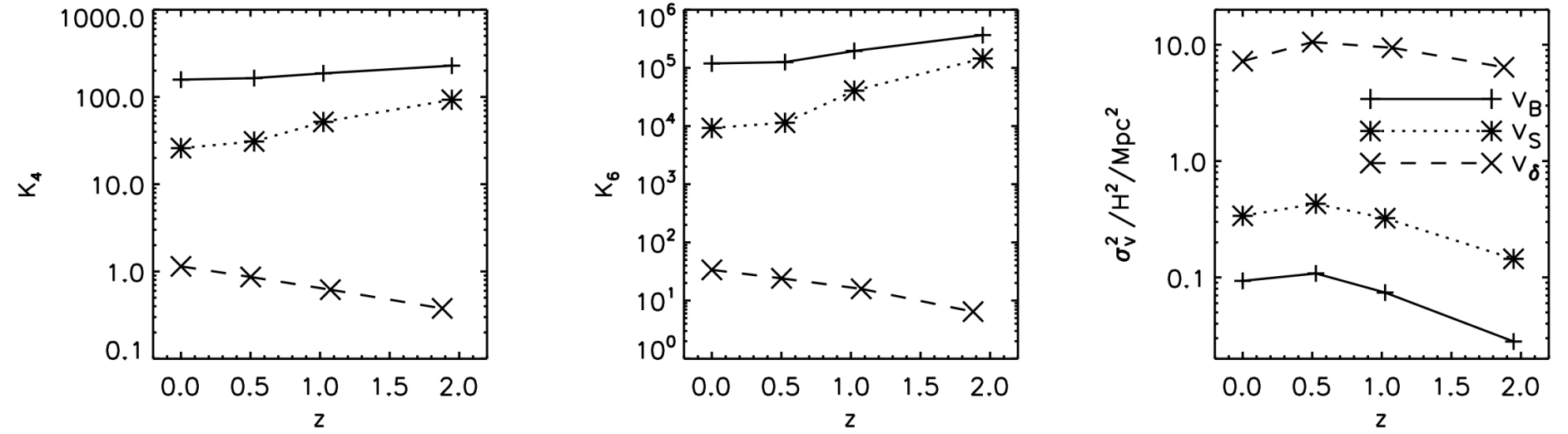
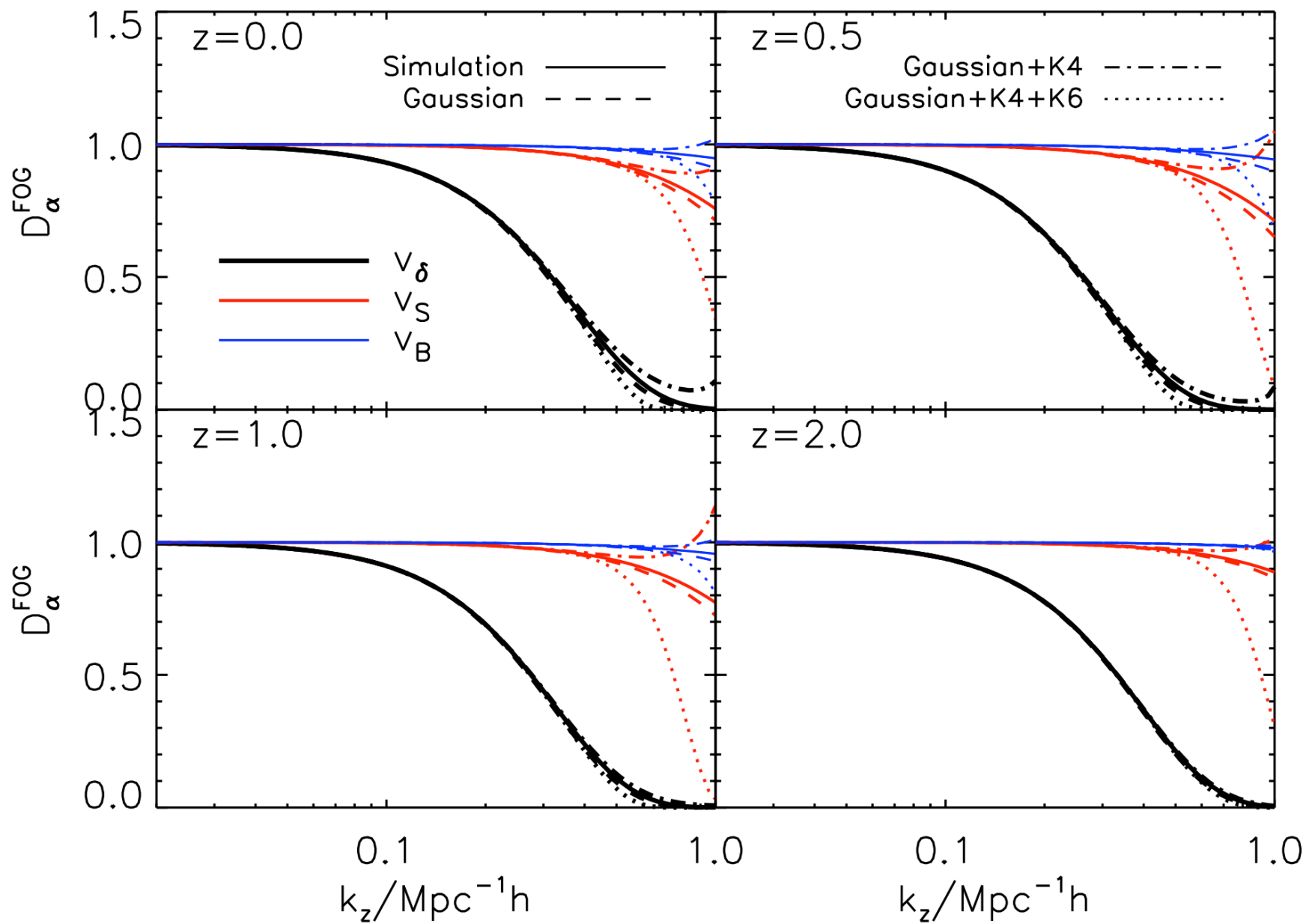


FIG. 9: *Left and middle panels:* The fourth and sixth order of reduced cumulants of  $\mathbf{v}_{\delta,S,B}$ . They confirm the non-Gaussianity results shown in Fig. [8]. Towards lower redshift, non-Gaussianities of  $\mathbf{v}_{S,B}$  decrease, likely due to ongoing halo virialization and the associated velocity randomization, while non-Gaussianity of  $\mathbf{v}_\delta$  increases due to nonlinear structure evolution. *Right panel:*  $\sigma_{v_\alpha}^2/H^2$  determines the leading-order damping to redshift space clustering caused by the FOG effect [Eq. (23), Fig. [10].

$$K_4 \equiv \frac{\langle v^4 \rangle}{\langle v^2 \rangle^2} - 3 ,$$

$$K_6 \equiv \frac{\langle v^6 \rangle}{\langle v^2 \rangle^3} - 10 \frac{\langle v^3 \rangle^2}{\langle v^2 \rangle^3} - 15 \frac{\langle v^4 \rangle}{\langle v^2 \rangle^2} + 30$$





locity dispersion,

$$\sigma_{v_\alpha}^2 = \xi_{v_{z,\alpha} v_{z,\alpha}}(r=0) = \frac{1}{3} \int \Delta_{v_\alpha v_\alpha}^2(k) \frac{dk}{k} . \quad (22)$$

To the first order, the damping functions take Gaussian form,

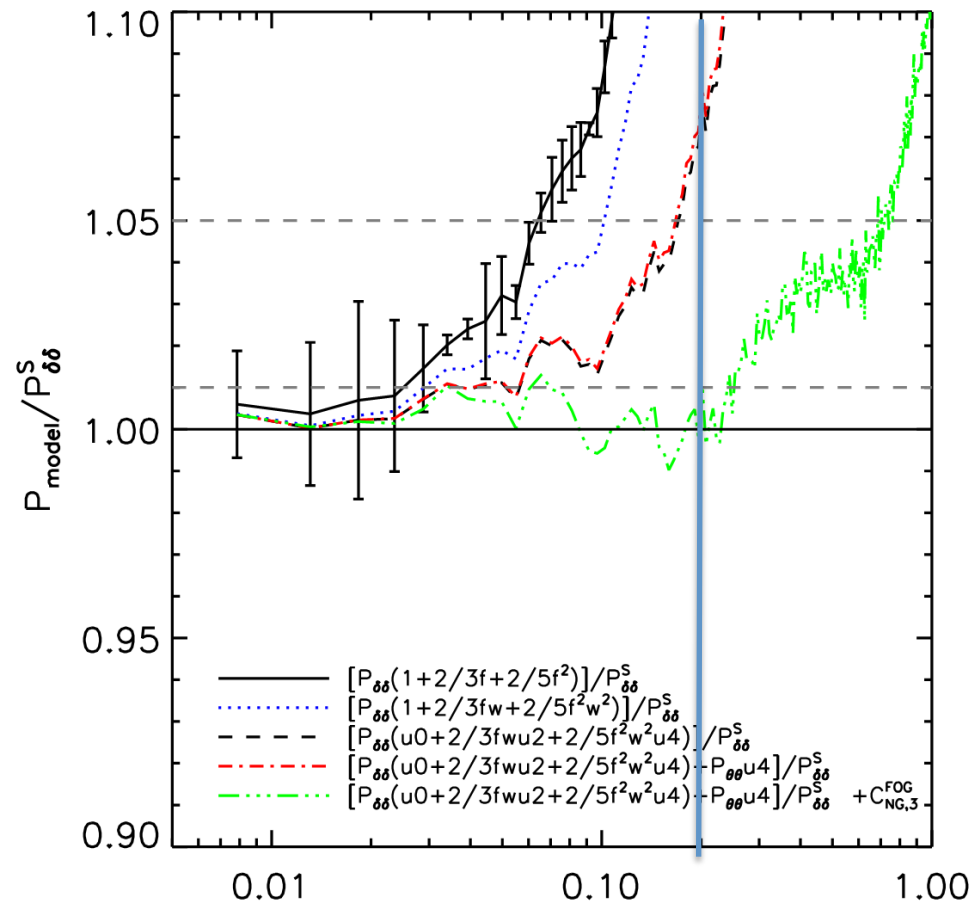
$$\sqrt{D_\alpha^{\text{FOG}}(k_z)} = \exp\left(-\frac{x}{2}\right) = \exp\left(-\frac{(k_z \sigma_{v_\alpha})^2}{2H^2}\right) . \quad (23)$$

$$\begin{aligned} D^{\text{FOG}}(k_z) &\equiv D_\delta^{\text{FOG}}(k_z) D_S^{\text{FOG}}(k_z) D_B^{\text{FOG}}(k_z) \quad (24) \\ &\simeq \exp\left(-\frac{k_z^2(\sigma_{v_\delta}^2 + \sigma_{v_S}^2 + \sigma_{v_B}^2)}{H^2}\right) \\ &\simeq \exp\left(-\frac{k_z^2 \sigma_{v_\delta}^2}{H^2}\right) . \end{aligned}$$

Gaussian, not Lorentz

# Disentangle RSD: 1% at $k < 0.2 \text{ Mpc/h}$

$$P^s(k, u) = \left[ P(k)(1 + f\tilde{W}(k)u^2)^2 + P_{\theta_s\theta_s}(k)u^4 + C_G(k, u) + C_{NG,3}(k, u) \right] D^{\text{FOG}}(ku)$$



- $C_G, C_{NG,3}$  arise from  $\mathbf{v}_\delta$ .
- Fully determined by  $\mathbf{W}$ ! No degrees of freedom (ZPJ et al. 2012)
- Including them improves the accuracy, without sacrifice on constraining power.
- Many more tests to fully quantify its accuracy (Zheng et al. 2014, in preparation)

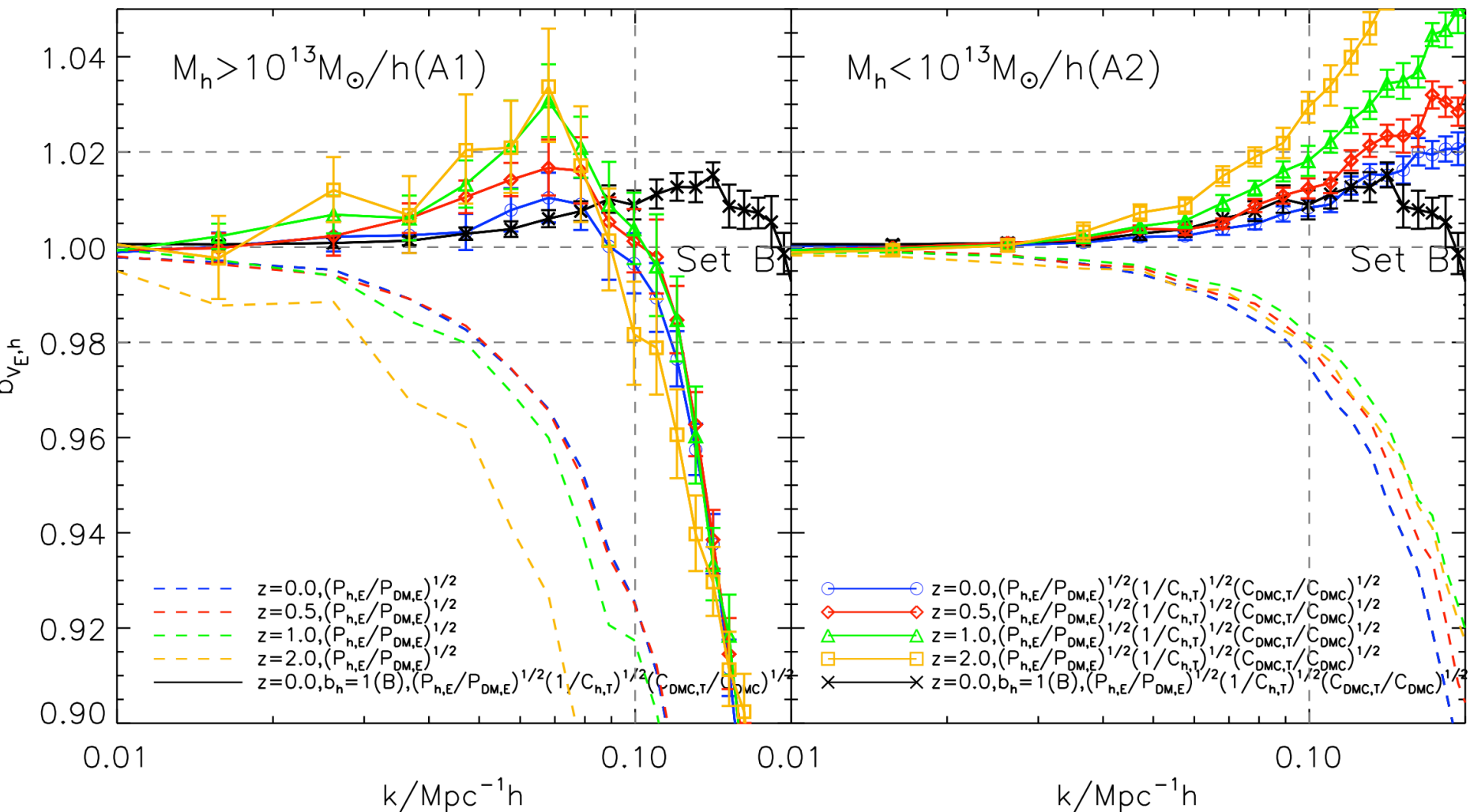
# Now galaxy bias

- Spatial sampling bias
- Dynamical velocity bias
- Spatial +velocity coupling bias
- .....
- First, go to dark matter halos

# Challenging to achieve 1% accuracy

- Many works to improve RSD model
  - e.g. Peebles 1980,..., Kaiser 1987,..., Hamilton 1992,..., Scoccimarro, 2000, ..., White 2001,..., Yang et al. 2002,..., Kang et al. 2002,..., Szapudi 2004,..., Zu et al. 2007,..., Tinker 2007, ..., Matsubara 2008,..., Taruya et al. 2010,..., Kwan et al. 2011,..., Seljak & McDonald, 2011,..., Reid & White 2011,..., Jennings et al. 2012,...
- Entangled complexities
  - **Nonlinear mapping between real and redshift space**
    - Redshift space 2pt is the sum of all N-pt in real space
  - **Nonlinearity in the dark matter density and velocity statistics**
    - Non-Gaussianity, no compact expression of redshift space ps
    - Stochastic velocity-density relation
  - **Nonlinear galaxy-dark matter relation**
    - Stochastic scale dependence density bias
    - Velocity bias
- Disentangle them!
  - ZPJ, Pan & Zheng, 2012; Zheng et al. 2013; ZPJ, Zheng & Jing, 2014, Zheng et al. in preparation,...
  - **Pengjie Zhang (SJTU), Yi Zheng (SHAO, Shanghai; Daejeong, Korea)**

# Velocity bias at $z \geq 0$ : No velocity bias for $k < 0.1 \text{ h/Mpc}$



ZHENG et al. 2014

# Conclusions

- 1% level accuracy presents a **key challenge** to the theoretical modeling of RSD;
- A way of decomposing velocity into 3 components **can filter out unwanted and simplify the modeling**; our results point to a promising start: 1% accuracy is achievable for  $k < 0.1\text{--}0.3 \text{ h/Mpc}$ ;
- Finger-of-God effect is a Gaussian form, determined by the velocity power spectrum of the density induced gradient part;
- **No significant halo velocity bias for  $k < 0.1 \text{ h/Mpc}$**

# Future

- Now we are applying the model to BOSS sample;
- Including subhalos to study galaxy velocity power spectrum;
- We are using scale-free models to improve our model accuracy;
- Hydro simulations (big enough?)