

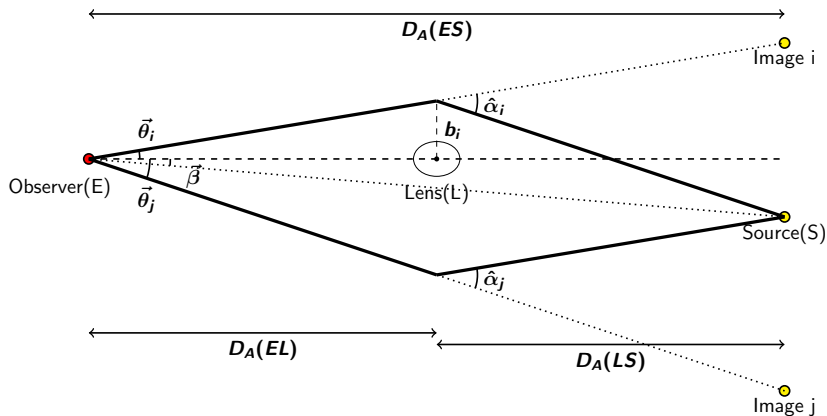
Measuring Angular Diameter Distances Using Time-delay Lenses

arXiv:1410.7770

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Strong lens with time delay



$$\Delta t_{i,j} = \frac{1 + z_L}{2c} \frac{D_A(EL) D_A(ES)}{D_A(LS)} \phi(\vec{\theta}, \vec{\beta}) \equiv \frac{D_{\Delta t}}{2c} \phi(\vec{\theta}, \vec{\beta}) \quad (1)$$

Time-delay distance $D_{\Delta t}$

- ▶ Strong lens with variable sources
- ▶ Measure of distance-like quantity, $D_{\Delta t}$
- ▶ Sensitive only to the Hubble constant H_0
- ▶ External convergence (mass external to the lens lies along the line-of-sight) as the main source of uncertainty (Suyu et al. 2006)

⇒ Alternative way to measure the distance using strong lenses?

Measuring D_A using time-delay lenses

Paraficz & Hjorth (2009)

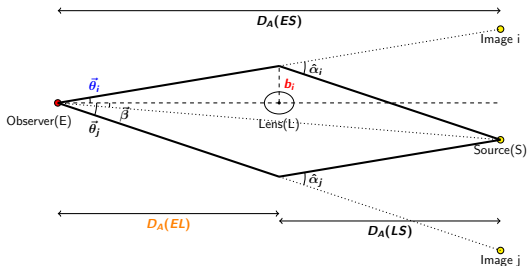
- ▶ Singular isothermal sphere (SIS) density profile
- ▶ Combine lensing dynamics (velocity dispersion) and the time-delay
- ▶ Measured the angular diameter distance using time delay $\Delta t_{i,j}$, velocity dispersion σ^2 , lens redshift z_L and the image positions θ_i, θ_j

$$D_A(EL) = \frac{c^3 \Delta t_{i,j}}{4\pi\sigma^2(1+z_L)} \frac{1}{(\theta_j - \theta_i)} \quad (2)$$

Limitations

- ▶ Spherically symmetric mass distribution, isotropic velocity dispersion
- ▶ No study on the effect of external convergence

Physical Intuition



When the mass distribution is known,

- ▶ Time delay \rightarrow Mass estimate
- ▶ Velocity dispersion \rightarrow Potential

\Rightarrow Combine them to get the **physical size** (b) of the system

Observation of strong lensing arc gives the **angular size** (θ) of the system

\Rightarrow The system can be used as a standard ruler to measure the **angular diameter distances** to the lens galaxy ($D_A(EL) = \frac{b}{\theta}$)

Power-law density profile and the time delay

Time delay

$$\begin{aligned}\Delta t_{i,j} &= \frac{(1+z_L)}{2c} \frac{D_A(EL)D_A(ES)}{D_A(LS)} \left[(\vec{\alpha}_i + \vec{\alpha}_j) \cdot (\vec{\theta}_i - \vec{\theta}_j) - \frac{2}{3-\gamma} (\vec{\alpha}_i \cdot \vec{\theta}_i - \vec{\alpha}_j \cdot \vec{\theta}_j) \right] \\ &= \frac{(1+z_L)}{2c} D_A(EL) \left[(\hat{\alpha}_i + \hat{\alpha}_j) \cdot (\vec{\theta}_i - \vec{\theta}_j) - \frac{2}{3-\gamma} (\hat{\alpha}_i \cdot \vec{\theta}_i - \hat{\alpha}_j \cdot \vec{\theta}_j) \right] \quad (6)\end{aligned}$$

⇒ The angular diameter distance becomes

$$D_A(EL) = \frac{c^3 \Delta t_{i,j}}{4\pi\sigma_r^2(r)(1+z_L)} (\Delta\tilde{\theta}_{i,j})^{-1} \quad (7)$$

where $\Delta\tilde{\theta}_{i,j}$ is a function of θ_i , θ_j and γ .

Mass-sheet transformation : properties

Used to model the external convergence

Family of the *source-position transformation*

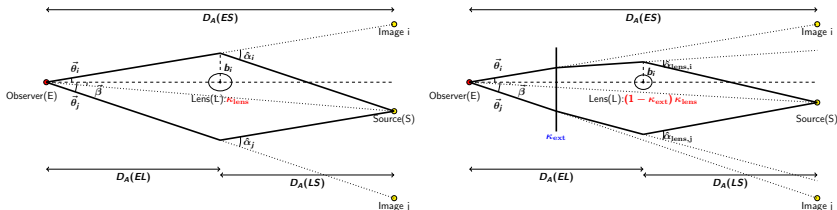
Can reproduce strong lens observables as

- ▶ Image position
- ▶ Flux ratio

Changes

- ▶ Source position (not an observable)
- ▶ Time delay

$$\kappa_{\text{lens}} \rightarrow \kappa_{\text{MST}} = \kappa_{\text{ext}} + (1 - \kappa_{\text{ext}}) \kappa_{\text{lens}} \quad (8)$$



Mass-sheet transformation : effect

Time-delay after the MST

$$\Delta t_{i,j,\text{MST}} = (1 - \kappa_{\text{ext}}) \Delta t_{i,j} \quad (9)$$

Velocity dispersion after the MST

$$\sigma_{\text{MST}}^2 = (1 - \kappa_{\text{ext}}) \sigma^2 \quad (10)$$

$\Rightarrow D_A(EL) \propto \frac{\Delta t}{\sigma^2}$ **invariant** under the MST!

No need to model the external convergence

Uncertainty on D_A

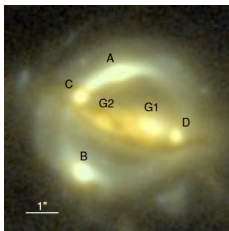


Figure: B1608+656

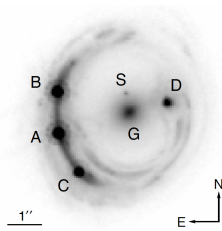


Figure: RXJ1131-1231

Tests on B1608+686 & RXJ1131-1231

(Data and figures from Suyu et al. 2010 & Suyu et al. 2013, and references therein, respectively)

- ▶ Uncertainties from γ and $\Delta t_{i,j}$ are negligible
- ▶ Velocity dispersion is the biggest source of uncertainty
- ▶ Uncertainty on D_A is $\sim 13 - 14\%$ with current data
- ▶ Potential estimation (velocity dispersion) seems to play an important role: How to take into account the anisotropic velocity dispersion?

Anisotropic velocity dispersion : modeling

Osipkov-Merritt anisotropy

$$\beta_{\text{ani}}(r) = \frac{r^2}{r_a^2 + r^2} = 1 - \frac{\sigma_T^2(r)}{\sigma_r^2(r)} \quad (11)$$

- ▶ Anisotropy parametrization : $r_a = nR_{\text{eff}}$
- ▶ Isotropic core & radial envelope

Jeans equation

$$\frac{1}{\rho_*} \frac{d(\sigma_r^2 \rho_*)}{dr} + 2\beta_{\text{ani}} \frac{\sigma_r^2}{r} = -\frac{GM(\leq r)}{r^2} \quad (12)$$

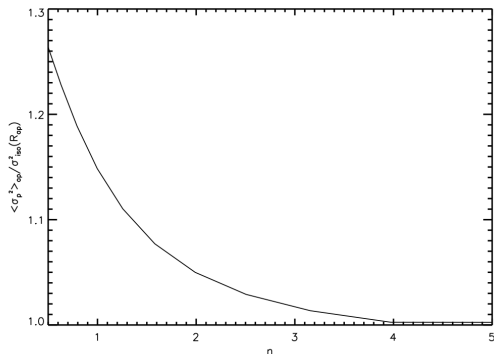
Projection & luminosity weighting (Hernquist profile)

$$\sigma_p^2(R) = I_H(R) \sigma_s^2(R) = 2 \int_R^\infty (1 - \beta_{\text{ani}} \frac{R^2}{r^2}) \frac{\rho_*(r) \sigma_r^2(r) r dr}{\sqrt{r^2 - R^2}} \quad (13)$$

Aperture-averaged velocity dispersion

Measured velocity dispersion is luminosity-weighted, aperture-averaged

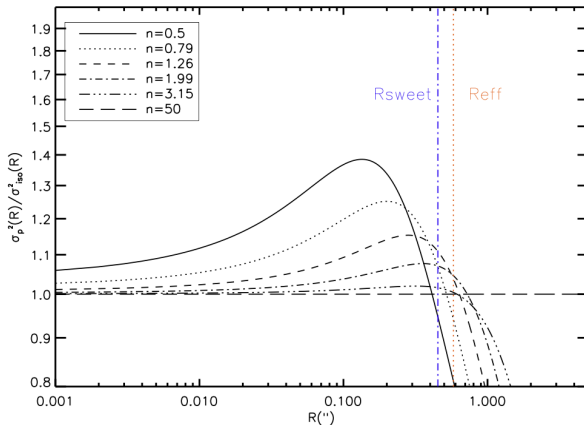
$$\langle \sigma_p^2 \rangle_{\text{ap}} \equiv \frac{\int_{\text{ap}} \sigma_s^2 I_H R \, dR \, d\theta}{\int_{\text{ap}} I_H R \, dR \, d\theta} \quad (14)$$



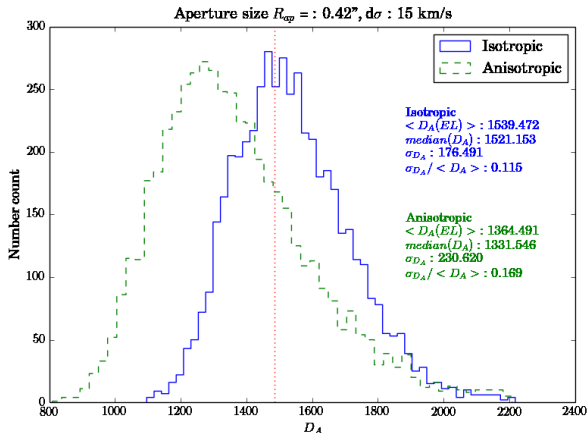
The velocity dispersion varies significantly due to the anisotropy!

Sweet-spot method

Radius where the scatter in anisotropic velocity dispersion is minimized

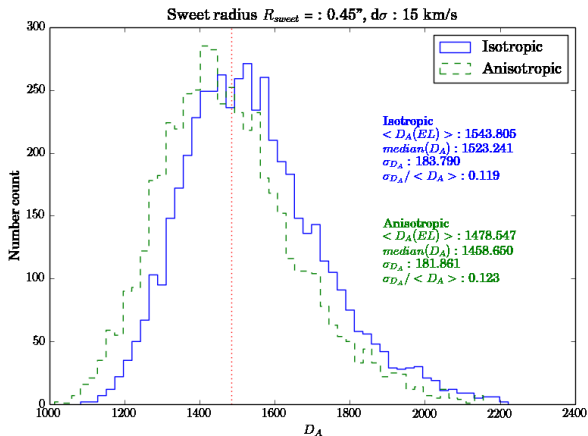


Monte-Carlo simulation 1: D_A measured at $\langle \sigma_p^2 \rangle_{\text{ap}}$



Anisotropic velocity dispersion biases the distribution, and the width of the distribution is increased

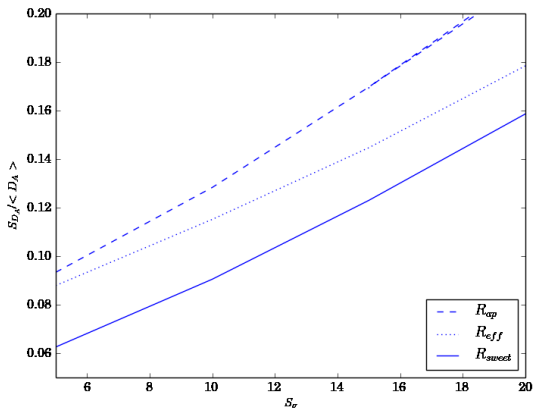
Monte-Carlo simulation 2: D_A measured at $\sigma_p^2(R_{\text{sweet}})$



Anisotropic velocity dispersion does not bias the distribution, and the width of the distribution does not change significantly

Expectation

Uncertainties on measured velocity dispersion [km/s] vs. the fractional uncertainty on D_A inferred



$\sim 7\%$ precision is achievable with 5% precision measurement on σ^2
from a single system!

Summary

- ▶ Strong lens with time delay can be used as a standard ruler to measure the **angular diameter distances** to the lens
- ▶ The external convergence cancels out : The main source of uncertainty in measuring the time-delay distances is not there
- ▶ The biggest uncertainty on D_A is from the velocity dispersion and its anisotropy
- ▶ Using spatially resolved velocity dispersion profile (at the sweet spot radius) will improve the precision
- ▶ More studies on anisotropy parametrization are required
- ▶ **arXiv:1410.7770** for more details!