

# Open KIAS Winter School Project on Charged Lepton Flavor Violation and Top Physics (Prof. Pyungwon Ko)

**Prob. 1** (a) Write down the operators describing proton decay ( $\Delta B = 1$ ), and derive the bound on the new physics scale from the lower bound on the proton lifetime.

(b) Write down the operators describing  $n - \bar{n}$  (neutron-antineutron) oscillation ( $\Delta B = 2$ ). Using the lower bound on the transition rate, estimate the new physics scale for  $n - \bar{n}$  (neutron-antineutron) oscillation, and compare it with the scale derived from proton decay in Prob. 1 (a).

(c) Write down the operators describing  $\mu \rightarrow e\gamma$  and  $\mu \rightarrow 3e$ , and estimate the lower bounds on the new physics scale for these decays using the current upper bounds on the branching ratios for these decays.

**Prob. 2** (a) Discuss the correlation between the electron spin and its energy in muon decay  $\mu^- \rightarrow e^- \bar{\nu}_e \nu_\mu$ . Compare this with the positron spin in antimuon decay  $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$ . You can use the  $(V - A) \times (V - A)$  nature of weak interactions (charged current).

(b) Consider Higgs decays

$$\begin{aligned} H &\rightarrow W^+ W^- \rightarrow (l^+ \nu_l)(l^- \bar{\nu}_l) \\ &\rightarrow \tau^+ \tau^- \rightarrow (\pi^+ \bar{\nu}_\tau)(\pi^- \nu_\tau) \end{aligned}$$

Discuss the correlation between the energy of the final charged leptons or charged pions and the helicity of  $W$ 's or  $\tau$ 's using the helicity conservation and  $(V - A) \times (V - A)$  nature of weak interactions (charged current) and assuming the spin of Higgs boson is either 0 or 2.

(c) Consider the top decays  $t \rightarrow bW^+$  followed by  $W^+ \rightarrow l^+ \nu_l$ . Discuss the correlation between the energy of the final charged lepton and its helicity, relative to the direction of the initial top spin.

Note : You can access "Particle Data Group" at <http://pdg.lbl.gov> and get informations on the particle properties in order to solve these problems.