

# Non-Abelian models of t-channel top physics

University of Michigan  
Sunghoon Jung

May 24, 2011 @ KIAS LHC  
meeting

Based on SJ, A.Pierce, J.Wells [1103.4835]

# What was discussed last Friday

- Regarding Tevatron measurements of  $A_{fb}$  and  $W_{jj}$ .
- Light  $V'$  ( $m_{V'} < m_t$ ) can contribute to both  $A_{fb}$  and  $W_{jj}$ .
- Demonstration of important unfolding issue.
- Summary of hadron collider phenomenology of t-channel physics models (mostly for  $m_{V'} > m_t$ )
- Hadron collider phenomenology for the light  $V'$ .
- Direct asymmetry observables at the LHC.

# Today, a non-Abelian model and pheno

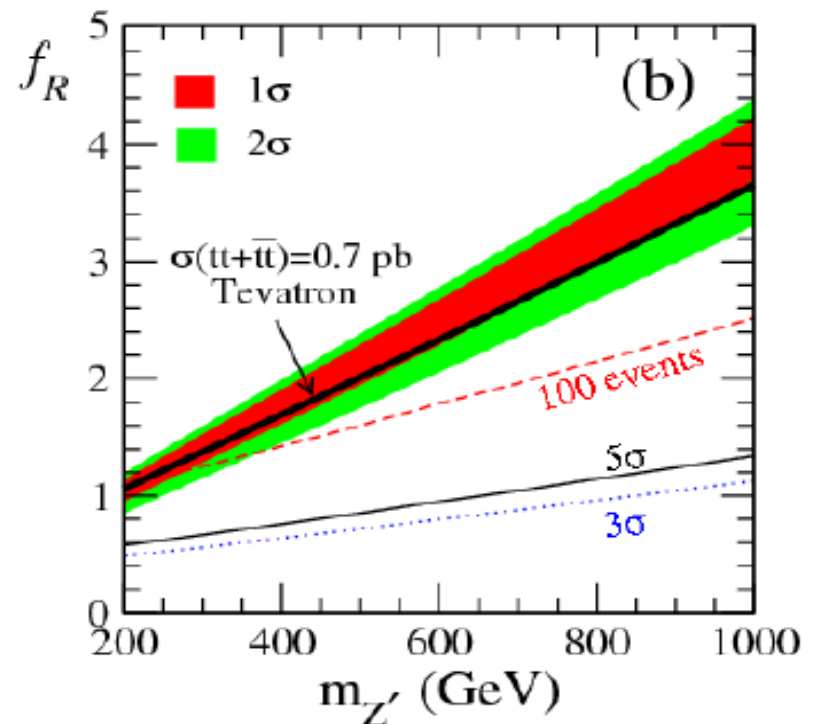
- Focus on one specific model : non-Abelian model of  $V'$ - $u$ - $t$  coupling.
- Issues in Model buildings.
- Hadron collider phenomenology (some are for this model, some are for general  $t$ -channel models).

# Abelian model suffers

Abelian  $Z'$ - $u$ - $t$  model is a simple implementation of  $t$ -channel physics idea.

$$\mathcal{L} \ni g_X Z'_\mu \bar{u} \gamma^\mu P_R t + h.c.$$

But,  $Z'$  couples both to top and anti-top. Like-sign dileptons from like-sign top pairs are already strong for most of parameter space except for the light  $Z'$ . LHC will probe there as well.



# Lagrangian for non-Abelian Zut model

SU(2) model.  $(t_R, u_R)$  is a doublet.

$$\begin{aligned}\mathcal{L} = & \frac{g_X}{\sqrt{2}} W'_\mu \left\{ \bar{t}_R \gamma^\mu t_R (-cs) + \bar{u}_R \gamma^\mu u_R (cs) + \bar{t}_R \gamma^\mu u_R (c^2) + \bar{u}_R \gamma^\mu t_R (-s^2) \right\} \\ & + \frac{g_X}{\sqrt{2}} W'_\mu \left\{ \bar{t}_R \gamma^\mu t_R (-cs) + \bar{u}_R \gamma^\mu u_R (cs) + \bar{t}_R \gamma^\mu u_R (-s^2) + \bar{u}_R \gamma^\mu t_R (c^2) \right\} \\ & + \frac{g_X}{2} Z'_\mu \left\{ \bar{t}_R \gamma^\mu t_R (c^2 - s^2) + \bar{u}_R \gamma^\mu u_R (s^2 - c^2) + \bar{t}_R \gamma^\mu u_R (2cs) + \bar{u}_R \gamma^\mu t_R (2cs) \right\}.\end{aligned}$$

If gauge boson couples to mass eigenstate fermions, mixing between  $t_R$  and  $u_R$  will be induced, parametrized by  $\cos \theta = c$ .

# Mixing angle $c$

For  $c=1$ ,

$W^+$  couples only to  $t$ - $\bar{u}$  and  $W^-$  to  $u$ - $\bar{t}$ .

For  $c < 1$ ,

All sorts of couplings are induced :  $W^+$  to  $t$ - $\bar{u}$ ,  $u$ - $\bar{t}$ ,  $t$ - $\bar{t}$ ,  $u$ - $\bar{u}$ .

It's possible only when there exists non-doublet Higgs.

We will work in a region around  $c=1$  to avoid like-sign top pairs.

# Top number : convenient for memory

Top number = +1 for top and  $W^+$ .

Top number = -1 for anti-top and  $W^-$ .

Each top number breaking by a unit 1 accompanies  $\sin \theta$  suppression (amplitude).

ex1)  $t\bar{t}$  production preserves top number.  $\propto s^0$

ex2) single top production is  $\propto s^1$

ex3) like-sign top pair is  $\propto s^2$

Thus, dangerous contributions are suppressed by  $s$ .

Many diagrams, but qualitatively t-channel exchange of W'

$$\frac{d\sigma_{(sG-tV)}}{d\cos\theta} = 2 \cdot \frac{\pi\beta}{18s} \alpha_S \alpha_X \xi_{tV} \cdot \frac{4(u_t^2 + sm_t^2) + 2\frac{m_t^2}{m_V^2}(t_t^2 + sm_t^2)}{s \cdot t_V}$$

$$\frac{d\sigma_{(tV-tV)}}{d\cos\theta} = \frac{\pi\beta}{8s} \alpha_X^2 \xi_{tV}^2 \cdot \frac{4u_t^2 + \frac{m_t^4}{m_V^4}(t_t^2 + 4sm_V^2)}{t_V^2}$$

$$\frac{d\sigma_{(tX-tY)}}{d\cos\theta} = 2 \cdot \frac{\pi\beta}{8s} \alpha_X^2 \xi_{tX} \xi_{tY} \cdot \frac{4u_t^2 + \frac{m_t^4}{m_X^2 m_Y^2} t_t^2 + 2\frac{m_t^4}{m_X^4} sm_X^2 + 2\frac{m_t^4}{m_Y^4} sm_Y^2}{t_X \cdot t_Y}$$

$$\frac{d\sigma_{(sX-tY)}}{d\cos\theta} = 2 \cdot \frac{\pi\beta}{24s} \alpha_X^2 \xi_{sX} \xi_{tY} \cdot \frac{4u_t^2 + 2\frac{m_t^2}{m_Y^2} sm_t^2}{s_X \cdot t_Y}$$

$$\frac{d\sigma_{(sV-sV)}}{d\cos\theta} = \frac{\pi\beta}{8s} \alpha_X^2 \xi_{sV}^2 \cdot \frac{4u_t^2}{s_V^2}$$

$$\frac{d\sigma_{(sX-sY)}}{d\cos\theta} = 2 \cdot \frac{\pi\beta}{8s} \alpha_X^2 \xi_{sX} \xi_{sY} \cdot \frac{4u_t^2}{s_X \cdot s_Y}$$



# Masses of gauge boson $W'$ and $Z'$

We want (light)  $W'$ . Can we heavy-decouple  $Z'$ ? Not likely.

$$M_{W'}^2 = g_X^2 v_T^2 \frac{T(T+1) - T_3^2}{2}, \quad M_{Z'}^2 = g_X^2 v_T^2 T_3^2,$$

For the vacuum with  $\langle T_3 = T \rangle$  and  $T \gg 1$ ,

$M_{W'}^2$  is propto  $T$

$M_{Z'}^2$  is propto  $T^2$

So possible to decouple  $Z'$  with a very large rep. But not beautiful.  $\Rightarrow$  We consider light  $W'$  and  $Z'$ .

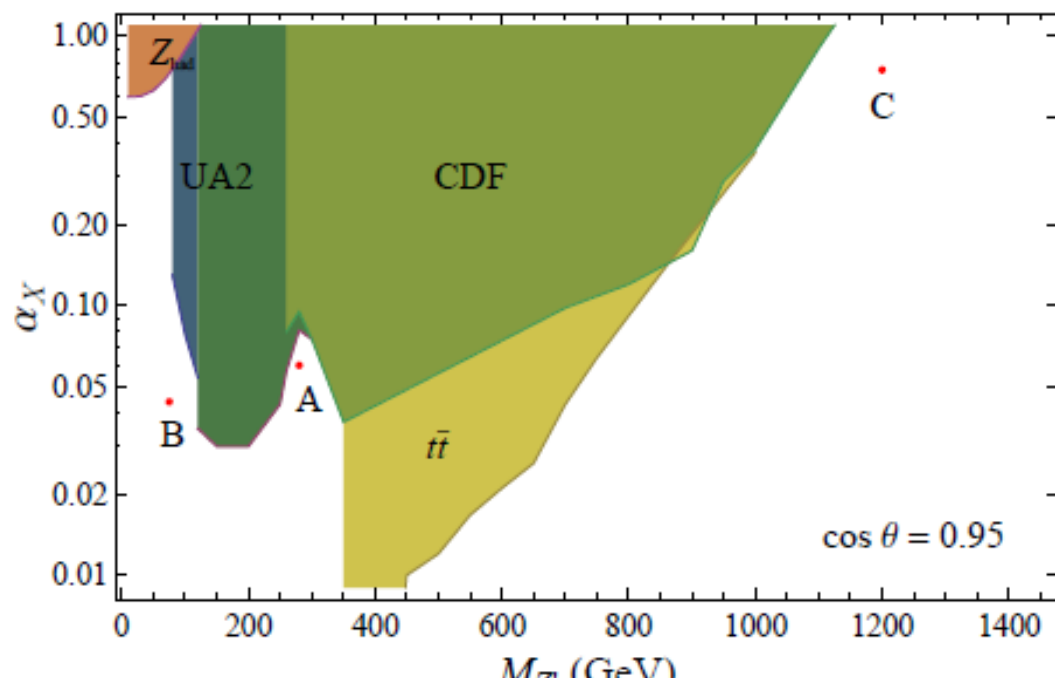
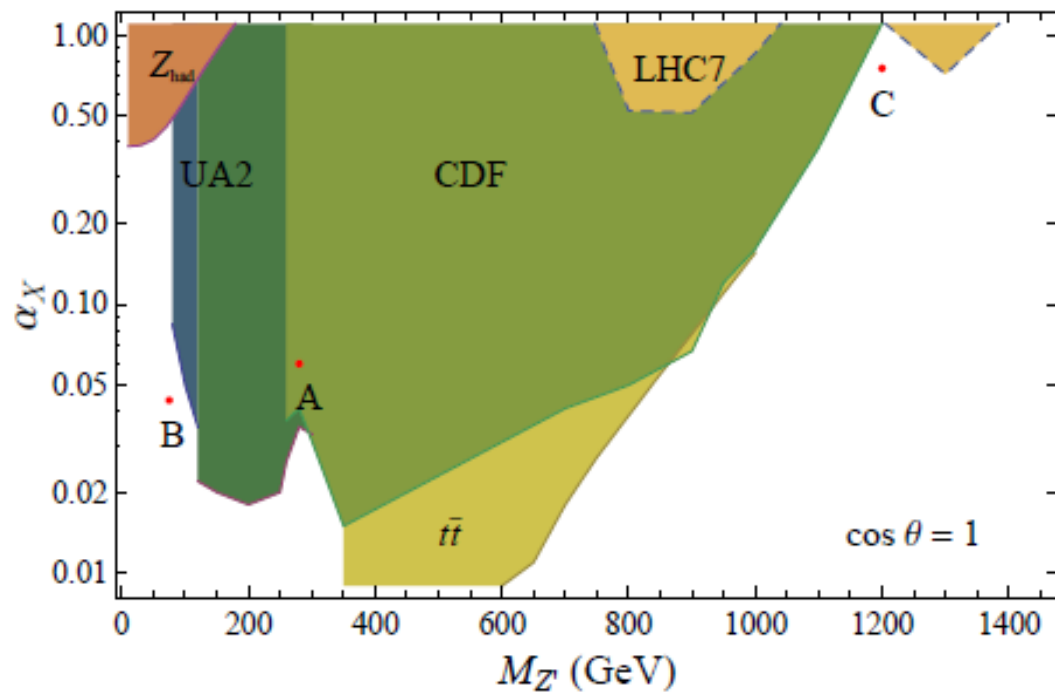
# Masses of gauge boson $W'$ and $Z'$

Effective Yukawa from Doublet Higgs  $\phi_D$ .

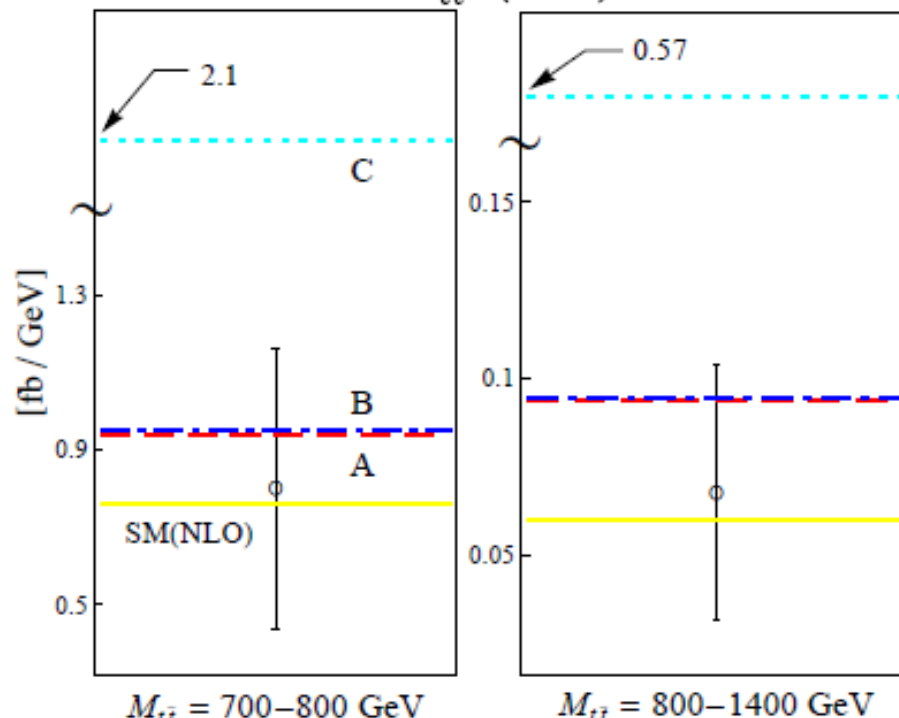
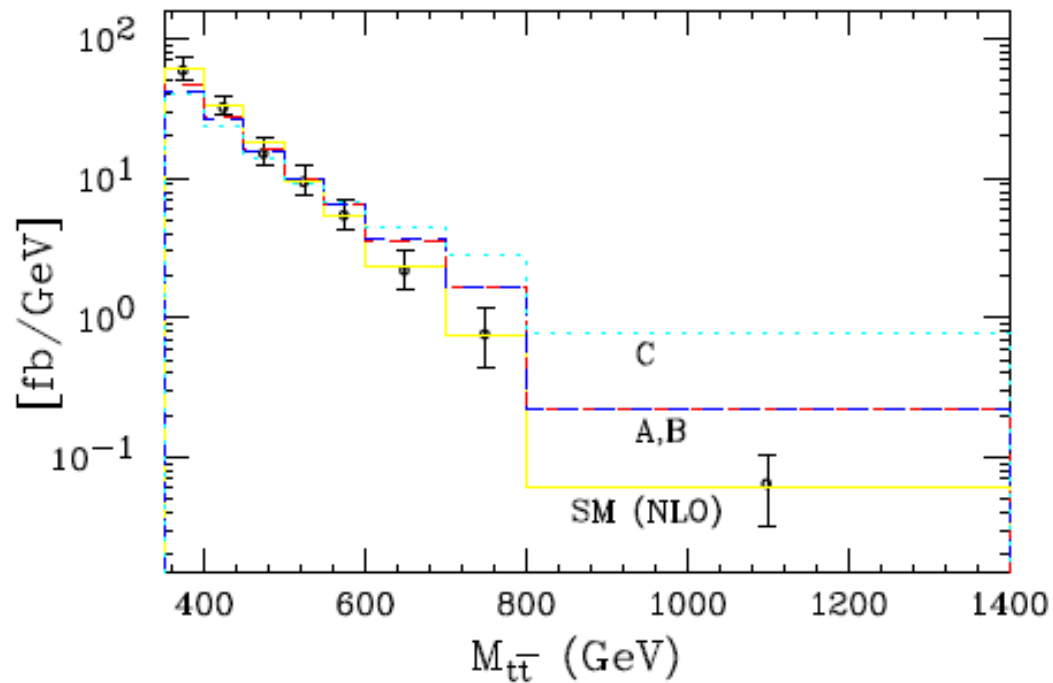
$$\Delta\mathcal{L} \ni \frac{(\lambda'_u)_i}{M} (\bar{Q}_i \cdot h_{SM}) (\phi_D \cdot q).$$

- Other Higgs rep does not allow this low-dimension Yukawa.
- Top Yukawa ( $v_D/M$ ) comes from this doublet Higgs.
- $M$  can't too above  $W'/Z'$  masses.
- Doublet vev gives common masses to all  $W'$  and  $Z'$ .  
=> We consider light  $W'$  and  $Z'$  s.

# Constraints on light gauge bosons



# Before and after the unfolding



# Inclusive $t\bar{t}$ cross sections (Tevatron)

	$\sigma(t\bar{t})_{thy}$	$A_{FB}^t$	$\sigma(t\bar{t})_{lj}$	$\sigma(t\bar{t})_{ll}$
CDF	$7.50 \pm 0.48$ pb [48]	$0.158 \pm 0.074$ [4]	$7.22 \pm 0.79$ pb [49]	$7.25 \pm 0.92$ pb [50, 51]
SM	7.34 pb	$0.058 \pm 0.009$	7.34 pb (normalized)	7.34 pb (normalized)
Model A	6.69 pb	0.14	7.0 pb	6.6 pb

TABLE II: Cross sections for point  $A$  at the Tevatron. The theoretical value of exclusive top pair cross section is shown in the column denoted  $\sigma(t\bar{t})_{thy}$ , where we apply a  $K$ -factor found by normalizing the LO SM to the approximated NNLO results 7.34 pb, averaged over three independent results [52–54]. The rest-frame asymmetry  $A_{FB}^t$  is also shown. Inclusive top pair cross sections in the semi-leptonic ( $\sigma(t\bar{t})_{lj}$ ) and dileptonic ( $\sigma(t\bar{t})_{ll}$ ) are obtained by applying CDF selection cuts [49–51] and by including other faking contributions, see text for detail.

# Inclusive $t\bar{t}$ cross sections (LHC7)

	$\sigma(t\bar{t})_{\ell j}$	$\sigma(t\bar{t})_{\ell\ell}$	$\sigma(t\bar{t})_{thy}$	$A_{boost}$
ATLAS [58]	$142^{+61}_{-46}$ pb	$151^{+86}_{-66}$ pb	$145^{+52}_{-41}$ pb	—
CMS [59]	—	$194_{\pm 79}$ pb	—	—
Model A	193 pb	177 pb	166 pb	6%

TABLE III: Detailed LHC7 cross section predictions for Point A. Exclusive  $pp \rightarrow t\bar{t}$  cross section is shown in the column denoted by  $\sigma(t\bar{t})_{thy}$ , with a  $K = 1.89$  normalizing LO SM to the approximate NNLO SM calculation  $\sigma(t\bar{t}) = 164.6^{+11.4}_{-15.7}$  pb [58, 60, 61]. The other two columns  $\sigma(t\bar{t})_{\ell j}$  and  $\sigma(t\bar{t})_{\ell\ell}$  represent predictions for observed inclusive cross-sections in the semi-leptonic and dileptonic channels. Here we have included possible “fake” contributions dominantly from the process  $\sigma(gu \rightarrow W't) = 47$  pb at the leading order and applied the cuts from the ATLAS analysis [58]. See text for more discussions.  $A_{boost}$  observable is defined in Eq. 4.

# Why non-zero theta ( $c < 1$ ) considered?

1. To relax dijet bound on  $Z'$ .  
(see previous figures)

2. To suppress faking contributions to inclusive xsec.

If instead,  $\cos \theta = 1$ , the top cross sections would be measured as  $\sigma(tt)_{l,j,u} = 8.0, 7.5$  pb with a (somewhat smaller) asymmetry,  $A_{FB}^t = 0.12$ . The decrease in the asymmetry is largely a result of contributions from the process  $gu \rightarrow W'^-t$ .

# c-dependence and like-sign top pairs again

$\cos \theta$ (Point A)	$\sigma(tt)_{\ell j}$	$\sigma(tt)_{\ell \ell}$	$\sigma(tt, \bar{t}\bar{t})$
0.9	175 pb	166 pb	3.90 pb
0.95	193 pb	177 pb	1.34 pb
1.0	233 pb	216 pb	0 pb

TABLE IV: The  $\cos \theta$  dependence of two relevant LHC signals (7 TeV) for a mass spectrum corresponding to Point A. Point A is defined with  $\cos \theta = 0.95$  but other values in the range of  $0.92 \lesssim \cos \theta \lesssim 0.98$  are also allowed. The inferred inclusive  $t\bar{t}$  cross-sections are shown in  $\sigma(t\bar{t})_{\ell j, \ell \ell}$ . Refer to table III for more details and corresponding LHC7 data. The inclusive like-sign top pair production (including  $tt, \bar{t}\bar{t}$  and vector boson decays to like-sign tops) is calculated at LO. Current deduced upper bound of  $\sigma(tt, \bar{t}\bar{t})$  from heavy exotic quark searches at LHC7 is about 5 pb at 95% CL.



# LHC Afb

With respect to the  $t\bar{t}$  boost direction,

$$A_{boost} = \frac{N(a > 0) - N(a < 0)}{N(a > 0) + N(a < 0)}, \quad a \equiv (y_t + y_{\bar{t}})(y_t - y_{\bar{t}}).$$

for  $M_{tt} > 450 \text{ GeV}$ .

- 25% chance of mismatch of q-direction and boost direction.
- $A_{boost} = 6\%$  is predicted (while  $A_{fb} = 15\%$ ,  $A_{fb+} = 30\%$ ).
- Roughly a few  $\text{fb}^{-1}$  of data is required to gain statistics.