

# Thermodynamic uncertainty relation of interacting oscillators in synchrony

Sangwon Lee<sup>1</sup>, Changbong Hyeon<sup>2</sup> and Junghyo Jo<sup>2</sup>

<sup>1</sup> Department of Physics and Astronomy, Seoul National University, Seoul, Korea

<sup>2</sup>Korea Institute for Advanced Study, Seoul, Korea

The thermodynamic uncertainty relation sets the minimal bound of the cost-precision trade-off relation for dissipative processes. Examining the dynamics of an internally coupled system that is driven by a constant thermodynamic force, we however find that the trade-off relation of a sub-system is not constrained by the minimal bound of conventional uncertainty relation. We made our point explicit by using an exactly solvable model of interacting oscillators. As the number ( $N$ ) of interacting oscillators increases, the uncertainty bound of individual oscillators is reduced to  $2k_B T/N$  upon full synchronization under strong coupling. The cost-precision trade-off for the sub-system is particularly relevant for sub-cellular processes where collective dynamics emerges from multiple energy-expending components interacting with each other.

† S. Lee, C. Hyeon and J. Jo, arXiv:1804.10362 (2018).